

Exotic sources of electroweak symmetry breaking

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The Standard Model as written down by Weinberg in 1967 implements electroweak symmetry breaking using a spin-zero doublet of $SU(2)_L$:

$$\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}, \qquad \langle \Phi \rangle = \begin{pmatrix} 0 \\ v/\sqrt{2} \end{pmatrix}$$

This is the simplest possible option – the minimum nontrivial "charge" under $SU(2)_L$.

Q: Could there be contributions to electroweak symmetry breaking from scalars in larger ("exotic") representations of $SU(2)_L$?

Objectives:

- Identify all possible models
- Find generic search strategies to constrain exotic vevs

Outline

Requirements for a sensible theory

- allowed reps from perturbative unitarity
- allowed vevs from rho parameter
- some model building

Georgi-Machacek model and constraints from VBF $ightarrow H_5
ightarrow VV$

Constraining other models (GM-like; septet)

Promising channels at lower masses

Conclusions

How high an isospin is ok?

Higher isospin \rightarrow higher maximum "weak charge" (gT^3 , etc.) Higher isospin \rightarrow higher multiplicity of scalars

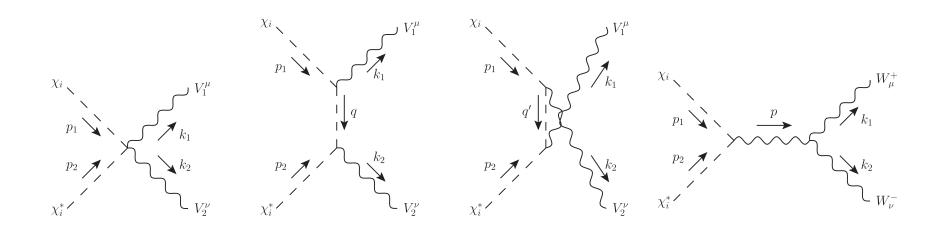
Unitarity of the scattering matrix:

$$|\operatorname{Re} a_{\ell}| \le 1/2,$$
 $\mathcal{M} = 16\pi \sum_{\ell} (2\ell + 1) a_{\ell} P_{\ell}(\cos \theta)$

Scattering of longitudinally-polarized Ws & Zs famously used to put upper bound on Higgs mass Lee, Quigg & Thacker 1977

To bound the strength of the weak charge, consider *transversely* polarized Ws & Zs (the ordinary gauge modes).

Too strong a charge \rightarrow nonperturbative



$$a_0 = \frac{g^2}{16\pi} \frac{(n^2 - 1)\sqrt{n}}{2\sqrt{3}}$$
 complex χ , $n = 2T + 1$

- Real scalar multiplet: divide by $\sqrt{2}$ to account for smaller multiplicity
- More than one multiplet: add a_0 's in quadrature
- Complex multiplet $\Rightarrow T \leq 7/2$ (8-plet)
- Real multiplet $\Rightarrow T \leq 4$ (9-plet)
- Constraints tighter if more than one large multiplet

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Exotic EWSB

| \overline{T} | \overline{Y} |
|----------------|----------------|
| 1/2 | 1/2 |
| 1 | 0 |
| 1 | 1 |
| 3/2 | 1/2 |
| 3/2 | 3/2 |
| 2 | O |
| 2 | 1 |
| 2 | 2 |
| 5/2 | 1/2 |
| 5/2 | 3/2 |
| 5/2 | 5/2 |
| 3 | Ó |
| 3 | 1 |
| 3 | 2 |
| 3 | 3 |
| 7/2 | 1/2 |
| 7/2 | 3/2 |
| 7/2 | 5/2 |
| 7/2 | 7/2 |
| 4 | 0 |
| | |

Complete list of (perturbative) scalars that can contribute to EWSB:

- Singlet $T=\mathbf{0},\ Y=\mathbf{0}$ doesn't contribute to EWSB
- Must have a neutral component $(Q = T^3 + Y = 0)$
- $Y \rightarrow -Y$ is just the conjugate multiplet

How much can these contribute to EWSB?

$$\mathcal{L} \supset \frac{g^2}{2} \left\{ \langle X \rangle^{\dagger} (T^+ T^- + T^- T^+) \langle X \rangle \right\} W_{\mu}^+ W^{-\mu}$$

$$+ \frac{(g^2 + g'^2)}{2} \left\{ \langle X \rangle^{\dagger} (T^3 T^3 + Y^2) \langle X \rangle \right\} Z_{\mu} Z^{\mu} + \cdots$$

Must have at least one doublet to give masses to SM fermions

$$M_W^2 = \left(\frac{g^2}{4}\right) \left[v_\phi^2 + a\langle X_0 \rangle^2\right]$$

 $M_Z^2 = \left(\frac{g^2 + g'^2}{4}\right) \left[v_\phi^2 + b\langle X_0 \rangle^2\right]$

where $\langle \Phi_{\text{SM}} \rangle = (0, v_{\phi}/\sqrt{2})^T$ and

$$a = 4 \left[T(T+1) - Y^2 \right] c$$

$$b = 8Y^2$$

c=1 for complex and c=1/2 for real multiplet

SM Higgs doublet: a=b=2 (cancels $(1/\sqrt{2})^2$ in $\langle \Phi_0 \rangle^2$)

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Exotic EWSB

Extremely strong constraint from low-energy weak interaction strength measurements:

$$\rho \equiv \frac{\text{weak neutral current}}{\text{weak charged current}} = \frac{(g^2 + g'^2)/M_Z^2}{g^2/M_W^2} = \frac{v_\phi^2 + a\langle X_0 \rangle^2}{v_\phi^2 + b\langle X_0 \rangle^2}$$

$$a = 4 \left[T(T+1) - Y^2 \right] c$$
$$b = 8Y^2$$

Experiment: (Moriond 2017, Erler 1704.08330)

$$\rho = 1.00036 \pm 0.00019$$

| T | \overline{Y} | \overline{a} | b | δho | $\delta M_W^2 _{\sf max}$ | $\delta M_Z^2 { m max} $ |
|-----|----------------|----------------|----|--------------|----------------------------|---------------------------|
| 1/2 | 1/2 | 2 | 2 | 0 | _ | _ |
| 1 | 0 | 4 | 0 | + | 0.068% | O |
| 1 | 1 | 4 | 8 | _ | 0.021% | 0.042% |
| 3/2 | 1/2 | 14 | 2 | + | 0.079% | 0.011% |
| 3/2 | 3/2 | 6 | 18 | _ | 0.011% | 0.032% |
| 2 | 0 | 12 | 0 | + | 0.068% | 0 |
| 2 | 1 | 20 | 8 | + | 0.113% | 0.045% |
| 2 | 2 | 8 | 32 | _ | 0.007% | 0.028% |
| 5/2 | 1/2 | 34 | 2 | + | 0.072% | 0.004% |
| 5/2 | 3/2 | 26 | 18 | + | 0.221% | 0.153% |
| 5/2 | 5/2 | 10 | 50 | _ | 0.005% | 0.026% |
| 3 | 0 | 24 | 0 | + | 0.068% | 0 |
| 3 | 1 | 44 | 8 | + | 0.083% | 0.015% |
| 3 | 2 | 32 | 32 | 0 | _ | _ |
| 3 | 3 | 12 | 72 | _ | 0.004% | 0.025% |
| 7/2 | 1/2 | 62 | 2 | + | 0.070% | 0.002% |
| 7/2 | 3/2 | 54 | 18 | + | 0.102% | 0.034% |
| 7/2 | 5/2 | 38 | 50 | _ | 0.067% | 0.088% |
| 7/2 | 7/2 | 14 | 98 | _ | 0.004% | 0.025% |
| 4 | 0 | 40 | 0 | + | 0.068% | 0 |

work in progress

with Jesi Goodman

| T | Y | a | b | δho | $\delta M_W^2 _{\sf max}$ | $\delta M_Z^2 $ max | |
|-----|-----|----|----|--------------|----------------------------|----------------------|---------|
| 1/2 | 1/2 | 2 | 2 | 0 | _ | _ | doublet |
| 1 | 0 | 4 | 0 | + | 0.068% | O | |
| 1 | 1 | 4 | 8 | | 0.021% | 0.042% | |
| 3/2 | 1/2 | 14 | 2 | + | 0.079% | 0.011% | |
| 3/2 | 3/2 | 6 | 18 | _ | 0.011% | 0.032% | |
| 2 | 0 | 12 | 0 | + | 0.068% | 0 | |
| 2 | 1 | 20 | 8 | + | 0.113% | 0.045% | |
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| 5/2 | 3/2 | 26 | 18 | + | 0.221% | 0.153% | |
| 5/2 | 5/2 | 10 | 50 | _ | 0.005% | 0.026% | |
| 3 | 0 | 24 | 0 | + | 0.068% | 0 | |
| 3 | 1 | 44 | 8 | + | 0.083% | 0.015% | |
| 3 | 2 | 32 | 32 | 0 | _ | _ | septet |
| 3 | 3 | 12 | 72 | _ | 0.004% | 0.025% | |
| 7/2 | 1/2 | 62 | 2 | + | 0.070% | 0.002% | |
| 7/2 | 3/2 | 54 | 18 | + | 0.102% | 0.034% | |
| 7/2 | 5/2 | 38 | 50 | _ | 0.067% | 0.088% | |
| 7/2 | 7/2 | 14 | 98 | _ | 0.004% | 0.025% | |
| 4 | 0 | 40 | 0 | + | 0.068% | 0 | |

| \overline{T} | \overline{Y} | \overline{a} | b | δho | $\delta M_W^2 _{\sf max}$ | $\delta M_Z^2 _{\sf max}$ |
|----------------|----------------|----------------|----|--------------|----------------------------|----------------------------|
| 1/2 | 1/2 | 2 | 2 | 0 | _ | _ |
| 1 | O | 4 | 0 | + | 0.068% | 0 |
| 1 | 1 | 4 | 8 | _ | 0.021% | 0.042% |
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| 3 | 2 | 32 | 32 | 0 | _ | _ |
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| 7/2 | 5/2 | 38 | 50 | _ | 0.067% | 0.088% |
| 7/2 | 7/2 | 14 | 98 | _ | 0.004% | 0.025% |
| 4 | 0 | 40 | 0 | + | 0.068% | 0 |

Include both reps with $v_1 = v_2$:

$$\rho = \frac{v_{\phi}^2 + a_1 v_1^2 + a_2 v_2^2}{v_{\phi}^2 + b_1 v_1^2 + b_2 v_2^2}$$

$$\sum a = 8$$

$$\sum b = 8$$

| \overline{T} | Y | \overline{a} | b | δho | $\delta M_W^2 _{\sf max}$ | $\delta M_Z^2 _{\sf max}$ |
|----------------|-----|----------------|----|--------------|----------------------------|----------------------------|
| 1/2 | 1/2 | 2 | 2 | 0 | _ | _ |
| 1 | O | 4 | 0 | + | 0.068% | 0 |
| 1 | 1 | 4 | 8 | _ | 0.021% | 0.042% |
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| 2 | O | 12 | 0 | + | 0.068% | 0 |
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| 3 | O | 24 | 0 | + | 0.068% | 0 |
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| 3 | 2 | 32 | 32 | 0 | _ | _ |
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| 7/2 | 5/2 | 38 | 50 | _ | 0.067% | 0.088% |
| 7/2 | 7/2 | 14 | 98 | _ | 0.004% | 0.025% |
| 4 | 0 | 40 | 0 | + | 0.068% | 0 |

Include both reps with $v_1 = v_2$:

$$\rho = \frac{v_{\phi}^2 + a_1 v_1^2 + a_2 v_2^2}{v_{\phi}^2 + b_1 v_1^2 + b_2 v_2^2}$$

$$\sum a = 20$$

$$\sum b = 20$$

| \overline{T} | \overline{Y} | \overline{a} | b | δho | $\delta M_W^2 _{\sf max}$ | $\delta M_Z^2 _{\sf max}$ |
|----------------|----------------|----------------|----|--------------|----------------------------|----------------------------|
| 1/2 | 1/2 | 2 | 2 | 0 | _ | _ |
| 1 | 0 | 4 | 0 | + | 0.068% | O |
| 1 | 1 | 4 | 8 | _ | 0.021% | 0.042% |
| 3/2 | 1/2 | 14 | 2 | + | 0.079% | 0.011% |
| 3/2 | 3/2 | 6 | 18 | _ | 0.011% | 0.032% |
| 2 | 0 | 12 | 0 | + | 0.068% | 0 |
| 2 | 1 | 20 | 8 | + | 0.113% | 0.045% |
| 2 | 2 | 8 | 32 | _ | 0.007% | 0.028% |
| 5/2 | 1/2 | 34 | 2 | + | 0.072% | 0.004% |
| 5/2 | 3/2 | 26 | 18 | + | 0.221% | 0.153% |
| 5/2 | 5/2 | 10 | 50 | _ | 0.005% | 0.026% |
| 3 | 0 | 24 | 0 | + | 0.068% | 0 |
| 3 | 1 | 44 | 8 | + | 0.083% | 0.015% |
| 3 | 2 | 32 | 32 | 0 | _ | _ |
| 3 | 3 | 12 | 72 | _ | 0.004% | 0.025% |
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| 7/2 | 3/2 | 54 | 18 | + | 0.102% | 0.034% |
| 7/2 | 5/2 | 38 | 50 | _ | 0.067% | 0.088% |
| 7/2 | 7/2 | 14 | 98 | _ | 0.004% | 0.025% |
| 4 | 0 | 40 | 0 | + | 0.068% | 0 |

Include all 3 reps with $v_1 = v_2 = v_3$:

$$\rho = \frac{v_\phi^2 + \sum a_i v_i^2}{v_\phi^2 + \sum b_i v_i^2}$$

$$\sum a = 40$$

$$\sum a = 40$$
$$\sum b = 40$$

| \overline{T} | Y | \overline{a} | b | δho | $\delta M_W^2 _{\sf max}$ | $\delta M_Z^2 _{\sf max}$ |
|----------------|-----|----------------|----|--------------|----------------------------|----------------------------|
| 1/2 | 1/2 | 2 | 2 | 0 | _ | _ |
| 1 | 0 | 4 | 0 | + | 0.068% | O |
| 1 | 1 | 4 | 8 | _ | 0.021% | 0.042% |
| 3/2 | 1/2 | 14 | 2 | + | 0.079% | 0.011% |
| 3/2 | 3/2 | 6 | 18 | _ | 0.011% | 0.032% |
| 2 | 0 | 12 | 0 | + | 0.068% | O |
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| 2 | 2 | 8 | 32 | _ | 0.007% | 0.028% |
| 5/2 | 1/2 | 34 | 2 | + | 0.072% | 0.004% |
| 5/2 | 3/2 | 26 | 18 | + | 0.221% | 0.153% |
| 5/2 | 5/2 | 10 | 50 | _ | 0.005% | 0.026% |
| 3 | 0 | 24 | 0 | + | 0.068% | 0 |
| 3 | 1 | 44 | 8 | + | 0.083% | 0.015% |
| 3 | 2 | 32 | 32 | 0 | _ | _ |
| 3 | 3 | 12 | 72 | _ | 0.004% | 0.025% |
| 7/2 | 1/2 | 62 | 2 | + | 0.070% | 0.002% |
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| 7/2 | 5/2 | 38 | 50 | _ | 0.067% | 0.088% |
| 7/2 | 7/2 | 14 | 98 | _ | 0.004% | 0.025% |
| 4 | 0 | 40 | 0 | + | 0.068% | 0 |

Include all 3 reps with $v_1 = v_2 = v_3$:

$$\rho = \frac{v_{\phi}^2 + \sum a_i v_i^2}{v_{\phi}^2 + \sum b_i v_i^2}$$

$$\sum a = 70$$

$$\sum a = 70$$

$$\sum b = 70$$

Complete list of models with sizable exotic sources of EWSB:

- 1) Doublet + septet (T,Y)=(3,2): Scalar septet model Hisano & Tsumura, 1301.6455; Kanemura, Kikuchi & Yagyu, 1301.7303
- 2) Doublet + triplets (1,0)+(1,1): Georgi-Machacek model (ensure triplet vevs are equal using a global "custodial" symmetry)

 Georgi & Machacek 1985; Chanowitz & Golden 1985
- 3) Doublet + quartets $\left(\frac{3}{2}, \frac{1}{2}\right) + \left(\frac{3}{2}, \frac{3}{2}\right)$: Generalized Georgi-
- 4) Doublet + quintets (2,0)+(2,1)+(2,2): Machacek models
- 5) Doublet + sextets $(\frac{5}{2}, \frac{1}{2}) + (\frac{5}{2}, \frac{3}{2}) + (\frac{5}{2}, \frac{5}{2})$:

(ensure exotics' vevs are equal using a global "custodial" symmetry)

Galison 1984; Robinett 1985; HEL 1999; Chang et al 2012; HEL & Rentala 2015 Larger than sextets \rightarrow too many large multiplets, violates perturbativity!

Can also have duplications, combinations \rightarrow ignore that here.

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- allowed reps from perturbative unitarity
- allowed vevs from rho parameter
- some model building

Georgi-Machacek model and constraints from VBF $ightarrow H_5
ightarrow VV$

Constraining other models (GM-like; septet)

Promising channels at lower masses

Conclusions

Georgi-Machacek model

Georgi & Machacek 1985; Chanowitz & Golden 1985

SM Higgs (bi-)doublet + triplets (1,0) + (1,1) in a bi-triplet:

$$\Phi = \begin{pmatrix} \phi^{0*} & \phi^{+} \\ -\phi^{+*} & \phi^{0} \end{pmatrix} \qquad X = \begin{pmatrix} \chi^{0*} & \xi^{+} & \chi^{++} \\ -\chi^{+*} & \xi^{0} & \chi^{+} \\ \chi^{++*} & -\xi^{+*} & \chi^{0} \end{pmatrix}$$

Global $SU(2)_L \times SU(2)_R \rightarrow \text{custodial symmetry } \langle \chi^0 \rangle = \langle \xi^0 \rangle \equiv v_{\chi}$

Physical spectrum:

Bidoublet: $2 \otimes 2 \rightarrow 1 \oplus 3$

Bitriplet: $3 \otimes 3 \rightarrow 1 \oplus 3 \oplus 5$

- Two custodial singlets mix $\rightarrow h^0$, H^0 m_h , m_H Usually identify $h^0 = h(125)$
- Two custodial triplets mix \to (H_3^+, H_3^0, H_3^-) m_3 + Goldstones Phenomenology very similar to H^\pm, A^0 in 2HDM Type I, $\tan \beta \to \cot \theta_H$
- Custodial fiveplet $(H_5^{++}, H_5^+, H_5^0, H_5^-, H_5^{--})$ $m_5 \leftarrow \star$ Fermiophobic; H_5VV couplings $\propto s_H \equiv \sqrt{8}v_\chi/v_{\rm SM}$ $s_H^2 \equiv$ exotic fraction of M_W^2 , M_Z^2

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Exotic EWSB

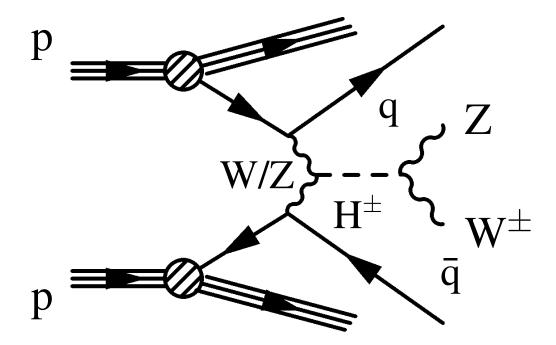
Smoking-gun processes:

$$VBF \rightarrow H_5^{\pm\pm} \rightarrow W^{\pm}W^{\pm}$$

VBF + like-sign dileptons + MET

$$VBF \to H_5^{\pm} \to W^{\pm}Z$$

VBF + $qq\ell\ell$; VBF + 3ℓ + MET



Cross section $\propto s_H^2 \equiv$ fraction of M_W^2, M_Z^2 due to exotic scalars

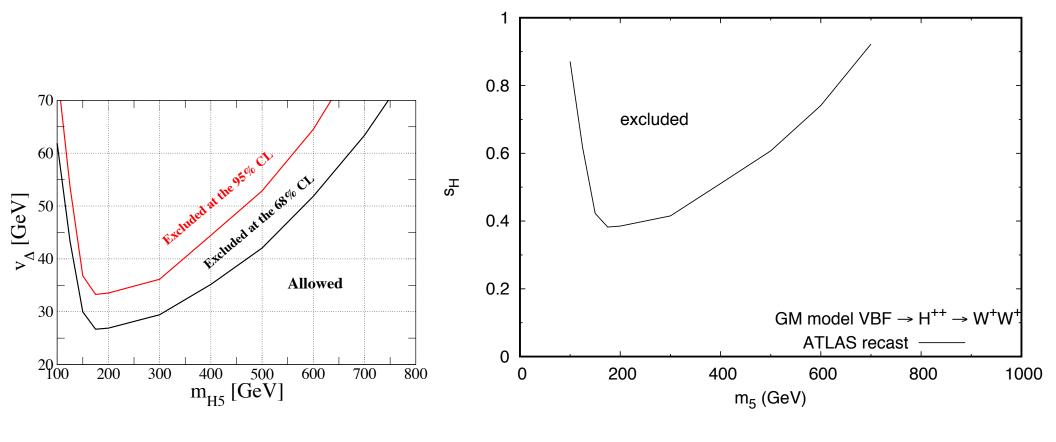
Searches

SM VBF $\rightarrow W^{\pm}W^{\pm} \rightarrow \ell^{\pm}\ell^{\pm}$ + MET cross section measurement

ATLAS Run 1 1405.6241, PRL 2014

Recast to constrain VBF $\rightarrow H_5^{\pm\pm} \rightarrow W^{\pm}W^{\pm} \rightarrow \ell^{\pm}\ell^{\pm}$ + MET

Chiang, Kanemura, Yagyu, 1407.5053



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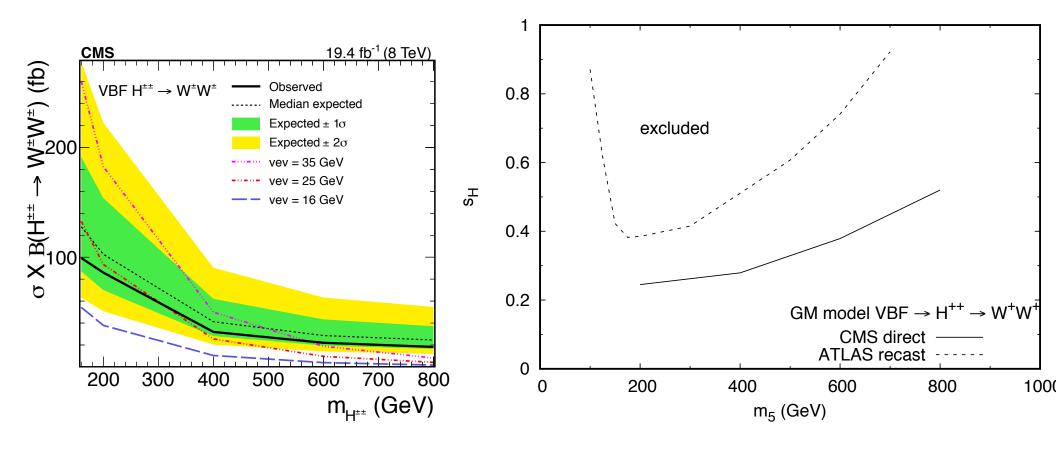
Exotic EWSB

TRIUMF 2018 Feb 19

Searches

VBF
$$H_5^{\pm\pm} \rightarrow W^{\pm}W^{\pm} \rightarrow \ell^{\pm}\ell^{\pm} + MET$$
 (CMS Run 1)

CMS 1410.6315, PRL 2015



Translated using VBF $ightarrow H^{\pm\pm}$ cross sections from LHCHXSWG-2015-001

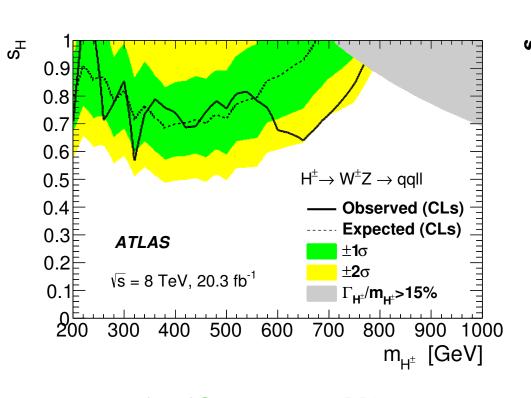
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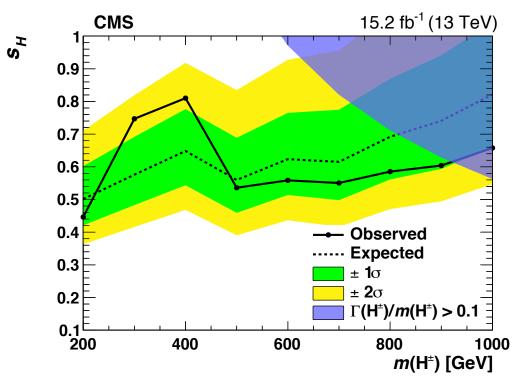
Exotic EWSB

Searches

VBF
$$H_5^{\pm} \rightarrow W^{\pm}Z \rightarrow qq\ell\ell$$
 (ATLAS Run 1)

VBF
$$H_5^{\pm} \rightarrow W^{\pm}Z \rightarrow 3\ell + MET$$
 (CMS Run 2)





ATLAS 1503.04233, PRL 2015

CMS 1705.02942, PRL 2017

(Not yet as constraining as VBF $H_5^{\pm\pm} \to W^{\pm}W^{\pm} \to \ell^{\pm}\ell^{\pm} + \text{MET}$)

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Exotic EWSB

One more constraint from $VV \rightarrow H_5 \rightarrow VV$: unitarity!

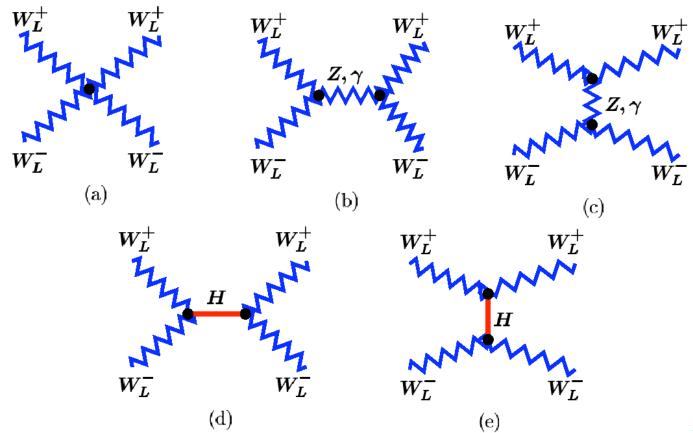


figure: S. Chivukula

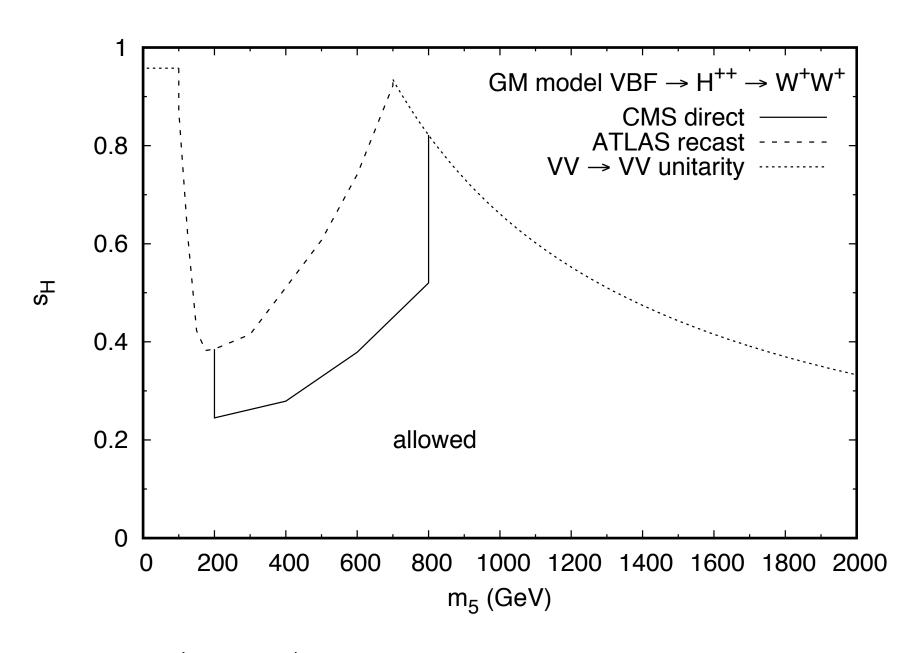
SM: $m_h^2 < 16\pi v^2/5 \simeq (780~{
m GeV})^2$ Lee, Quigg & Thacker 1977

GM: $s_H^2 < 12\pi v^2/5m_5^2 \simeq (675 \text{ GeV}/m_5)^2$

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Exotic EWSB

One more constraint from $VV \rightarrow H_5 \rightarrow VV$: unitarity!



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Generalized Georgi-Machacek models

Galison 1984; Robinett 1985; HEL 1999; Chang et al 2012; HEL & Rentala 2015

- 3) Doublet + quartets $(\frac{3}{2}, \frac{1}{2}) + (\frac{3}{2}, \frac{3}{2})$ 4) Doublet + quintets (2,0) + (2,1) + (2,2)
- 5) Doublet + sextets $(\frac{5}{2}, \frac{1}{2}) + (\frac{5}{2}, \frac{3}{2}) + (\frac{5}{2}, \frac{5}{2})$

Replace the GM bi-triplet with a bi-n-plet

 \implies "GGMn"

Bi-doublet: $2 \otimes 2 \rightarrow 1 \oplus 3$

Bi-triplet: $3 \otimes 3 \rightarrow 1 \oplus 3 \oplus 5$

Bi-quartet: $4 \otimes 4 \rightarrow 1 \oplus 3 \oplus 5 \oplus 7$

Bi-pentet: $5 \otimes 5 \rightarrow 1 \oplus 3 \oplus 5 \oplus 7 \oplus 9$

Bi-sextet: $6 \otimes 6 \rightarrow 1 \oplus 3 \oplus 5 \oplus 7 \oplus 9 \oplus 11$

Larger bi-n-plets forbidden by perturbativity of weak charges!

All models contain custodial fiveplet $(H_5^{++}, H_5^+, H_5^0, H_5^-, H_5^{--})$

Compositions & couplings of fiveplet states are determined by the global symmetry!

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Exotic EWSB

Generalized Georgi-Machacek models

Galison 1984; Robinett 1985; HEL 1999; Chang et al 2012; HEL & Rentala 2015

Custodial-fiveplet is fermiophobic; couples to VV:

$$H_5^0 W_\mu^+ W_\nu^- : \qquad -i \frac{2 M_W^2}{v} \frac{g_5}{\sqrt{6}} g_{\mu\nu},$$

$$H_5^0 Z_\mu Z_\nu : \qquad i \frac{2 M_Z^2}{v} \sqrt{\frac{2}{3}} g_5 g_{\mu\nu},$$

$$H_5^+ W_\mu^- Z_\nu : \qquad -i \frac{2 M_W M_Z}{v} \frac{g_5}{\sqrt{2}} g_{\mu\nu},$$

$$H_5^{++} W_\mu^- W_\nu^- : \qquad i \frac{2 M_W^2}{v} g_5 g_{\mu\nu},$$

$$GM3 : \qquad g_5 = \sqrt{24/5} s_H$$

$$GGM4 : \qquad g_5 = \sqrt{42/5} s_H$$

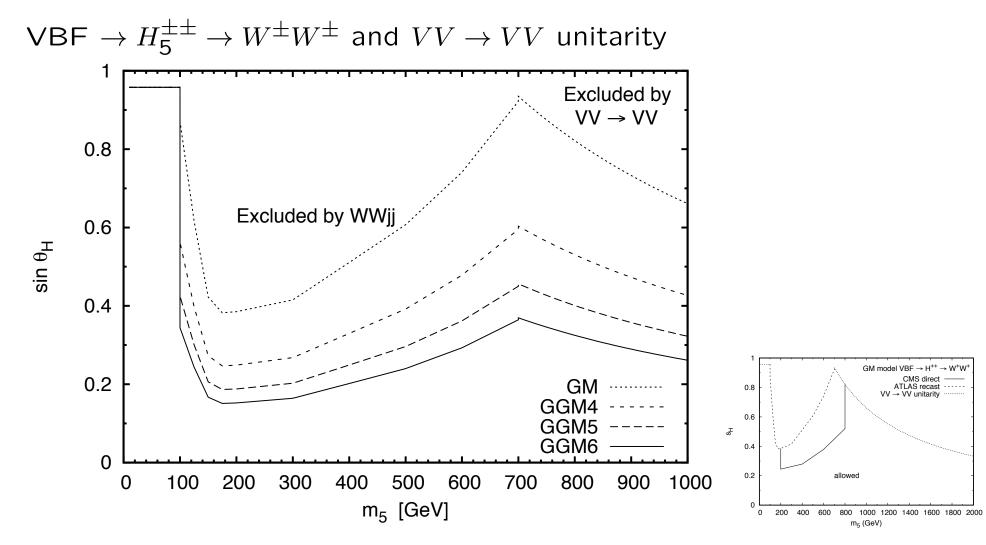
$$GGM6 : \qquad g_5 = \sqrt{64/5} s_H$$

 $s_H^2 =$ fraction of M_W^2, M_Z^2 from exotic scalars

GGM6:

Generalized Georgi-Machacek models

Galison 1984; Robinett 1985; HEL 1999; Chang et al 2012; HEL & Rentala 2015



HEL & Rentala, 1502.01275

(plot needs updating: CMS Run 1 direct search not shown)

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Exotic EWSB

Scalar septet model (T, Y) = (3, 2)

Hisano & Tsumura, 1301.6455; Kanemura, Kikuchi & Yagyu, 1301.7303

$$\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}, \qquad X = \begin{pmatrix} \chi^{+5} \\ \chi^{+4} \\ \chi^{+3} \\ \chi^{+2} \\ \chi^{+1} \\ \chi^0 \\ \chi^{-1} \end{pmatrix}.$$

Detailed pheno study in Alvarado, Lehman & Ostdiek, 1404.3208:

- h^0 couplings \rightarrow upper bound on septet vev
- S and T parameters \rightarrow septet states must be fairly degenerate
- LHC SUSY searches (2SSL, 3L) + inclusive septet pair production \rightarrow lower bound on common septet mass

Scalar septet model (T, Y) = (3, 2)

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$$\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}, \qquad X = \begin{pmatrix} \chi^{+5} \\ \chi^{+4} \\ \chi^{+3} \\ \chi^{+2} \\ \chi^{+1} \\ \chi^0 \\ \chi^{-1} \end{pmatrix}.$$

 $\rho=1$, yet there is no custodial symmetry in the scalar spectrum

- $H^{++} = \chi^{+2}$: analogue of H_5^{++}
- ϕ^+ , χ^{+1} , $(\chi^{-1})^*$ mix: no purely fermiophobic analogue of H_5^+
- Only 2 CP-even neutral scalars $(h^0,\,H^0)$: no analogue of H_5^{0}

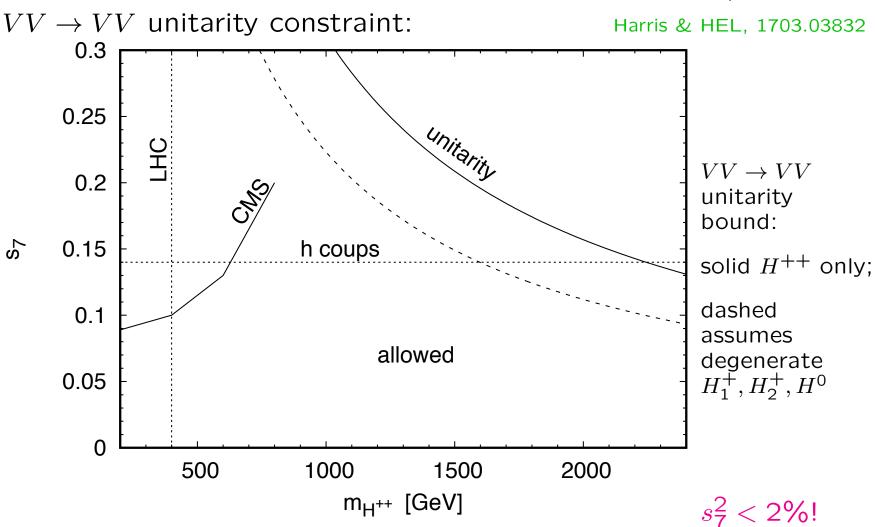
$$H^{++}W_{\mu}^{-}W_{\nu}^{-}: i\frac{2M_{W}^{2}}{v}\sqrt{15}s_{7}g_{\mu\nu},$$

 $s_7^2 =$ fraction of M_W^2, M_Z^2 from septet vev

Scalar septet model (T, Y) = (3, 2)

Hisano & Tsumura, 1301.6455; Kanemura, Kikuchi & Yagyu, 1301.7303

Translate CMS VBF $\rightarrow H^{++} \rightarrow W^+W^+$ direct search,



Dots: LHC SUSY searches, h^0 couplings Alvarado, Lehman & Ostdiek, 1404.3208

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Outline

Requirements for a sensible theory

- allowed reps from perturbative unitarity
- allowed vevs from rho parameter
- some model building

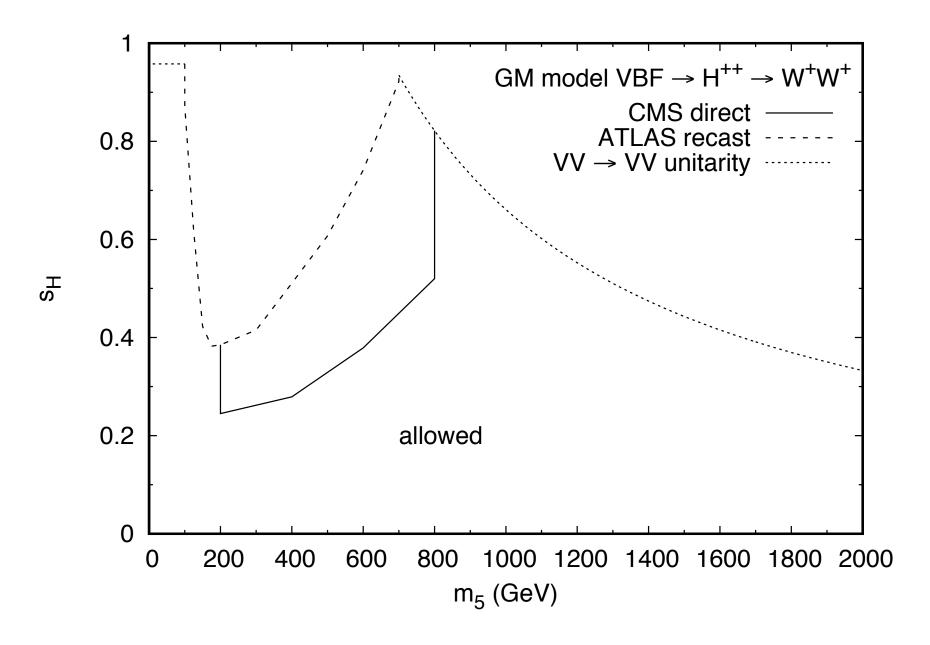
Georgi-Machacek model and constraints from VBF $ightarrow H_5
ightarrow VV$

Constraining other models (GM-like; septet)

Promising channels at lower masses

Conclusions

Constraints on GM model at low mass?



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Constraints on GM model at low mass?

Studied already:

- Drell-Yan
$$pp \to H_5^{++}H_5^{--} + H_5^{\pm\pm}H_5^{\mp}$$
, $H_5^{\pm\pm} \to \text{like-sign dimuons}$

- LEP $e^+e^- o ZH_5^0$, recoil method (independent of H_5^0 decay)
- LEP $e^+e^- \rightarrow ZH_5^0$, $H_5^0 \rightarrow \gamma\gamma$ (fermiophobic!)

For the future:

- Drell-Yan $pp o H_5^0 H_5^\pm$, $H_5^0 o \gamma\gamma$
- Drell-Yan $pp \to H_5^\pm H_5^0 + H_5^\pm H_5^\mp + H_5^\pm H_5^{\mp\mp}$, $H_5^\pm \to W^\pm \gamma$

Drell-Yan $pp \to H_5^{++}H_5^{--} + H_5^{\pm\pm}H_5^{\mp}$, $H_5^{\pm\pm} \to \text{like-sign dimuons}$

ATLAS Run 1 anomalous like-sign dimuon search ATLAS, 1412.0237

Recast for $pp \to H^{\pm\pm}H^{\mp\mp} + H^{\pm\pm}H^{\mp}$ in Higgs Triplet Model Kanemura, Kikuchi, Yagyu & Yokoya, 1412.7603

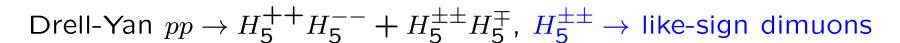
Adapt to generalized GM models using

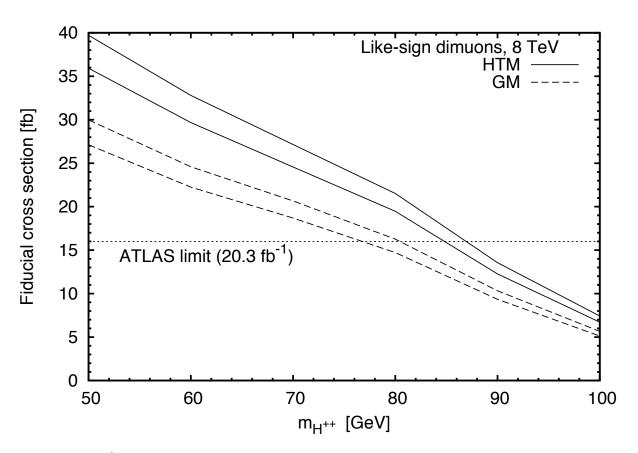
$$\sigma_{\text{tot}}^{\text{NLO}}(pp \to H_5^{++}H_5^{--})_{\text{GM}} = \sigma_{\text{tot}}^{\text{NLO}}(pp \to H^{++}H^{--})_{\text{HTM}},$$

$$\sigma_{\text{tot}}^{\text{NLO}}(pp \to H_5^{\pm\pm}H_5^{\mp})_{\text{GM}} = \frac{1}{2}\sigma_{\text{tot}}^{\text{NLO}}(pp \to H^{\pm\pm}H^{\mp})_{\text{HTM}}.$$

HEL & Rentala, 1502.01275

Take advantage of mass degeneracy of all H_5 states.





 $\Rightarrow m_5 \gtrsim$ 76 GeV, no s_H dependence!

HEL & Rentala, 1502.01275

Assumes no decays $H_5^{\pm\pm} \to H_3^{\pm} W^{\pm}$:

Constraint on $e^+e^- \to H_3^+ H_3^-$ in Type-I 2HDM LEP, hep-ex/0107031 $m_3 > 78.6$ GeV assuming no decays $H_3 \to H_5 V$

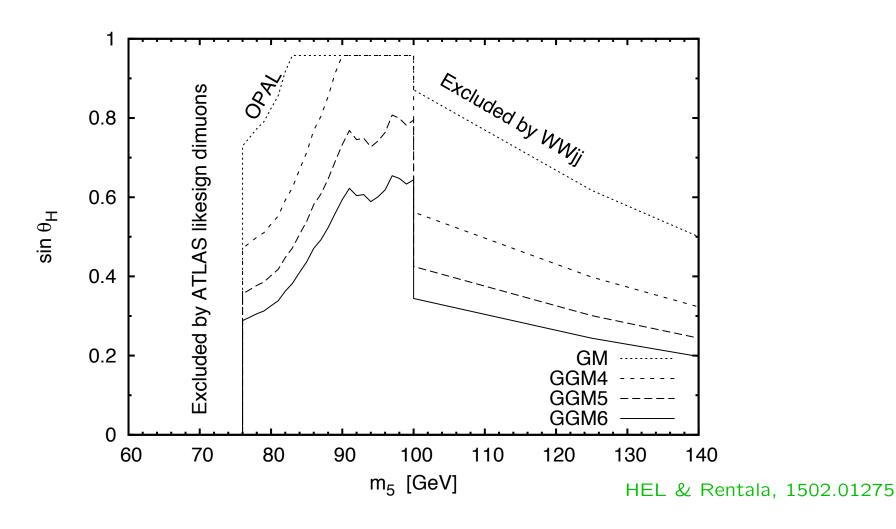
 \Rightarrow take $m_3 > 76$ GeV also ($m_5 > 76$ GeV guarantees no competing decays)

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LEP $e^+e^- \rightarrow ZH_5^0$, recoil method (independent of H_5^0 decay)

OPAL search for $Z+S^0$ production opaL hep-ex/0206022 \to upper bound on H_5^0ZZ coupling $\propto s_H^2$ as a function of m_5



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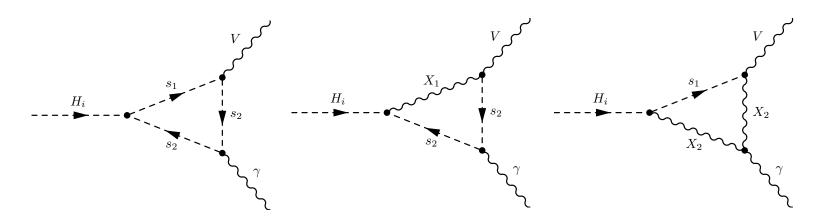
Exotic EWSB

LEP $e^+e^- \rightarrow ZH_5^0$, $H_5^0 \rightarrow \gamma\gamma$ (fermiophobic!)

Below $H_5^0 \to VV$ threshold: tree-level decays suppressed

 $H_5^0 \to W^+W^-, ZZ$ calculated including doubly off-shell effects $H_5^0 \to \gamma\gamma$ calculated as usual

 $H_5^0 \to Z\gamma$ (competing mode): new diagrams with $m_1 \neq m_2$

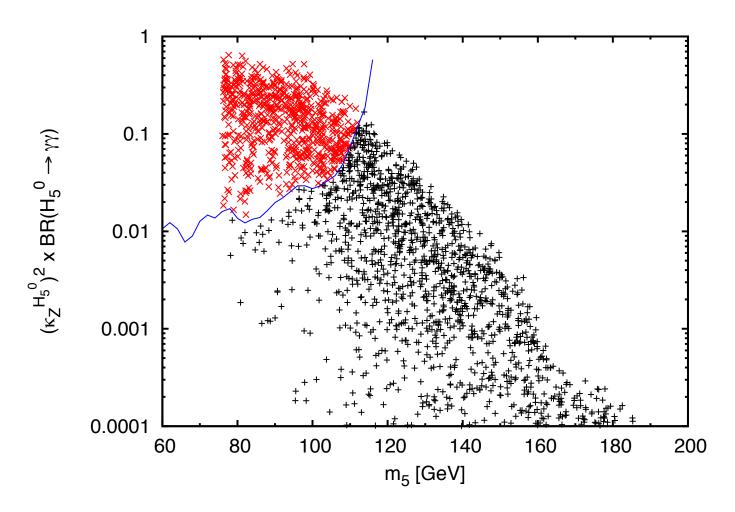


Degrande, Hartling & HEL, 1708.08753

Implemented in GMCALC 1.3.0

LEP
$$e^+e^- \to ZH_5^0$$
, $H_5^0 \to \gamma\gamma$ (fermiophobic!) LHWG Note 2002-02

Numerical limit is in HiggsBounds 4.2.0 Bechtle et al., 1507.06706



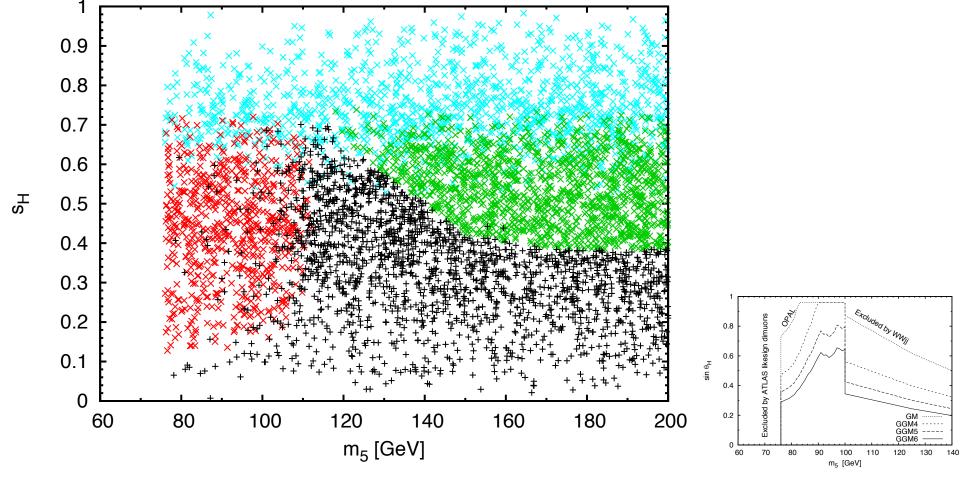
Degrande, Hartling & HEL, 1708.08753

Production cross section $\propto s_H^2$

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Exotic EWSB

LEP
$$e^+e^- \rightarrow ZH_5^0$$
, $H_5^0 \rightarrow \gamma\gamma$ (fermiophobic!)



Cyan $b \to s \gamma$ SuperIso + 2HDMC Degrande, Hartling & HEL, 1708.08753 green $H_5^{\pm\pm} o W^\pm W^\pm$ ATLAS recast red LEP $H_5^0 \rightarrow \gamma \gamma$

GMCALC Hartling, Kumar & HEL, 1412.7387

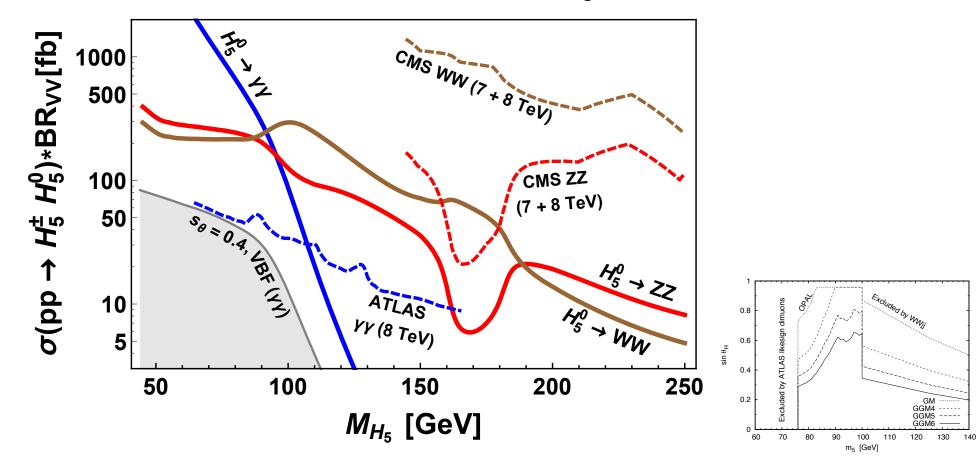
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Exotic EWSB

For the future 1:

- Drell-Yan $pp o H_5^0 H_5^\pm$, $H_5^0 o \gamma\gamma$

Drell-Yan cross section depends only on m_5 and gauge couplings!



Delgado, Garcia-Pepin, Quiros, Santiago & Vega-Morales, 1603.00962

First pass: only W loop included in $H_5^0 \to \gamma\gamma, Z\gamma$ calculation.

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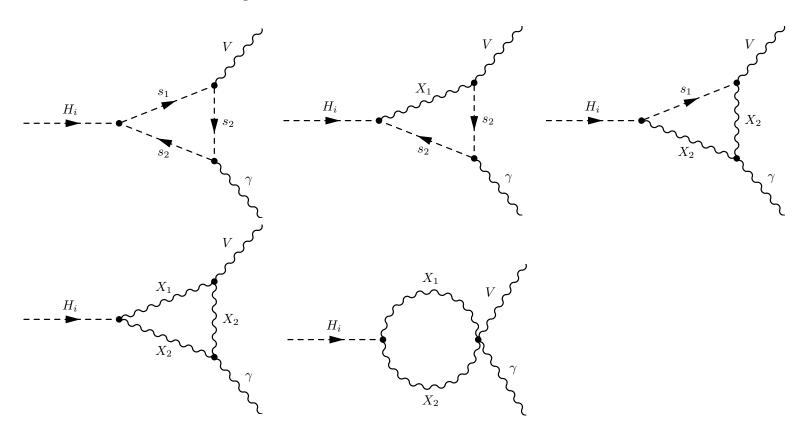
Exotic EWSB

For the future 2:

fermiophobic!

- Drell-Yan $pp o H_5^\pm H_5^0 + H_5^\pm H_5^\mp + H_5^\pm H_5^{\mp\mp}$, $H_5^\pm \to W^\pm \gamma$

Below $H_5^\pm \to W^\pm Z$ threshold: tree-level decays suppressed Calculation of $H_5^\pm \to W^\pm \gamma$ involves nonstandard diagrams:



Degrande, Hartling & HEL, 1708.08753

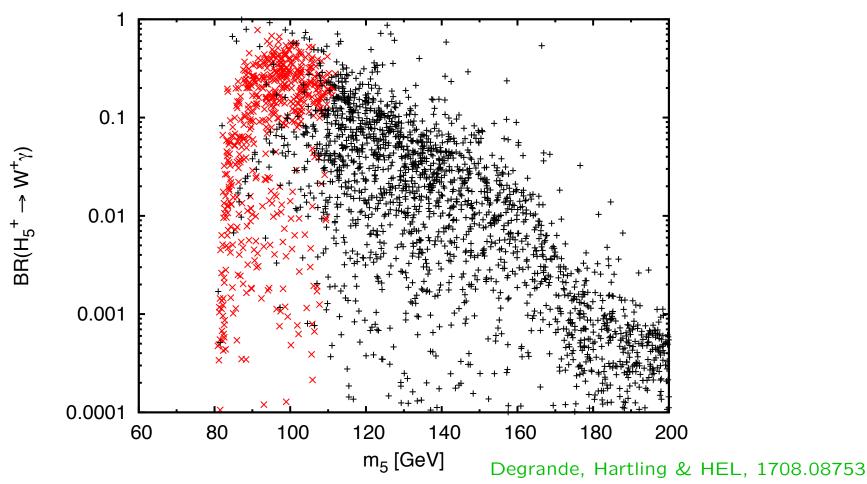
Implemented in GMCALC 1.3.0

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Exotic EWSB

For the future 2:

- Drell-Yan
$$pp \to H_5^{\pm} H_5^0 + H_5^{\pm} H_5^{\mp} + H_5^{\pm} H_5^{\mp\mp}, \; H_5^{\pm} \to W^{\pm} \gamma$$



Red points excluded by LEP $e^+e^- o ZH_5^0$, $H_5^0 o \gamma\gamma$

Drell-Yan cross section depends only on m_5 and gauge couplings!

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Exotic EWSB

For the future: implementation for LHC searches

- Drell-Yan $pp o H_5^0 H_5^\pm$, $H_5^0 o \gamma\gamma$
- Drell-Yan $pp \to H_5^{\pm} H_5^{0} + H_5^{\pm} H_5^{\mp} + H_5^{\pm} H_5^{\mp\mp}, \ H_5^{\pm} \to W^{\pm} \gamma$
- Drell-Yan $pp \to H_5^{++}H_5^{--} + H_5^{\pm\pm}H_5^{\mp}$, $H_5^{\pm\pm} \to \text{like-sign dimuons}$

MadGraph model file with effective vertices for $H_5^0\gamma\gamma$, $H_5^0Z\gamma$, $H_5^\pm W^\mp\gamma$ in preparation. work in progress with Yongcheng Wu

- Drell-Yan $pp \to H_5H_5$ cross sections are generic to all generalized GM models.
- Loop decays are specific to Georgi-Machacek model: detailed predictions for loop-induced BRs can't be applied to generalized GM models without dedicated calculations.

Combinations of complementary searches can be generic:

$$H_5^0$$
: BR $(W^+W^- + ZZ + Z\gamma + \gamma\gamma) = 1$

$$H_5^{\pm}$$
: BR $(W^{\pm}Z + W\gamma) = 1$

$$H_5^{\pm\pm}$$
: BR $(W^{\pm}W^{\pm})=1$ by charge conservation!

Conclusions

Goal:

- Enumerate the possibilities for exotic contributions to EWSB
- Find ways to constrain their contributions to M_W^2, M_Z^2

VBF $\rightarrow H^{\pm\pm} \rightarrow W^{\pm}W^{\pm}$ very generic: constrains GM, its generalizations, & septet model

VBF $\to H^\pm \to W^\pm Z$ also pretty generic: constrains GM & its generalizations, but not septet model

Low mass region $m_5 \lesssim 2M_V$ is the next target:

- Drell-Yan is probably best channel depends only on $m_{\mathbf{5}}$
- Loop decays to $\gamma\gamma$, $Z\gamma$, $W^{\pm}\gamma$ become interesting
- $H_5^{\pm\pm}$ decays to like-sign dileptons still very generic

HIGGS BOSON TRIPLETS WITH $M_{\rm W} = M_{\rm Z} \cos \theta_{\rm w}$

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Received 23 September 1985

The requirement that an irreducible representation of $SU(2)_L$ give $\rho = 1$ in tree approximation yields [4] a Diophantine equation in the isospin t and hypercharge y, $t^2 + t - 3y^2 = 0$, which has 11 solutions for t < 1000000, the largest being t, $y = 489060\frac{1}{2}$, $282359\frac{1}{2}$. We are offering a prize for the most original model based on this representation.

$$a_0 = \frac{g^2}{16\pi} \frac{(n^2 - 1)\sqrt{n}}{2\sqrt{3}} \simeq 2.3 \times 10^{12} > 1/2$$