

Higgs physics beyond the Standard Model

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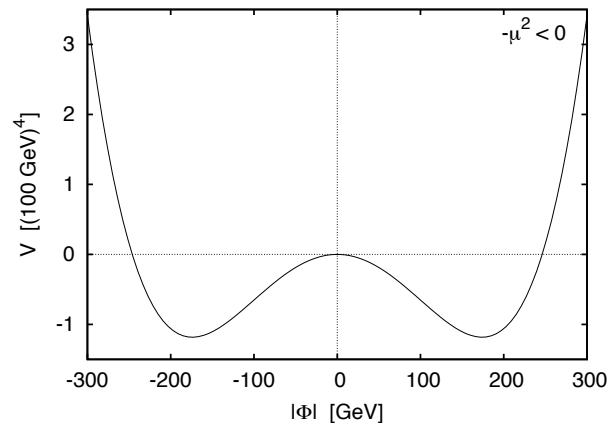
The Standard Model: electroweak symmetry breaking from a scalar $SU(2)_L$ doublet

A one-line theory:

$$\mathcal{L}_{Higgs} = |\mathcal{D}_\mu \Phi|^2 - [-\mu^2 \Phi^\dagger \Phi + \lambda (\Phi^\dagger \Phi)^2] - [y_f \bar{f}_R \Phi^\dagger F_L + \text{h.c.}]$$

Most general, renormalizable, gauge-invariant theory involving a single spin-zero (scalar) field with isospin 1/2, hypercharge 1.

$-\mu^2$ term: **vacuum condensate!** EW symmetry spontaneously broken; Goldstone bosons gauged away, 1 physical particle h .



$$\Phi = \begin{pmatrix} G^+ \\ (v + h + iG^0)/\sqrt{2} \end{pmatrix}$$

Mass and vacuum expectation value of h are fixed by minimizing the Higgs potential:

$$v^2 = \mu^2 / \lambda$$

$$M_h^2 = 2\lambda v^2 = 2\mu^2$$

The Standard Model:

electroweak symmetry breaking from a scalar $SU(2)_L$ doublet

SM Higgs couplings to SM particles are fixed by the mass-generation mechanism.

W and Z :

$$g_Z \equiv g / \cos \theta_W = \sqrt{g^2 + g'^2}, \quad v = 246 \text{ GeV}$$

$$\mathcal{L} = |\mathcal{D}_\mu \Phi|^2 \rightarrow (g^2/4)(h+v)^2 W^+ W^- + (g_Z^2/8)(h+v)^2 Z Z$$

$$M_W^2 = g^2 v^2 / 4 \quad h W W : i(g^2 v / 2) g^{\mu\nu}$$

$$M_Z^2 = g_Z^2 v^2 / 4 \quad h Z Z : i(g_Z^2 v / 2) g^{\mu\nu}$$

Fermions:

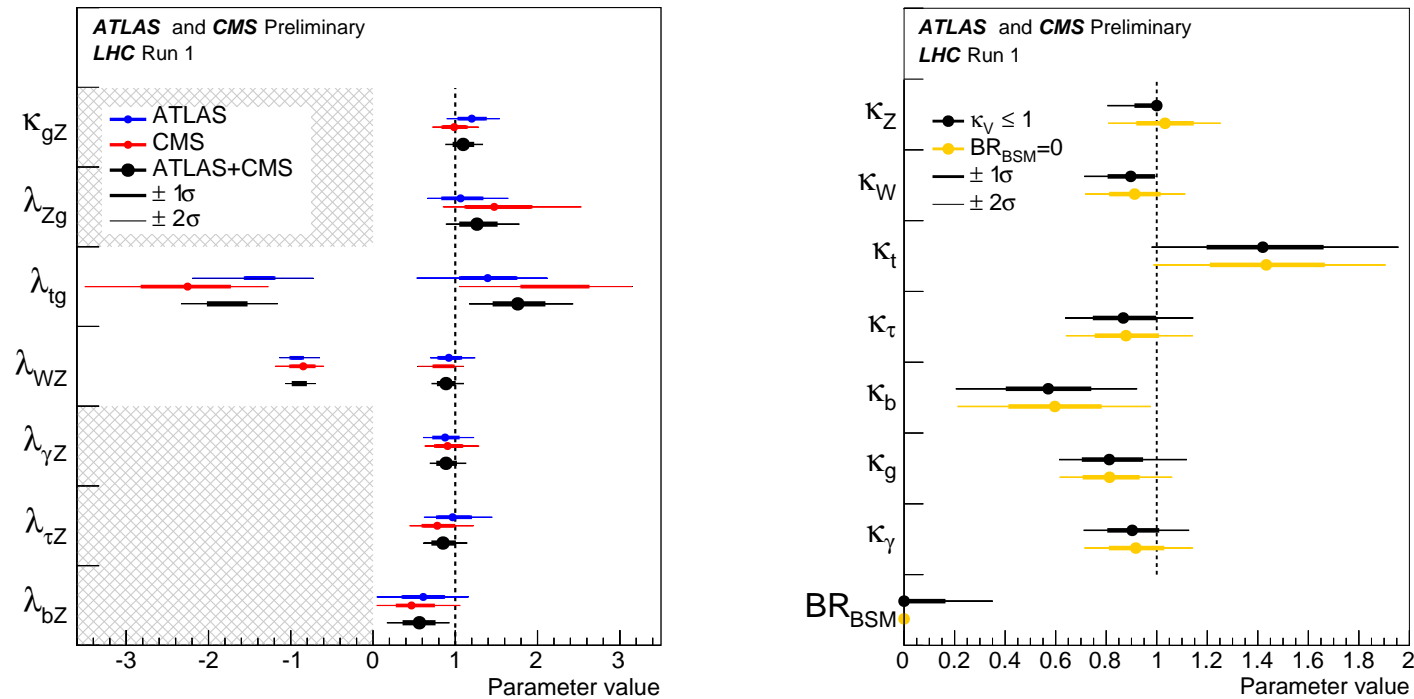
$$\mathcal{L} = -y_f \bar{f}_R \Phi^\dagger F_L + \dots \rightarrow -(y_f / \sqrt{2})(h+v) \bar{f}_R f_L + \text{h.c.}$$

$$m_f = y_f v / \sqrt{2} \quad h \bar{f} f : i m_f / v$$

Gluon pairs and photon pairs:

induced at 1-loop by fermions, W -boson.

LHC measurements of 125 GeV Higgs boson properties are fully consistent with SM picture: ATLAS-CONF-2015-044



But there is still plenty of room for extensions of the Higgs sector.

This talk:

- What else could be condensed in the vacuum?
- How do we search for its excitations?

This talk: Outline

What else could be condensed in the vacuum?

(1) Additional source of fermion masses?

→ two-Higgs-doublet models

(2) Additional (non-doublet) source of electroweak breaking?

→ models with higher-isospin scalar multiplets

For each: How do we search for its excitations?

- Properties & signatures of extra Higgs bosons
- Patterns of couplings and spectra
- A few under-exploited search channels

Conclusions

Additional sources of fermion masses?

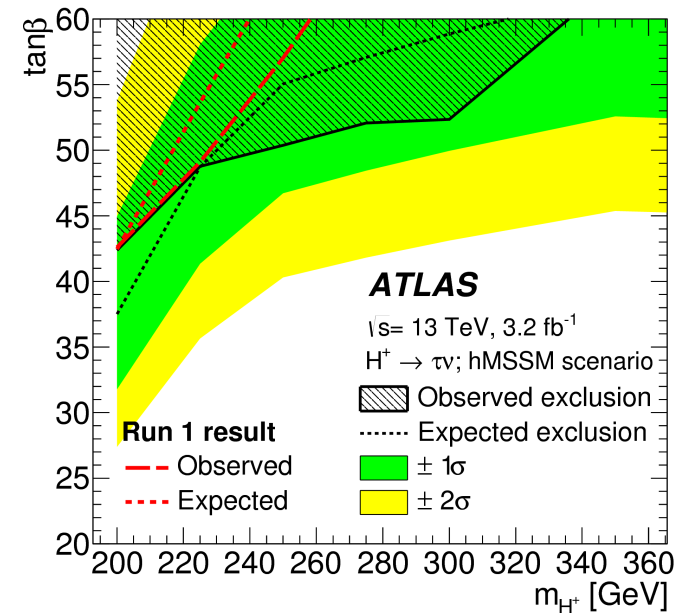
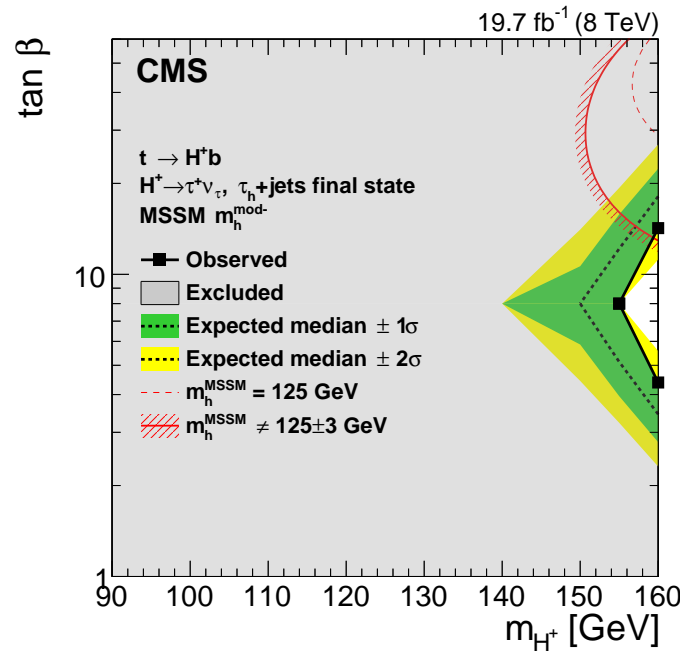
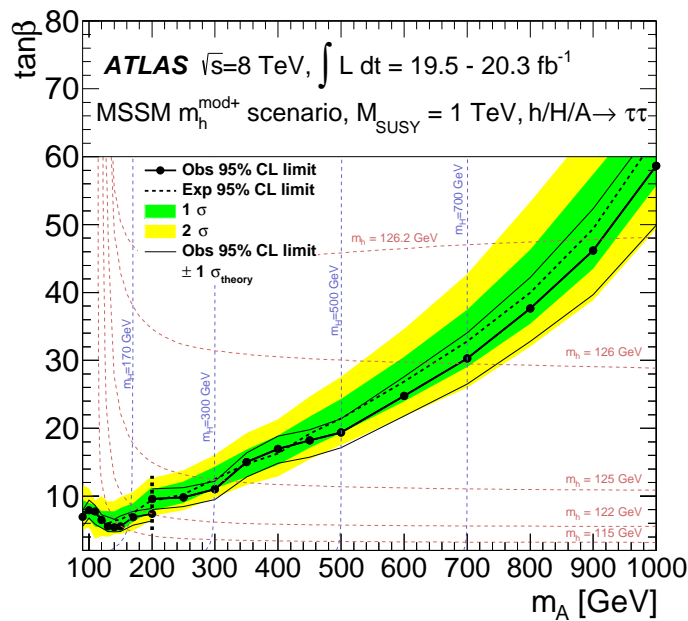
→ Two-Higgs-Doublet Model

Two-Higgs-Doublet Model

“Type-II” model is the Higgs sector of the MSSM (at tree level)
 Five Higgs states: h, H, A, H^\pm

Most-well-known searches:

$$b\bar{b} \rightarrow H/A \rightarrow \tau\tau; t \rightarrow bH^+ \text{ or } pp \rightarrow \bar{t}H^+, H^+ \rightarrow \tau\nu$$



Also $gg \rightarrow H \rightarrow WW, ZZ; pp \rightarrow H/A \rightarrow Z + A/H$

Two-Higgs-Doublet Model

Two doublets: Φ_1 and Φ_2 , vevs $v_1^2 + v_2^2 = v_{\text{SM}}^2$, $v_2/v_1 \equiv \tan \beta$

- Up-type quark masses from Φ_2 : coupling strength m_u/v_2
- Down-type quark and lepton masses from Φ_2 (Type I) or Φ_1 (Type II): coupling strength $m_{d,\ell}/v_2$ (Type I) or $m_{d,\ell}/v_1$ (Type II)

Five Higgs states (counting H^+ and H^- as two):

$$\begin{aligned} h &= \cos \alpha \phi_2^{0,r} - \sin \alpha \phi_1^{0,r} & H &= \sin \alpha \phi_2^{0,r} + \cos \alpha \phi_1^{0,r} \\ A &= \cos \beta \phi_2^{0,i} - \sin \beta \phi_1^{0,i} & H^\pm &= \cos \beta \phi_2^\pm - \sin \beta \phi_1^\pm \end{aligned}$$

First do a change of basis to the **Higgs basis**:

$$\Phi_h = \sin \beta \Phi_2 + \cos \beta \Phi_1 \quad \Phi_0 = \cos \beta \Phi_2 - \sin \beta \Phi_1$$

Defined by vacuum expectation values:

$$\Phi_h \text{ vev} = v_{\text{SM}}, \quad \Phi_0 \text{ vev} = 0$$

Two-Higgs-Doublet Model: Higgs basis

$$\Phi_h \text{ vev} = v_{\text{SM}}, \quad \Phi_0 \text{ vev} = 0$$

Five Higgs states (counting H^+ and H^- as two):

$$\begin{aligned} h &= \sin(\beta - \alpha) \phi_h^{0,r} - \cos(\beta - \alpha) \phi_0^{0,r} \\ H &= \cos(\beta - \alpha) \phi_h^{0,r} + \sin(\beta - \alpha) \phi_0^{0,r} \\ A &= \phi_0^{0,i} & H^\pm &= \phi_0^\pm \end{aligned}$$

Couplings to vector boson pairs:

$\phi_h^{0,r} VV$ couplings same as SM, while $\phi_0^{0,r} VV = 0$:

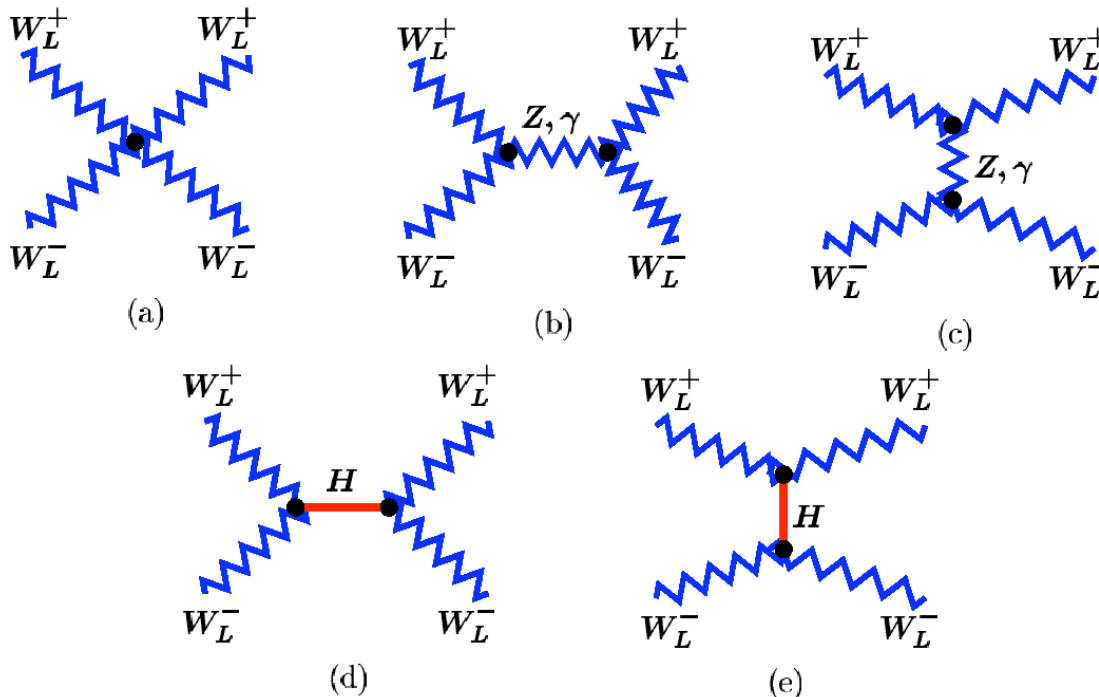
- Couplings of h to VV universally suppressed by $\sin(\beta - \alpha) \equiv \kappa_V^h$
- Couplings of H to VV are complementary: $\cos(\beta - \alpha) \equiv \kappa_V^H$

$$\text{Sum rule: } (\kappa_V^h)^2 + (\kappa_V^H)^2 = \sin^2(\beta - \alpha) + \cos^2(\beta - \alpha) = 1$$

Q: how big can $\kappa_V^H = \cos(\beta - \alpha)$ be? Controls $H \rightarrow WW, ZZ$ and $\text{VBF} \rightarrow H$

From h coupling measurements: $\kappa_V^h \sim 1 \pm 0.2 \Rightarrow |\kappa_V^H| \lesssim 0.45$

Perturbative unitarity of $WW \rightarrow WW$ scattering: E^0 term



Graphic: S. Chivukula

- SM: $m_h^2 < 16\pi v^2/5 \simeq (780 \text{ GeV})^2$ Lee, Quigg & Thacker 1977

- 2HDM: $(\kappa_V^h)^2 m_h^2 + (\kappa_V^H)^2 m_H^2 < 16\pi v^2/5$

- combine with sum rule $(\kappa_V^h)^2 + (\kappa_V^H)^2 = 1$:

$$\cos^2(\beta - \alpha) \equiv (\kappa_V^H)^2 < \frac{16\pi v^2 - 5m_h^2}{5(m_H^2 - m_h^2)} \simeq \frac{16\pi v^2}{5m_H^2} \simeq \left(\frac{780 \text{ GeV}}{m_H} \right)^2$$

Two-Higgs-Doublet Model: Higgs basis Haber et al, 1507.00933

$$\mathcal{V} = Y_1 H_1^\dagger H_1 + Y_2 H_2^\dagger H_2 + Y_3 [H_1^\dagger H_2 + \text{h.c.}] + \frac{1}{2} Z_1 (H_1^\dagger H_1)^2 + \frac{1}{2} Z_2 (H_2^\dagger H_2)^2 + Z_3 (H_1^\dagger H_1) (H_2^\dagger H_2) \\ + Z_4 (H_1^\dagger H_2) (H_2^\dagger H_1) + \left\{ \frac{1}{2} Z_5 (H_1^\dagger H_2)^2 + [Z_6 (H_1^\dagger H_1) + Z_7 (H_2^\dagger H_2)] H_1^\dagger H_2 + \text{h.c.} \right\}, \quad (2)$$

$$Y_1, Y_2, Y_3 \sim (\text{mass})^2, \quad Z_1, \dots, Z_7 \text{ dimensionless} \quad H_1 \equiv \Phi_h, \quad H_2 \equiv \Phi_0$$

Minimization of potential yields $Y_1 = -Z_1 v^2/2$, $Y_3 = -Z_6 v^2/2$
 Only one dimensionful parameter $Y_2 \equiv M^2$, can be large $\gg v^2$

Masses:

$$m_{H^\pm}^2 = Y_2 + Z_3 v^2/2 \quad m_A^2 = m_{H^\pm}^2 + (Z_4 - Z_5) v^2/2$$

$$M_{h,H}^2 = \begin{pmatrix} Z_1 v^2 & Z_6 v^2 \\ Z_6 v^2 & m_A^2 + Z_5 v^2 \end{pmatrix}$$

$$m_h^2 \simeq Z_1 v^2 \quad m_H^2 \simeq M^2 \quad \cos(\beta - \alpha) \simeq Z_6 v^2 / M^2 \sim v^2 / M^2$$

\Rightarrow **Fast decoupling!** Bad news for VBF $\rightarrow H$ and $H \rightarrow WW/ZZ$ at high m_H

$$\cos^2(\beta - \alpha) \equiv (\kappa_V^H)^2 \simeq Z_6^2 \frac{v^4}{m_H^4} = Z_6^2 \left(\frac{246 \text{ GeV}}{m_H} \right)^4$$

Two-Higgs-Doublet Model: fermion couplings

Two doublets: Φ_1 and Φ_2 , vevs $v_1^2 + v_2^2 = v_{\text{SM}}^2$, $v_2/v_1 \equiv \tan \beta$

- Up-type quark masses from Φ_2 : coupling strength m_u/v_2
- Down-type quark and lepton masses from Φ_2 (Type I) or Φ_1 (Type II): coupling strength $m_{d,\ell}/v_2$ (Type I) or $m_{d,\ell}/v_1$ (Type II)

First do a change of basis to the **Higgs basis**: Φ_h vev = v_{SM} , Φ_0 vev = 0

$$\Phi_h = \sin \beta \Phi_2 + \cos \beta \Phi_1 \quad \Phi_0 = \cos \beta \Phi_2 - \sin \beta \Phi_1$$

Physical Higgs states: $\cos(\beta - \alpha) \simeq Z_6 v^2 / M^2 \sim v^2 / M^2$

$$\begin{aligned} h &= \sin(\beta - \alpha) \phi_h^{0,r} - \cos(\beta - \alpha) \phi_0^{0,r} \\ H &= \cos(\beta - \alpha) \phi_h^{0,r} + \sin(\beta - \alpha) \phi_0^{0,r} \\ A &= \phi_0^{0,i} & H^\pm &= \phi_0^\pm \end{aligned}$$

So $A = \phi_0^{0,i}$, $H^\pm = \phi_0^\pm$, and for decoupling or alignment $H \simeq \phi_0^{0,r}$: the BSM Higgs bosons all live in the Φ_0 doublet.

Two-Higgs-Doublet Model: fermion couplings

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First do a change of basis to the **Higgs basis**: Φ_h vev = v_{SM} , Φ_0 vev = 0

$$\Phi_h = \sin \beta \Phi_2 + \cos \beta \Phi_1 \quad \Phi_0 = \cos \beta \Phi_2 - \sin \beta \Phi_1$$

Coupling strengths of Φ_0 to fermions:

Type I: $\cos \beta \times m_f/v_2 = \cot \beta \times m_f/v_{\text{SM}}$ (all quarks & leptons)

Type II: $\cos \beta \times m_u/v_2 = \cot \beta \times m_u/v_{\text{SM}}$ (up-type)

Type II: $\sin \beta \times m_{d,\ell}/v_1 = \tan \beta \times m_{d,\ell}/v_{\text{SM}}$ (down-type & leptons)

These are NOT suppressed when the BSM Higgses are heavy!

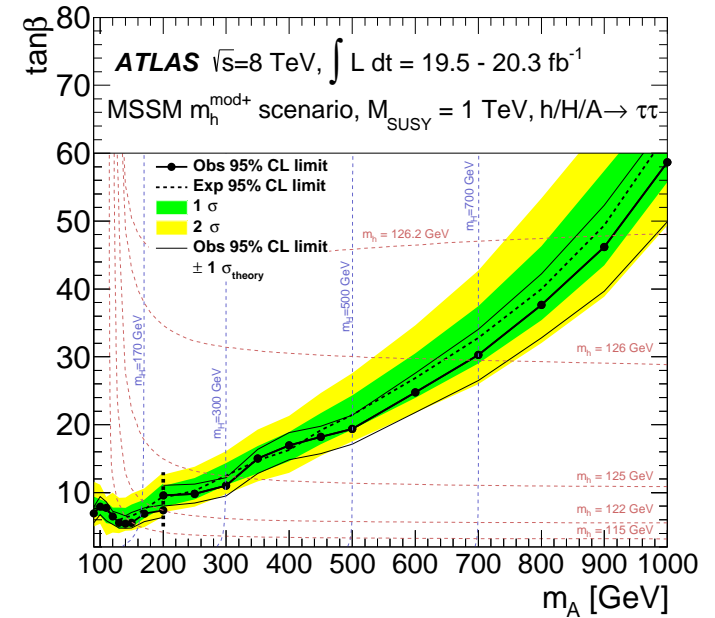
Good news for heavy Higgs production via gluon fusion, $b\bar{b}$ -fusion

Two-Higgs-Doublet Model: under-exploited search channels I: $gg \rightarrow H/A \rightarrow t\bar{t}$ at low $\tan \beta$

Type I: $\cot \beta \times m_f/v_{SM}$ (all quarks & leptons)

Type II: $\cot \beta \times m_u/v_{SM}$ (up-type)

Type II: $\tan \beta \times m_{d,l}/v_{SM}$ (down-type & leptons)



- Nontrivial interference with continuum $gg \rightarrow t\bar{t}$ background

Dicus, Stange, & Willenbrock, 1994

- Expts need theory prediction including signal/background interference, lineshape, & QCD corrections

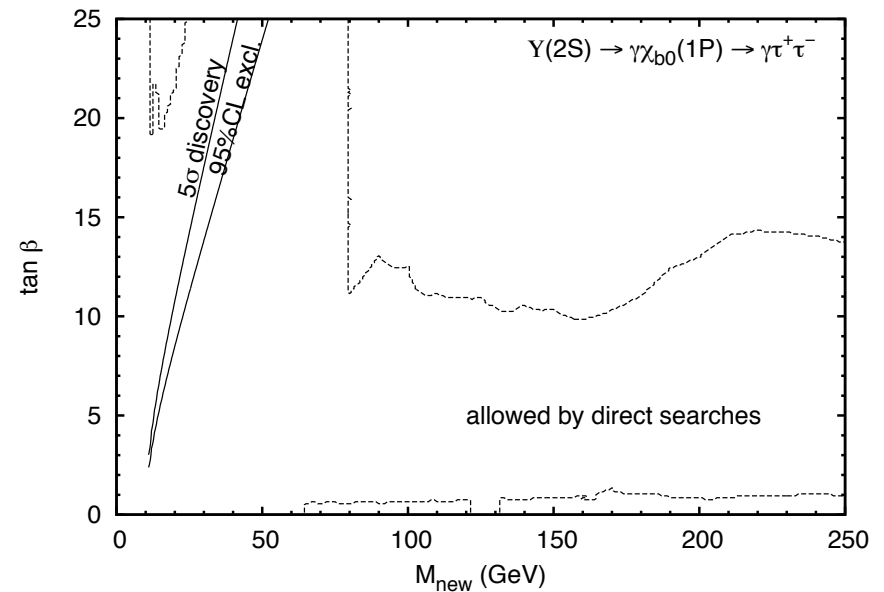
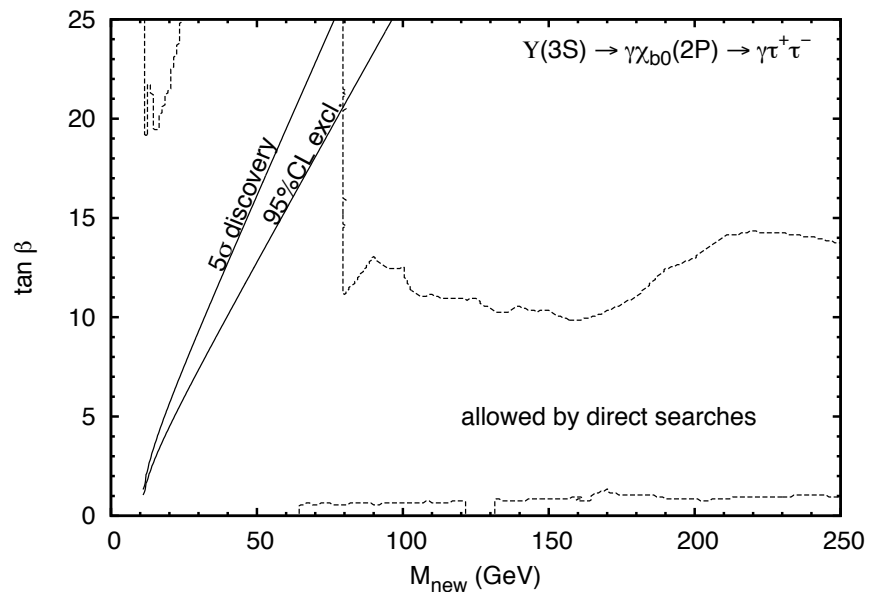
- Associated prod'n $pp \rightarrow b\bar{b}H/A$, $H/A \rightarrow t\bar{t}$ could help at moderate $\tan \beta$

Two-Higgs-Doublet Model: under-exploited search channels II: indirect probe of light h from scalar bottomonium χ_{b0} decay

Similar to charged Higgs in $B^+ \rightarrow \tau\nu$, pseudoscalar in $\eta_b \rightarrow \tau\tau$

Type-II 2HDM, H is 125 GeV SM-like Higgs, lighter $h \subset \Phi_0$

$\Upsilon \rightarrow \gamma\chi_{b0}$, $\chi_{b0} \rightarrow \tau\tau$ via off-shell h : rate $\propto \tan^4 \beta / m_h^4$



250 fb^{-1} on $\Upsilon(3S/2S)$ at Belle-II

S. Godfrey & HEL, 1510.04659

- CMS $pp \rightarrow \phi \rightarrow \tau\tau$ search goes down to 80 GeV [HiggsBounds 4.2.0](#)
- Continuum $e^+e^- \rightarrow \gamma\tau\tau$ background: $\sim 4\text{k}$ events under photon peak with no selection cut optimization \rightarrow room for improvement

Additional (non-doublet) sources of electroweak breaking?

→ models with higher-isospin scalar multiplets

Part of electroweak breaking from a higher-isospin scalar field?

Fermion masses can arise only from $SU(2)_L$ doublet(s)

$$\mathcal{L} = -y_f \bar{f}_R \Phi^\dagger F_L + \dots \rightarrow -(y_f/\sqrt{2})(\phi^{0,r} + v_\phi) \bar{f}_R f_L + \text{h.c.}$$
$$m_f = y_f v_\phi / \sqrt{2} \quad \phi^{0,r} \bar{f} f : iy_f / \sqrt{2} = im_f / v_\phi$$

F_L is doublet, f_R is singlet, need Φ doublet for gauge invariance

Top quark Yukawa perturbativity \Rightarrow lower bound on doublet vev:
define $\cos \theta_H \equiv v_\phi / v_{SM}$, then $\tan \theta_H < 10/3$ (or $\cos \theta_H > 0.287$)

Scalar couplings to fermions come from their doublet content

$$\Phi = \begin{pmatrix} \phi^+ \\ (v_\phi + \phi^{0,r} + i\phi^{0,i})/\sqrt{2} \end{pmatrix}$$

With other scalar fields in play, Goldstone bosons are linear combinations of different fields.

Part of electroweak breaking from a higher-isospin scalar field?

W and Z masses arise from anything carrying $SU(2)_L \times U(1)_Y$

$$M_W^2 = \frac{g^2}{4} \sum_k 2 \left[T_k(T_k + 1) - \frac{Y_k^2}{4} \right] v_k^2 = \frac{g^2}{4} v_{\text{SM}}^2$$
$$M_Z^2 = \frac{g^2}{4 \cos^2 \theta_W} \sum_k Y_k^2 v_k^2 = \frac{g^2}{4 \cos^2 \theta_W} v_{\text{SM}}^2$$

($Q = T^3 + Y/2$, vevs defined as $\langle \phi_k^0 \rangle = v_k/\sqrt{2}$ for complex reps and $\langle \phi_k^0 \rangle = v_k$ for real reps)

Used $Q = 0$ for component carrying the vev to simplify expressions

Top Yukawa perturbativity $\rightarrow (v_\phi/v_{\text{SM}})^2 > (0.287)^2 = 0.082$
 \Rightarrow At least 8.2% of $M_{W,Z}^2$ comes from doublet.

Lots of room for higher-isospin scalar contributions!

Can we constrain this exotic possibility?

Problem with higher-isospin scalar fields

$\rho \equiv$ ratio of strengths of charged and neutral weak currents

$$\rho = \frac{M_W^2}{M_Z^2 \cos^2 \theta_W} = \frac{\sum_k 2[T_k(T_k + 1) - Y_k^2/4]v_k^2}{\sum_k Y_k^2 v_k^2}$$

($Q = T^3 + Y/2$, vevs defined as $\langle \phi_k^0 \rangle = v_k/\sqrt{2}$ for complex reps and $\langle \phi_k^0 \rangle = v_k$ for real reps)

PDG 2014: $\rho = 1.000\,40 \pm 0.000\,24$

We can still have higher-isospin scalars with non-negligible vevs;
only two approaches using symmetry: (could also tune ρ by hand, but icky)

1) Impose **global $SU(2)_L \times SU(2)_R$ symmetry** on scalar sector
 \implies breaks to custodial $SU(2)$ upon EWSB; $\rho = 1$ at tree level

Georgi & Machacek 1985; Chanowitz & Golden 1985

2) $\rho = 1$ “by accident” for $(T, Y) = (\frac{1}{2}, 1)$ doublet; $(3, 4)$ **septet**

Septet: Hisano & Tsumura, 1301.6455; Kanemura, Kikuchi & Yagyu, 1301.7303

Larger solutions forbidden by perturbative unitarity of weak charges.

Hally, HEL, & Pilkington 1202.5073

The models

1) Models with global $SU(2)_L \times SU(2)_R$ symmetry:

a) Georgi-Machacek model

b) Generalizations to higher isospin

2) Model with a scalar septet (in progress)

All these models share a key common feature:

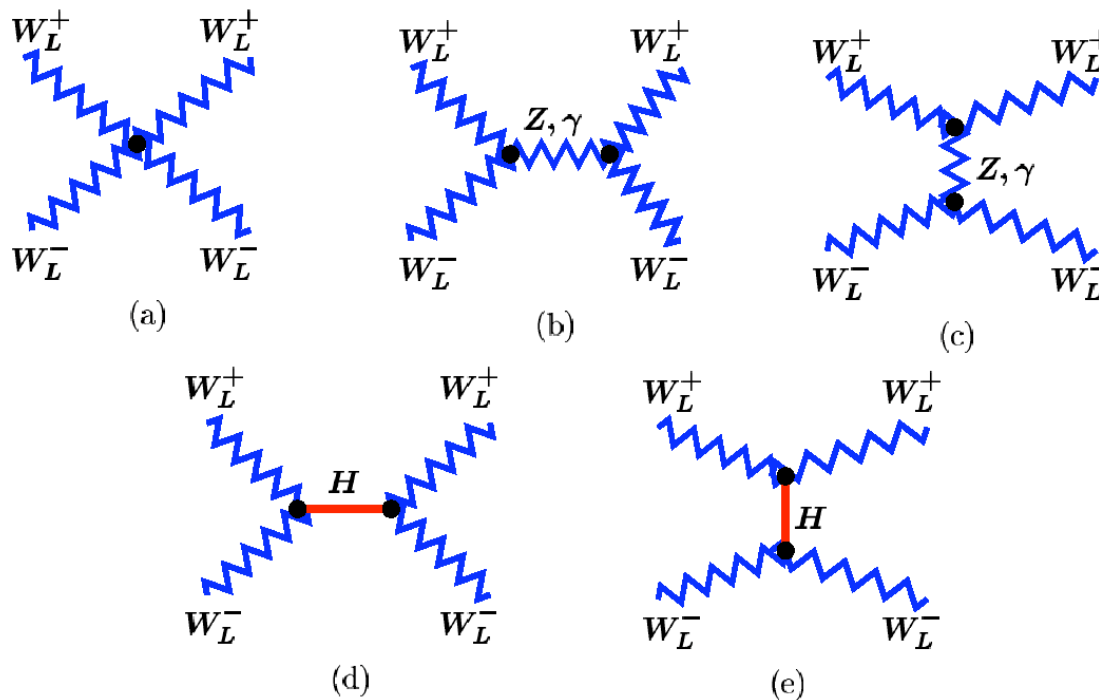
$$H^{\pm\pm} \leftrightarrow W^{\pm}W^{\pm} \text{ and } H^{\pm} \leftrightarrow W^{\pm}Z$$

with couplings controlled by vev of higher-isospin scalar(s)

Generic experimental probe is diboson resonance search in VBF.

Theoretical origin of common feature:

Unitarization of $WW \rightarrow WW$, $WW \rightarrow ZZ$ scattering amplitudes



Graphic: S. Chivukula

- SM: Higgs exchange cancels E^2/v^2 term in amplitude.
- 2HDM: cancellation \rightarrow sum rule $(\kappa_V^h)^2 + (\kappa_V^H)^2 = 1$
- Higher-isospin scalars: $(\kappa_V^h)^2 + (\kappa_V^H)^2 > 1$, need $H^{\pm\pm}$ and H^\pm in new u -channel diagrams: couplings inter-related

Falkowski, Rychkov & Urbano, 1202.1532 (see also Higgs Hunter's Guide)

Georgi-Machacek model Georgi & Machacek 1985; Chanowitz & Golden 1985

SM Higgs bidoublet + two isospin-triplets in a **bitriplet**:

$$\Phi = \begin{pmatrix} \phi^{0*} & \phi^+ \\ -\phi^{+*} & \phi^0 \end{pmatrix} \quad X = \begin{pmatrix} \chi^{0*} & \xi^+ & \chi^{++} \\ -\chi^{+*} & \xi^0 & \chi^+ \\ \chi^{++*} & -\xi^{+*} & \chi^0 \end{pmatrix}$$

Physical spectrum: Custodial symmetry fixes almost everything!

Bidoublet: $2 \times 2 \rightarrow 3 + 1$

Bitriplet: $3 \times 3 \rightarrow 5 + 3 + 1$

- Two custodial singlets mix $\rightarrow h^0, H^0$
- Two custodial triplets mix $\rightarrow (H_3^+, H_3^0, H_3^-) + \text{Goldstones}$
- Custodial fiveplet $(H_5^{++}, H_5^+, H_5^0, H_5^-, H_5^{--})$ unitarizes $VV \rightarrow VV$

Georgi-Machacek model Georgi & Machacek 1985; Chanowitz & Golden 1985

SM Higgs bidoublet + two isospin-triplets in a bitriplet:

$$\Phi = \begin{pmatrix} \phi^{0*} & \phi^+ \\ -\phi^{+*} & \phi^0 \end{pmatrix} \quad X = \begin{pmatrix} \chi^{0*} & \xi^+ & \chi^{++} \\ -\chi^{+*} & \xi^0 & \chi^+ \\ \chi^{++*} & -\xi^{+*} & \chi^0 \end{pmatrix}$$

Physical spectrum: Custodial symmetry fixes almost everything!

Bidoublet: $2 \times 2 \rightarrow 3 + 1$

Bitriplet: $3 \times 3 \rightarrow 5 + 3 + 1$

- Two custodial singlets mix $\rightarrow h^0, H^0$ m_h, m_H \leftarrow (very similar)
- Two custodial triplets mix $\rightarrow (H_3^+, H_3^0, H_3^-)$ m_3 \leftarrow to 2HDM)
- Custodial fiveplet $(H_5^{++}, H_5^+, H_5^0, H_5^-, H_5^{--})$ m_5 \leftarrow new!

Generalized Georgi-Machacek models

Galison 1984; Robinett 1985; HEL 1999; Chang et al 2012; HEL & Rentala 2015

Replace the bitriplet with a $bi-n$ -plet \implies “GGM $_n$ ”

Bidoublet: $2 \times 2 \rightarrow 3 + 1$

Bitriplet: $3 \times 3 \rightarrow 5 + 3 + 1$

Biquartet: $4 \times 4 \rightarrow 7 + 5 + 3 + 1$

Bipentet: $5 \times 5 \rightarrow 9 + 7 + 5 + 3 + 1$

Bisextet: $6 \times 6 \rightarrow 11 + 9 + 7 + 5 + 3 + 1$

Larger $bi-n$ -plets forbidden by perturbative unitarity of weak charges!

Hally, HEL, & Pilkington 1202.5073

- Two custodial singlets mix $\rightarrow h^0, H^0$
- Two custodial triplets mix $\rightarrow (H_3^+, H_3^0, H_3^-) +$ Goldstones
- Custodial fiveplet $(H_5^{++}, H_5^+, H_5^0, H_5^-, H_5^{--})$ unitarizes $VV \rightarrow VV$
- Additional states

Phenomenology: custodial fiveplet $H_5^{++}, H_5^+, H_5^0, H_5^-, H_5^{--}$

Custodial-fiveplet comes only from higher-isospin scalars:
no couplings to fermions!

$s_H^2 \equiv$ fraction of M_W^2, M_Z^2 from higher-isospin scalar

$H_5 VV$ couplings are nonzero: very different from 2HDM!

$$\begin{aligned}
 H_5^0 W_\mu^+ W_\nu^- &: & -i \frac{2M_W^2}{v_{\text{SM}}} \frac{g_5}{\sqrt{6}} g_{\mu\nu}, \\
 H_5^0 Z_\mu Z_\nu &: & i \frac{2M_Z^2}{v_{\text{SM}}} \sqrt{\frac{2}{3}} g_5 g_{\mu\nu}, \\
 H_5^+ W_\mu^- Z_\nu &: & -i \frac{2M_W M_Z}{v_{\text{SM}}} \frac{g_5}{\sqrt{2}} g_{\mu\nu}, \\
 H_5^{++} W_\mu^- W_\nu^- &: & i \frac{2M_W^2}{v_{\text{SM}}} g_5 g_{\mu\nu},
 \end{aligned}$$

Coupling strength depends on the isospins of the scalars involved:

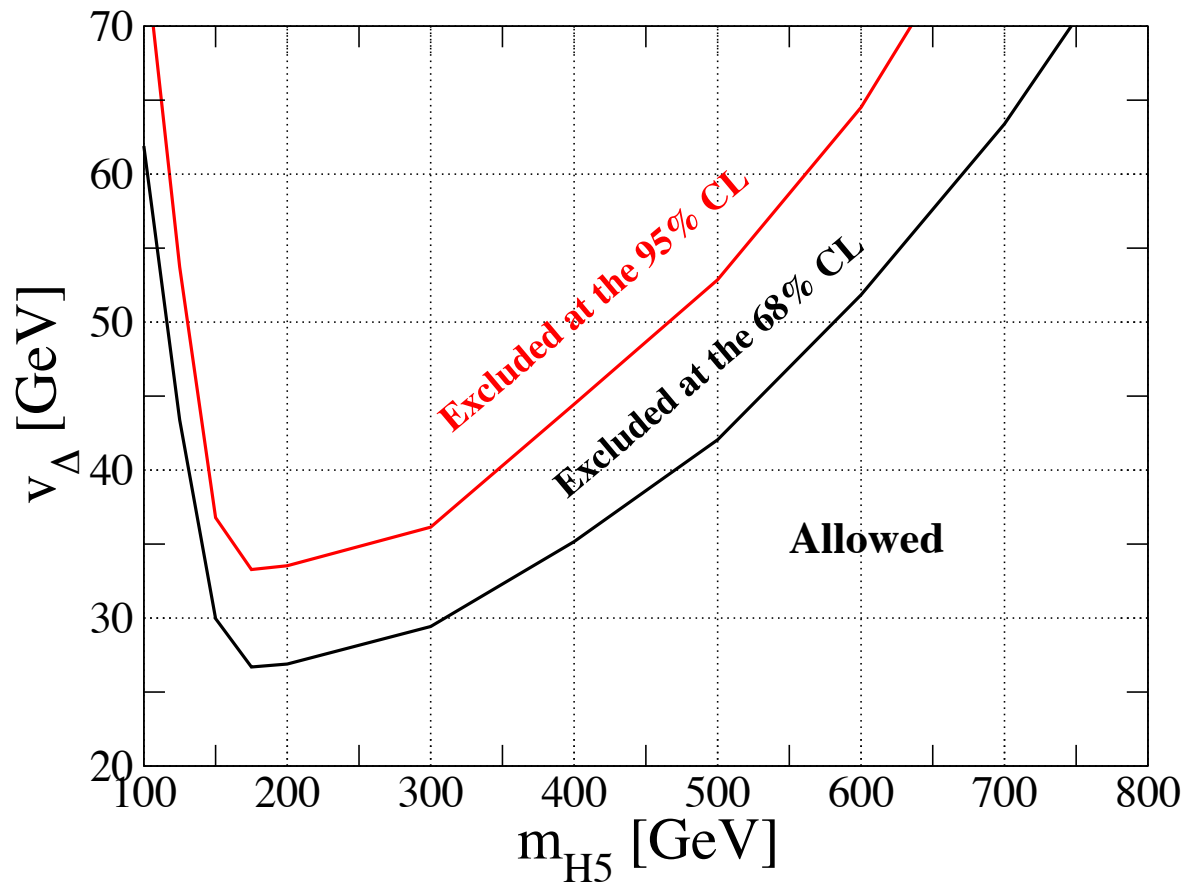
$$g_5^{\text{GM}} = \sqrt{2} s_H, \quad g_5^{\text{GGM4}} = \sqrt{\frac{24}{5}} s_H, \quad g_5^{\text{GGM5}} = \sqrt{\frac{42}{5}} s_H, \quad g_5^{\text{GGM6}} = \frac{8}{\sqrt{5}} s_H$$

Direct probe of higher-isospin vacuum condensate!

Constraint from VBF $H_5^{\pm\pm} \rightarrow W^\pm W^\pm \rightarrow$ same-sign dileptons

Theorist-recasting of ATLAS $W^\pm W^\pm jj$ cross-section measurement [ATLAS, 1405.6241](#)

\Rightarrow put limit on VBF $\rightarrow H_5^{\pm\pm}$ cross section, directly constrain g_5



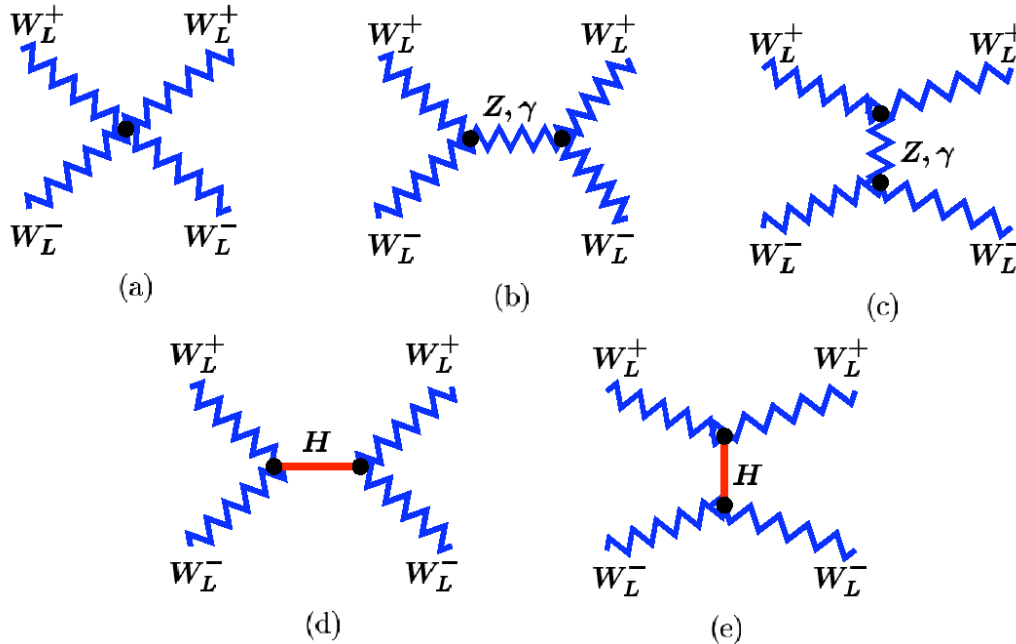
$$g_5 = \sqrt{2}s_H \text{ in GM model}$$

$$v_\Delta \equiv v_\chi = s_H v_{SM} / \sqrt{8}$$

[Chiang, Kanemura & Yagyu, 1407.5053](#)

What about higher H_5 masses?

Perturbative unitarity of $WW \rightarrow WW$ scattering: E^0 term

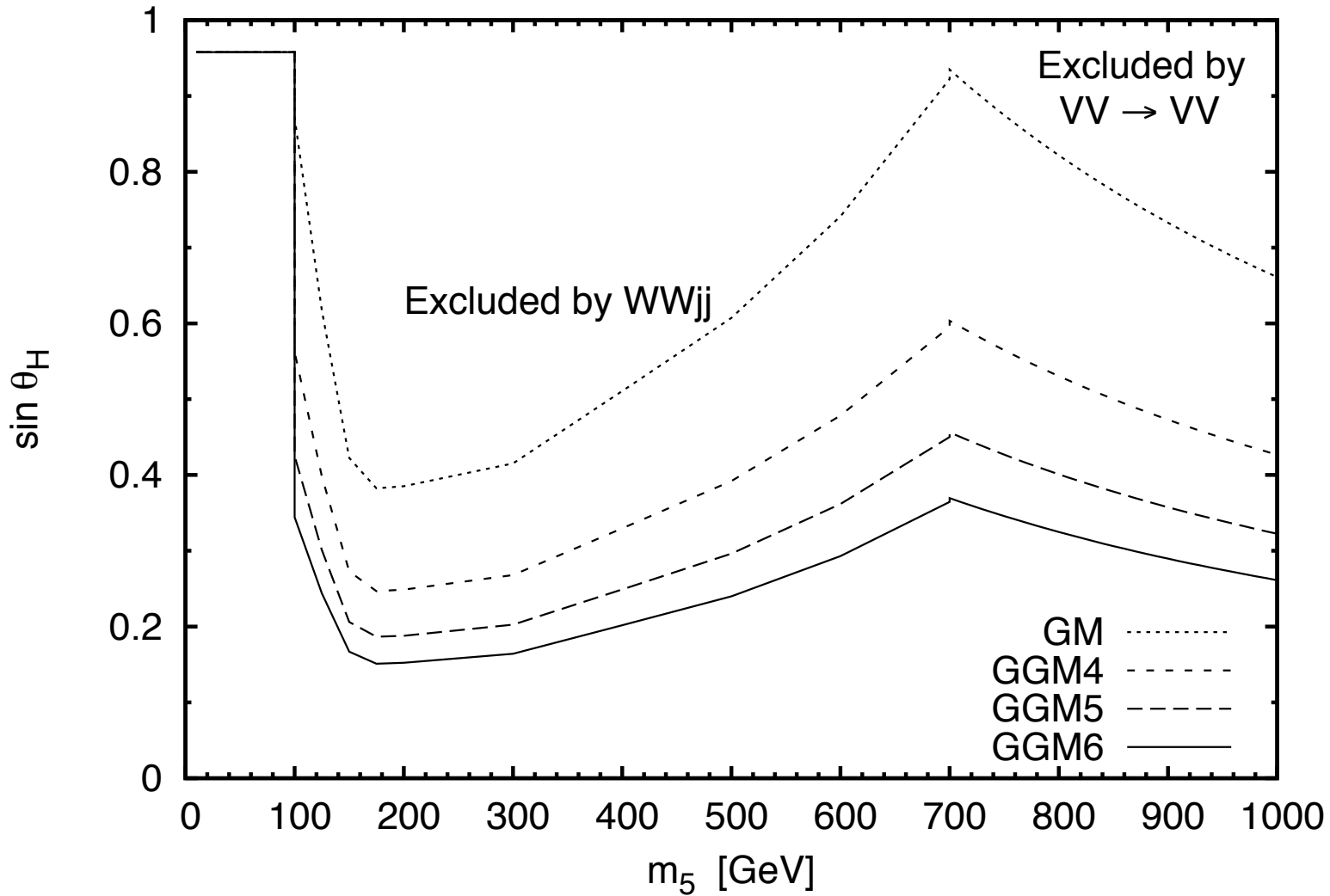


Graphic: S. Chivukula

- SM: $m_h^2 < 16\pi v_{\text{SM}}^2/5 \simeq (780 \text{ GeV})^2$ Lee, Quigg & Thacker 1977
- GM model: $\left[(\kappa_V^h)^2 m_h^2 + (\kappa_V^H)^2 m_H^2 + \frac{2}{3} g_5^2 m_5^2 \right] < 16\pi v_{\text{SM}}^2/5$
- combine with sum rule $(\kappa_V^h)^2 + (\kappa_V^H)^2 - \frac{5}{6} g_5^2 = 1$:

$$g_5^2 < \frac{6(16\pi v_{\text{SM}}^2 - 5m_h^2)}{5(4m_5^2 + 5m_h^2)} \simeq \frac{24\pi v_{\text{SM}}^2}{5m_5^2} \simeq \left(\frac{955 \text{ GeV}}{m_5} \right)^2$$

Good news for VBF production (compared to 2HDM $(\kappa_V^H)^2 \sim v^4/m_H^4$)



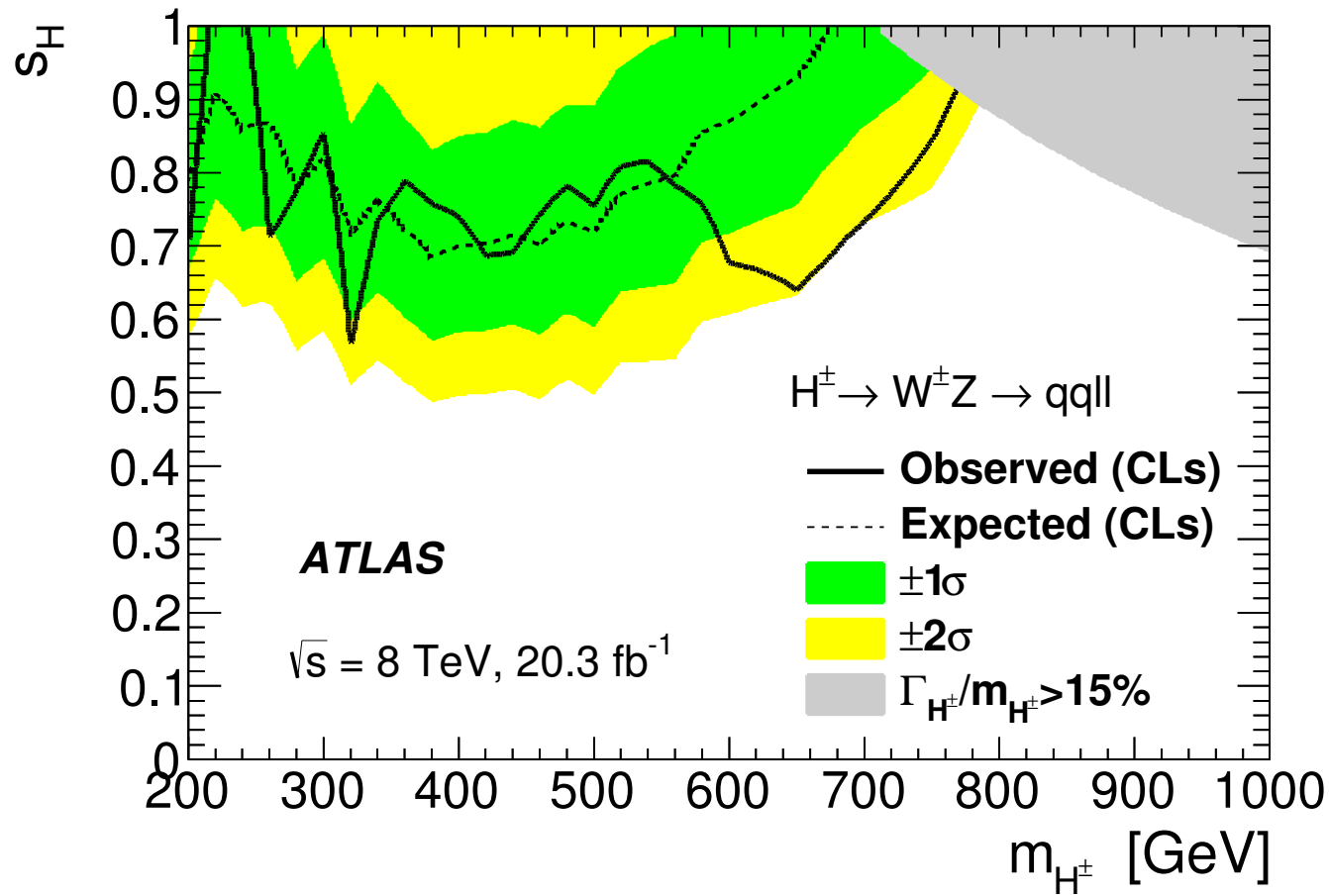
HEL & Rentala, 1502.01275

$$g_5^{\text{GM}} = \sqrt{2}s_H, \quad g_5^{\text{GGM4}} = \sqrt{\frac{24}{5}}s_H, \quad g_5^{\text{GGM5}} = \sqrt{\frac{42}{5}}s_H, \quad g_5^{\text{GGM6}} = \frac{8}{\sqrt{5}}s_H$$

Note: $s_H^2 \equiv$ exotic fraction of $M_{W,Z}^2$ is least constrained in original Georgi-Machacek model.

Constraint from VBF $H_5^\pm \rightarrow W^\pm Z \rightarrow qq\ell^+\ell^-$

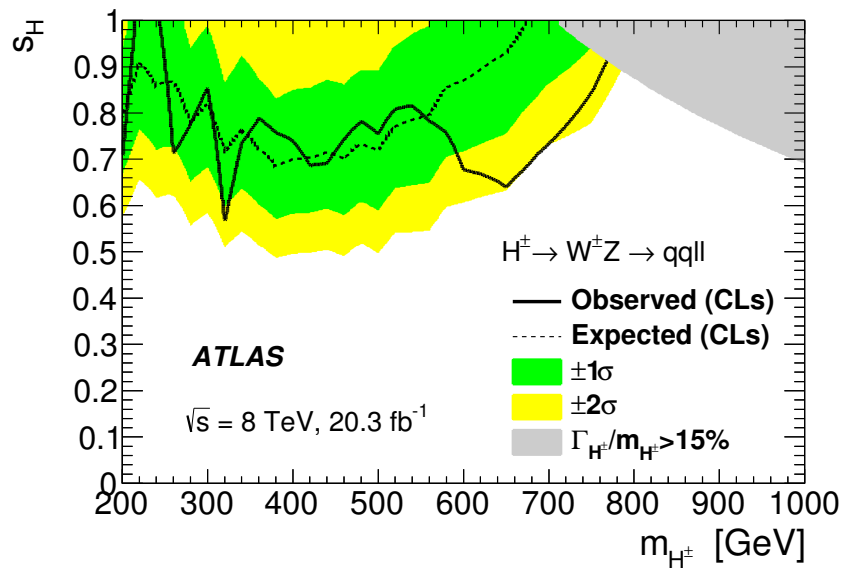
Dedicated ATLAS search for singly-charged resonance in VBF, using Georgi-Machacek model as benchmark



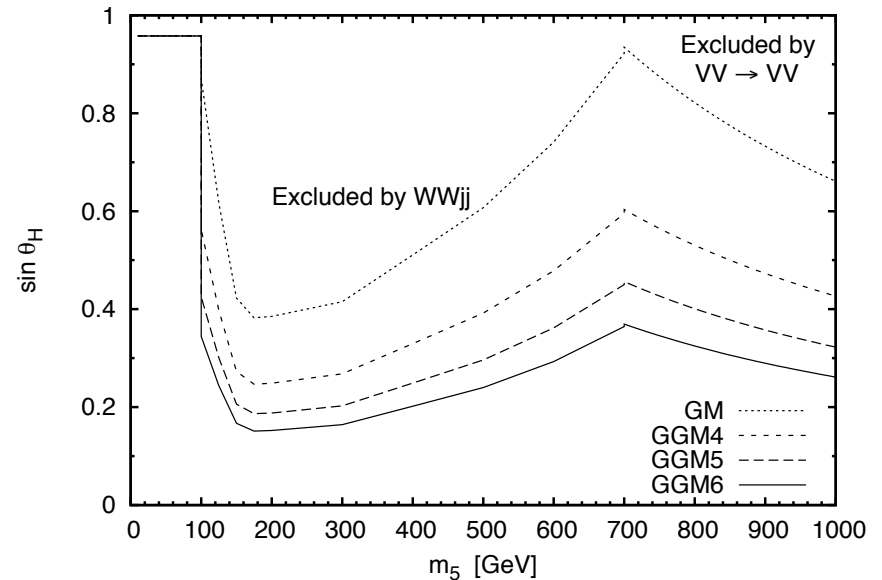
ATLAS 1503.04233

$$g_5^2 \lesssim (955 \text{ GeV}/m_5)^2 \quad \Rightarrow \quad \Gamma_{H^\pm}/m_5 \lesssim 15\% \text{ for } m_5 \gg M_W$$

$H_5^\pm \rightarrow W^\pm Z$ exclusion not quite as strong as $H_5^{\pm\pm} \rightarrow W^\pm W^\pm$, but more data is coming.



ATLAS 1503.04233



HEL & Rentala, 1502.01275,

after Chiang, Kanemura & Yagyu, 1407.5053,

after ATLAS, 1405.6241

Straightforward to translate constraint from Georgi-Machacek model onto its higher-isospin generalizations.

What about lower H_5 masses?

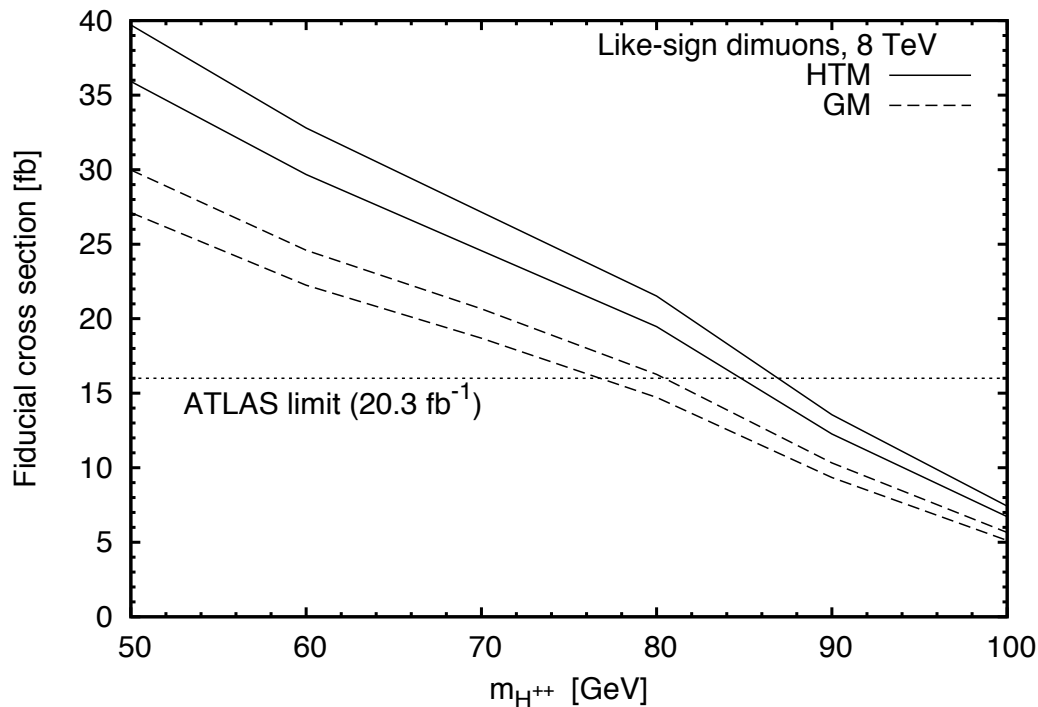
pair production, $H_5^{++} \rightarrow W^+W^+$

Constraint on $H^{\pm\pm}H^{\mp\mp} + H^{\pm\pm}H^{\mp}$ in Higgs Triplet Model from recasting ATLAS like-sign dimuons search [ATLAS, 1412.0237](#)

[Kanemura, Kikuchi, Yagyu & Yokoya, 1412.7603](#)

Adapt to generalized Georgi-Machacek models using

$$\begin{aligned}\sigma_{\text{tot}}^{\text{NLO}}(pp \rightarrow H_5^{++}H_5^{--})_{\text{GM}} &= \sigma_{\text{tot}}^{\text{NLO}}(pp \rightarrow H^{++}H^{--})_{\text{HTM}}, \\ \sigma_{\text{tot}}^{\text{NLO}}(pp \rightarrow H_5^{\pm\pm}H_5^{\mp})_{\text{GM}} &= \frac{1}{2}\sigma_{\text{tot}}^{\text{NLO}}(pp \rightarrow H^{\pm\pm}H^{\mp})_{\text{HTM}}.\end{aligned}$$



[HEL & Rental, 1502.01275](#)

$\Rightarrow m_5 \gtrsim 76 \text{ GeV}$,
independent of g_5

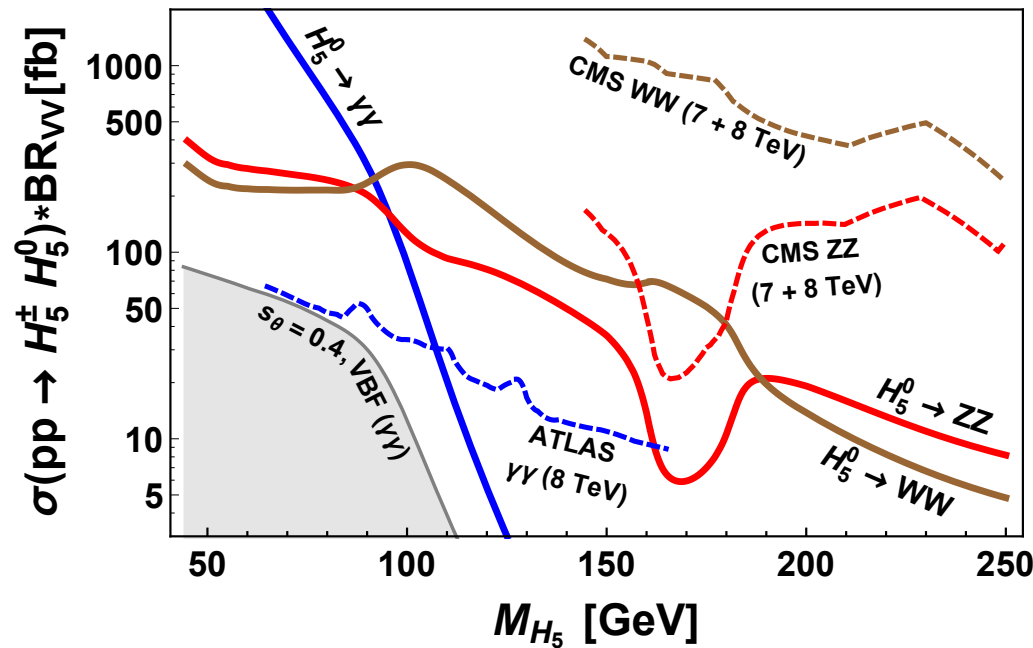
Takes advantage of mass-degeneracy of H_5^{++} and H_5^+

What about lower H_5 masses?

pair production, $H_5^0 \rightarrow \gamma\gamma$

Scalar pair prod'n $q\bar{q}' \rightarrow W^* \rightarrow H_5^0 H_5^\pm$: large xsec at low mass
 Fermiophobic H_5^0 : decays to $\gamma\gamma$ dominate at low mass

Take advantage of 8 TeV LHC diphoton cross-section limits!



Excludes $m_5 \lesssim 110$ GeV
 independent of exotic vev

For illustration: plot neglects
 charged scalar loop contribu-
 tions to $H_5^0 \rightarrow \gamma\gamma$
 (full model scan is feasible)

Delgado, Garcia-Pepin, Quirós, Santiago, & Vega-Morales, 1603.00962

$H_5^+ \rightarrow W^+ \gamma$ also interesting: BR implementation in progress

Conclusions

LHC Higgs measurements are (so far) consistent with the SM

But there is still room for New Physics in the electroweak-symmetry-breaking sector: additional scalar fields condensed in the vacuum!

(1) Additional source of fermion masses?

→ two-Higgs-doublet models

(2) Additional (non-doublet) source of electroweak breaking?

→ models with higher-isospin scalar multiplets

The more these contribute to EW breaking/fermion masses, the harder they are to hide from experiments.

- $H/A \rightarrow t\bar{t}$: probe low- $\tan\beta$ window of 2HDM
- VBF $H_5^{\pm\pm} \rightarrow W^\pm W^\pm$, $H_5^\pm \rightarrow W^\pm Z$: probe higher-isospin vev
- Fermiophobic scalar pair production at low mass: $\gamma\gamma$ and $W\gamma$

BACKUP

Septet model (work in progress)

Two CP-even neutral scalars:

$$h^0 = c_\alpha \phi^{0,r} - s_\alpha \chi^{0,r}, \quad H^0 = s_\alpha \phi^{0,r} + c_\alpha \chi^{0,r}$$

One CP-odd neutral scalar: ($c_H \equiv v_\phi/v_{\text{SM}}$ as usual)

$$A^0 = -s_H \phi^{0,i} + c_H \chi^{0,i}$$

Two charged scalars:

(one fermiophilic and one vectorphilic, but they mix in general)

$$H_f^+ = -s_H \phi^+ + c_H \left(\sqrt{\frac{5}{8}} \chi^{+1} - \sqrt{\frac{3}{3}} (\chi^{-1})^* \right),$$
$$H_V^+ = \sqrt{\frac{3}{8}} \chi^{+1} + \sqrt{\frac{5}{8}} (\chi^{-1})^*$$

A doubly-charged scalar, that couples to W^+W^+ :

$$H^{++} = \chi^{+2}$$

Some higher-charged states:

$$\chi^{+3}, \quad \chi^{+4}, \quad \chi^{+5}$$

- No H_5^0 ; would-be H_5^+ can mix with fermiophilic state
- Rely on H^{++} to constrain higher-isospin vacuum condensate

Septet model (work in progress)

$$H^{++}W_{\mu}^{-}W_{\nu}^{-} : i\frac{2M_W^2}{v_{\text{SM}}}(\sqrt{15}s_H)g_{\mu\nu}$$

VBF $H^{\pm\pm} \rightarrow W^{\pm}W^{\pm}$ is as good as ever! \rightarrow VBF like-sign dileptons

VBF $H^{\pm} \rightarrow W^{\pm}Z$ loses its clean interpretation:

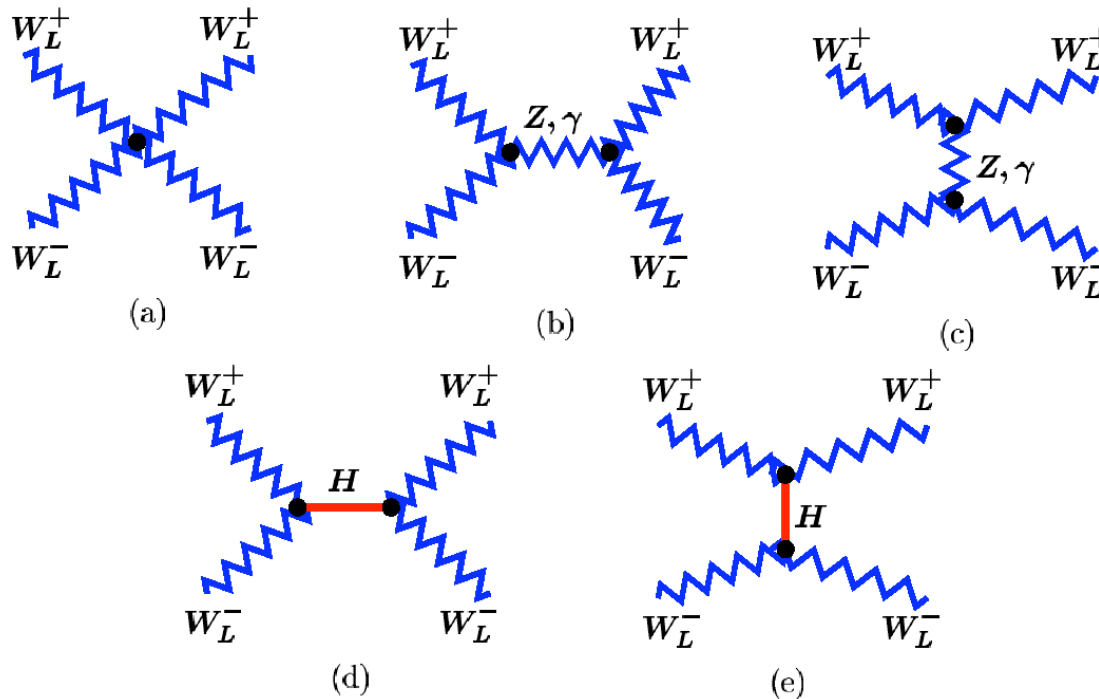
$H^{\pm} \rightarrow \bar{f}f$ competes with $W^{\pm}Z$; $m_{H^{\pm}} \neq m_{H^{\pm\pm}}$ in general

No custodial symmetry: unitarity bound on s_H at high $m_{H^{\pm\pm}}$ is modified, but still remains useful.

Analysis of LHC constraints on septet-state pair production (trileptons; like-sign dileptons) excludes low masses $\rightarrow M_{\text{septet}} \gtrsim 400$ GeV

Alvarado, Lehman & Ostdiek, 1404.3208

Perturbative unitarity of $WW \rightarrow WW$ scattering: E^2 term



Graphic: S. Chivukula

- SM: Higgs exchange cancels E^2/v^2 term in amplitude.
- 2HDM: To preserve cancellation at $E \gg m_H$, need a sum rule:

$$(\kappa_V^h)^2 + (\kappa_V^H)^2 = 1$$

Two-Higgs-Doublet Model: mass splittings

At high mass $H \simeq \phi_0^{0,r}$, $A = \phi_0^{0,i}$, $H^\pm = \phi_0^\pm$: the BSM Higgses all live (mostly) in a single doublet.

Mass splittings within an SU(2) multiplet come only from EWSB:

$$m_{H^\pm}^2 = Y_2 + Z_3 v^2/2 \quad m_A^2 = m_{H^\pm}^2 + (Z_4 - Z_5)v^2/2$$

$$M_{h,H}^2 = \begin{pmatrix} Z_1 v^2 & Z_6 v^2 \\ Z_6 v^2 & m_A^2 + Z_5 v^2 \end{pmatrix}$$

$$\Delta m^2 \sim \lambda v^2 \text{ and } m^2 \sim M^2 \quad \Rightarrow \quad \Delta m \sim \lambda v^2/M$$

Mass splittings $\Delta m \sim \lambda v \times v/M$

Heavy states become increasingly degenerate at high mass

Compare fermionic decay widths $\propto M$ at fixed coupling

(bosonic decay widths $\propto (v^4/M^4) \times M^3 \sim 1/M$ due to coupling suppression)

Both have theoretical “issues”:

1) Global $SU(2)_L \times SU(2)_R$ is broken by gauging hypercharge.

Gunion, Vega & Wudka 1991

Special relations among param's of *full* gauge-invariant scalar potential can only hold at one energy scale: violated by running due to hypercharge. Garcia-Pepin, Gori, Quiros, Vega, Vega-Morales, Yu 2014

Need the UV completion to be nearby!

2) Can't give the septet a vev through spontaneous breaking without generating a physical massless Goldstone boson.

Have to couple it to the SM doublet through a dimension-7 $X\Phi^*\Phi^5$ term Hisano & Tsumura 2013

Need the UV completion to be nearby!

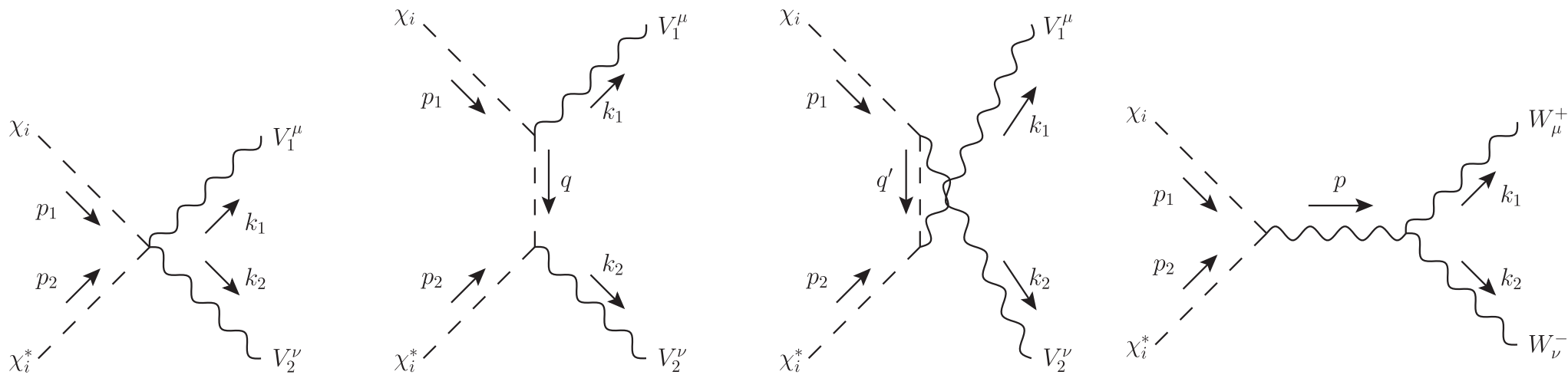
But we need a nearby UV completion to solve the hierarchy problem anyway.

How large can the isospin be?

Hally, HEL, & Pilkington 1202.5073

Consider $2 \rightarrow 2$ scattering amplitudes for $\phi\phi \rightarrow V_T V_T$:
transverse $SU(2)_L$ gauge bosons

- no growth with E^2 ; amplitude depends on weak charges & number of ϕ 's



How large can the isospin be?

Hally, HEL, & Pilkington 1202.5073

Consider $2 \rightarrow 2$ scattering amplitudes for $\phi\phi \rightarrow V_T V_T$:
transverse $SU(2)_L$ gauge bosons

- no growth with E^2 ; amplitude depends on weak charges & number of ϕ 's

General result for complex scalar multiplet with $n = 2T + 1$:

$$a_0^{\max} = \frac{g^2}{16\pi} \frac{(n^2 - 1)\sqrt{n}}{2\sqrt{3}}$$

- Real scalar multiplet: divide by $\sqrt{2}$ to account for smaller number of ϕ 's
- More than one multiplet: add a_0 's in quadrature

Unitarity: require largest amplitude a_0^{\max} satisfies $|\text{Re } a_0| < 1/2$:

- Complex multiplet $\Rightarrow T \leq 7/2$ (8-plet)
- Real multiplet $\Rightarrow T \leq 4$ (9-plet)
- Constraints tighter if more than one large multiplet is present

(generally required in $SU(2)_L \times SU(2)_R$ -symmetric models)

Essentially a requirement that the weak charges not be too large.

Phenomenology: custodial fiveplet $H_5^{++}, H_5^+, H_5^0, H_5^-, H_5^{--}$

Custodial-fiveplet comes only from higher-isospin scalars:
no couplings to fermions!

$s_H^2 \equiv$ fraction of M_W^2, M_Z^2 from higher-isospin scalar

$H_5 VV$ couplings are nonzero: very different from 2HDM!

$$H_5^0 W_\mu^+ W_\nu^- : \quad -i \frac{2M_W^2}{v_{\text{SM}}} \frac{g_5}{\sqrt{6}} g_{\mu\nu},$$

$$H_5^0 Z_\mu Z_\nu : \quad i \frac{2M_Z^2}{v_{\text{SM}}} \sqrt{\frac{2}{3}} g_5 g_{\mu\nu},$$

$$H_5^+ W_\mu^- Z_\nu : \quad -i \frac{2M_W M_Z}{v_{\text{SM}}} \frac{g_5}{\sqrt{2}} g_{\mu\nu},$$

$$H_5^{++} W_\mu^- W_\nu^- : \quad i \frac{2M_W^2}{v_{\text{SM}}} g_5 g_{\mu\nu},$$

But g_5 is also fixed by $VV \rightarrow VV$ unitarization sum rule:

$$(\kappa_V^h)^2 + (\kappa_V^H)^2 - \frac{5}{6} g_5^2 = 1$$

Falkowski, Rychkov & Urbano, 1202.1532 (see also Higgs Hunter's Guide)

(relies on custodial symmetry in scalar sector; same in *all* GGM models)

Detail:

SM + real triplet ξ : $\rho > 1$

SM + complex triplet χ ($Y = 2$): $\rho < 1$

Combine them both: $\langle \chi^0 \rangle = v_\chi$, $\langle \xi^0 \rangle = v_\xi$; doublet $\langle \phi^0 \rangle = v_\phi/\sqrt{2}$

$$\rho = \frac{v_\phi^2 + 4v_\xi^2 + 4v_\chi^2}{v_\phi^2 + 8v_\chi^2} = 1 \text{ when } v_\xi = v_\chi$$

To avoid this being fine-tuned, enforce $v_\xi = v_\chi$ using a symmetry.

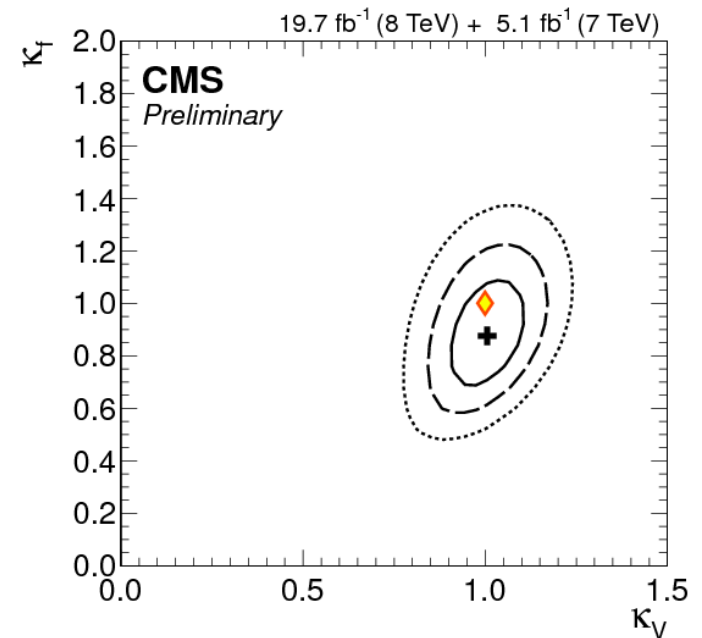
$SU(2)_L \times SU(2)_R$ global symmetry on scalar potential:

- present by accident in SM Higgs sector
- breaks to diagonal subgroup $SU(2)_{\text{custodial}}$ upon EWSB

Implementation of $\kappa_V^h > 1$

hVV coupling always **suppressed** in models with doublets/singlets:

- SM: $2i\frac{M_W^2}{v}g_{\mu\nu}$ ($v \simeq 246$ GeV)
- 2HDM: $2i\frac{M_W^2}{v}g_{\mu\nu} \sin(\beta - \alpha)$
- SM + singlet: $2i\frac{M_W^2}{v}g_{\mu\nu} \cos \alpha$ ($h = \phi \cos \alpha - s \sin \alpha$)



hWW coup can be **enhanced** in models with triplets (or larger):

- SM + **some multiplet X** : $2i\frac{M_W^2}{v}g_{\mu\nu} \cdot \frac{v_X}{v} 2 \left[T(T+1) - \frac{Y^2}{4} \right]$
($Q = T^3 + Y/2$)
- scalar with **isospin ≥ 1**
- must have a **non-negligible vev**
- must **mix into the observed Higgs h**

Motivation for enhanced hVV couplings

Simultaneous enhancement of all the h couplings can hide a non-SM contribution to the Higgs width.

LHC measures **rates** in particular final states:

$$\text{Rate}_{ij} = \frac{\sigma_i \Gamma_j}{\Gamma_{\text{tot}}} = \frac{\kappa_i^2 \sigma_i^{\text{SM}} \cdot \kappa_j^2 \Gamma_j^{\text{SM}}}{\sum_k \kappa_k^2 \Gamma_k^{\text{SM}} + \Gamma_{\text{new}}}$$

All rates will be identical to SM Higgs if all $\kappa_i \equiv \kappa \geq 1$ and

$$\kappa^2 = \frac{1}{1 - \text{BR}_{\text{new}}} \quad \text{BR}_{\text{new}} \equiv \frac{\Gamma_{\text{new}}}{\kappa^2 \Gamma_{\text{tot}}^{\text{SM}} + \Gamma_{\text{new}}}$$

Coupling enhancement hides presence of new decays!
New decays hide presence of coupling enhancement!

Constraint on Γ^{tot} (equivalently on κ) from off-shell $gg (\rightarrow h^*) \rightarrow ZZ$ assumes no new resonances in s -channel: a light H can cancel effect of modified h couplings. [1412.7577](#)

Study concrete models in which $\kappa > 1$ to gain insight.

Most general scalar potential:

Aoki & Kanemura, 0712.4053

Chiang & Yagyu, 1211.2658; Chiang, Kuo & Yagyu, 1307.7526

Hartling, Kumar & HEL, 1404.2640

$$\begin{aligned} V(\Phi, X) = & \frac{\mu_2^2}{2} \text{Tr}(\Phi^\dagger \Phi) + \frac{\mu_3^2}{2} \text{Tr}(X^\dagger X) + \lambda_1 [\text{Tr}(\Phi^\dagger \Phi)]^2 \\ & + \lambda_2 \text{Tr}(\Phi^\dagger \Phi) \text{Tr}(X^\dagger X) + \lambda_3 \text{Tr}(X^\dagger X X^\dagger X) \\ & + \lambda_4 [\text{Tr}(X^\dagger X)]^2 - \lambda_5 \text{Tr}(\Phi^\dagger \tau^a \Phi \tau^b) \text{Tr}(X^\dagger t^a X t^b) \\ & - M_1 \text{Tr}(\Phi^\dagger \tau^a \Phi \tau^b) (UXU^\dagger)_{ab} - M_2 \text{Tr}(X^\dagger t^a X t^b) (UXU^\dagger)_{ab} \end{aligned}$$

9 parameters, 2 fixed by M_W and $m_h \rightarrow$ free parameters are m_H , m_3 , m_5 , v_χ , α plus two triple-scalar couplings.

Dimension-3 terms usually omitted by imposing Z_2 sym. on X .

These dim-3 terms are essential for the model to possess a decoupling limit!

$(UXU^\dagger)_{ab}$ is just the matrix X in the Cartesian basis of $SU(2)$, found using

$$U = \begin{pmatrix} -\frac{1}{\sqrt{2}} & 0 & \frac{1}{\sqrt{2}} \\ -\frac{i}{\sqrt{2}} & 0 & -\frac{i}{\sqrt{2}} \\ 0 & 1 & 0 \end{pmatrix}$$

Phenomenology I: custodial singlets h^0, H^0

Vevs: $\langle \Phi \rangle = (v_\phi/\sqrt{2})I_{2 \times 2}$, $\langle X_n \rangle = v_n I_{n \times n} \implies$ define $c_H = v_\phi/v$

Recall $c_H^2 =$ fraction of $M_{W,Z}^2$ coming from doublet vev

Two custodial-singlet states are mixtures of $\phi^{0,r}$ and custodial singlet from higher-isospin scalars:

$$h^0 = c_\alpha \phi^{0,r} - s_\alpha H_1'^0, \quad H^0 = s_\alpha \phi^{0,r} + c_\alpha H_1'^0$$

Couplings to W^+W^-/ZZ and $\bar{f}f$:

$$\begin{aligned} \kappa_V^h &= c_\alpha c_H - \sqrt{A} s_\alpha s_H & \kappa_f^h &= c_\alpha / c_H \\ \kappa_V^H &= s_\alpha c_H + \sqrt{A} c_\alpha s_H & \kappa_f^H &= s_\alpha / c_H \end{aligned}$$

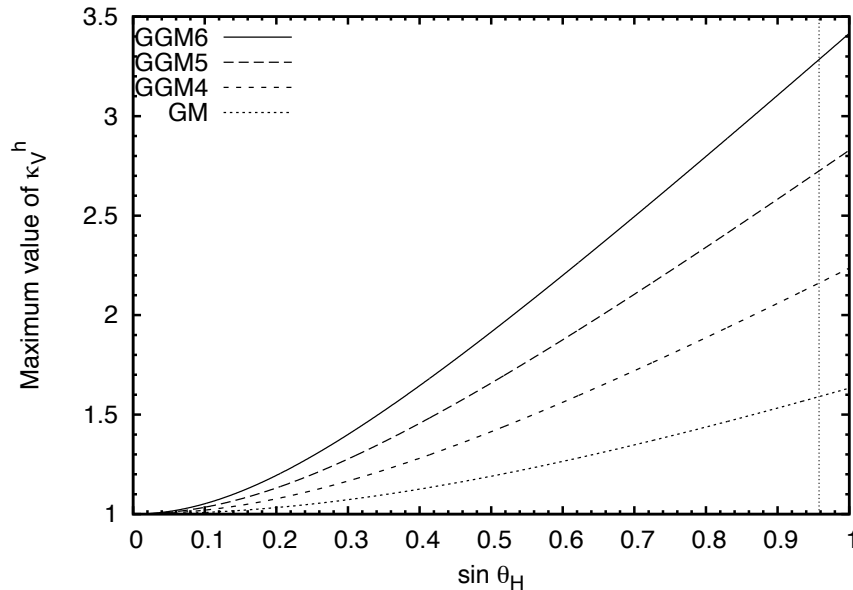
Note that $\kappa_V^h \leq [1 + (A-1)s_H^2]^{1/2}$, saturated when $\kappa_f^H = 0$.

\sqrt{A} factor comes from the generators: $A = 4T(T+1)/3$

$$A_{\text{GM}} = 8/3, \quad A_{\text{GGM4}} = 15/3, \quad A_{\text{GGM5}} = 24/3, \quad A_{\text{GGM6}} = 35/3$$

(Septet model: $A_7 = 16$)

Large enhancements of κ_V^h possible for large s_H (up to about 3.3):



Vertical line:

y_t perturbativity $\rightarrow \tan \theta_H < 10/3$

HEL & Rentala, 1502.01275

Impossible to have $\kappa_V^h, \kappa_f^h = 1$ without $s_H \rightarrow 0$:

High-precision measurements of Higgs couplings will constrain higher-isospin vacuum condensate.

$$\begin{aligned} \kappa_V^h &= c_\alpha c_H - \sqrt{A} s_\alpha s_H & \kappa_f^h &= c_\alpha / c_H \\ \kappa_V^H &= s_\alpha c_H + \sqrt{A} c_\alpha s_H & \kappa_f^H &= s_\alpha / c_H \end{aligned}$$

Phenomenology II: custodial triplet H_3^+, H_3^0, H_3^-

Couplings to fermions are the same as H^\pm, A^0 in [Type-I 2HDM](#):

$$H_3^0 \bar{u}u : \quad \frac{m_u}{v} \tan \theta_H \gamma_5, \quad H_3^0 \bar{d}d : \quad -\frac{m_d}{v} \tan \theta_H \gamma_5,$$

$$H_3^+ \bar{u}d : \quad -i \frac{\sqrt{2}}{v} V_{ud} \tan \theta_H (m_u P_L - m_d P_R),$$

$$H_3^+ \bar{\nu} \ell : \quad i \frac{\sqrt{2}}{v} \tan \theta_H m_\ell P_R.$$

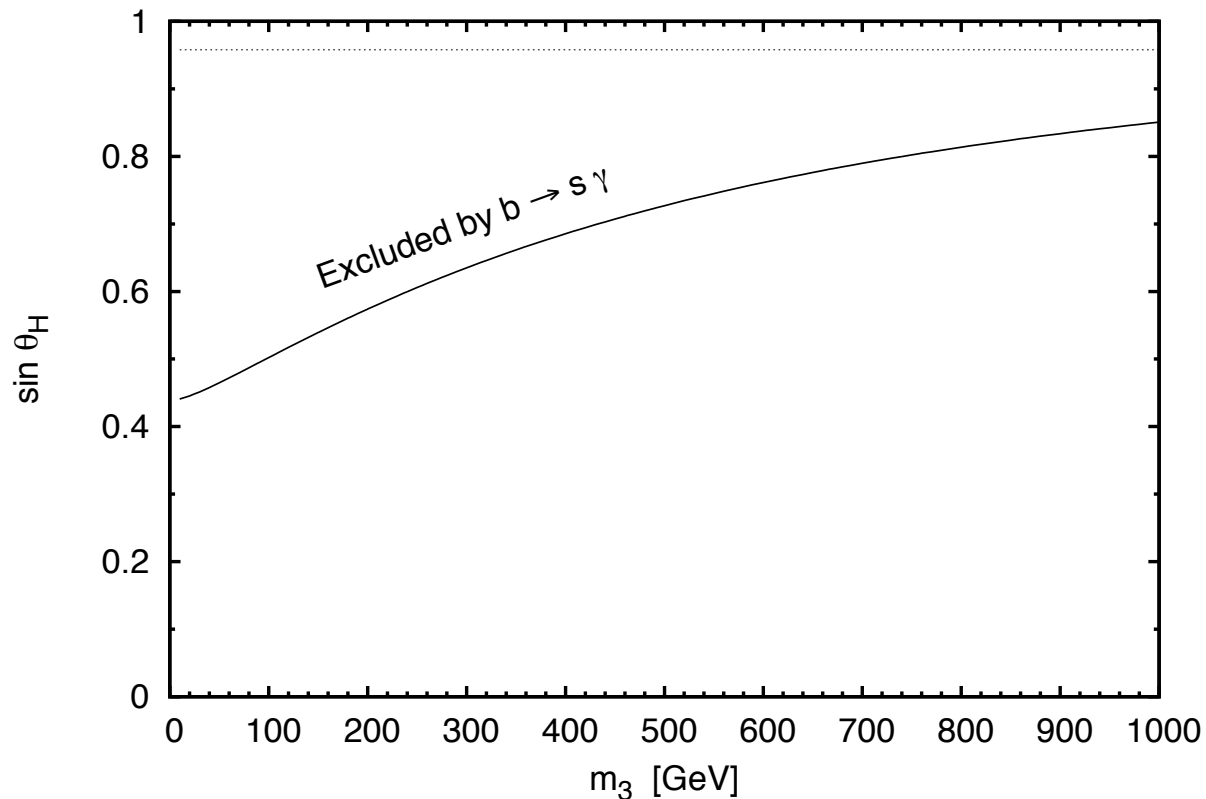
$Z H_3^+ H_3^-$ also the same as in 2HDM:

constraints from $b \rightarrow s\gamma$, $B_s \rightarrow \mu\mu$, R_b , etc translate directly.

Vector-phobic: no $H_3 VV$ couplings at tree level.

Constraint from $b \rightarrow s\gamma$

- H_3^+ in the loop: measurement constrains m_3 and $\sin\theta_H$
- Holds for all generalizations of Georgi-Machacek model
 - Also constrains septet model, but not identical



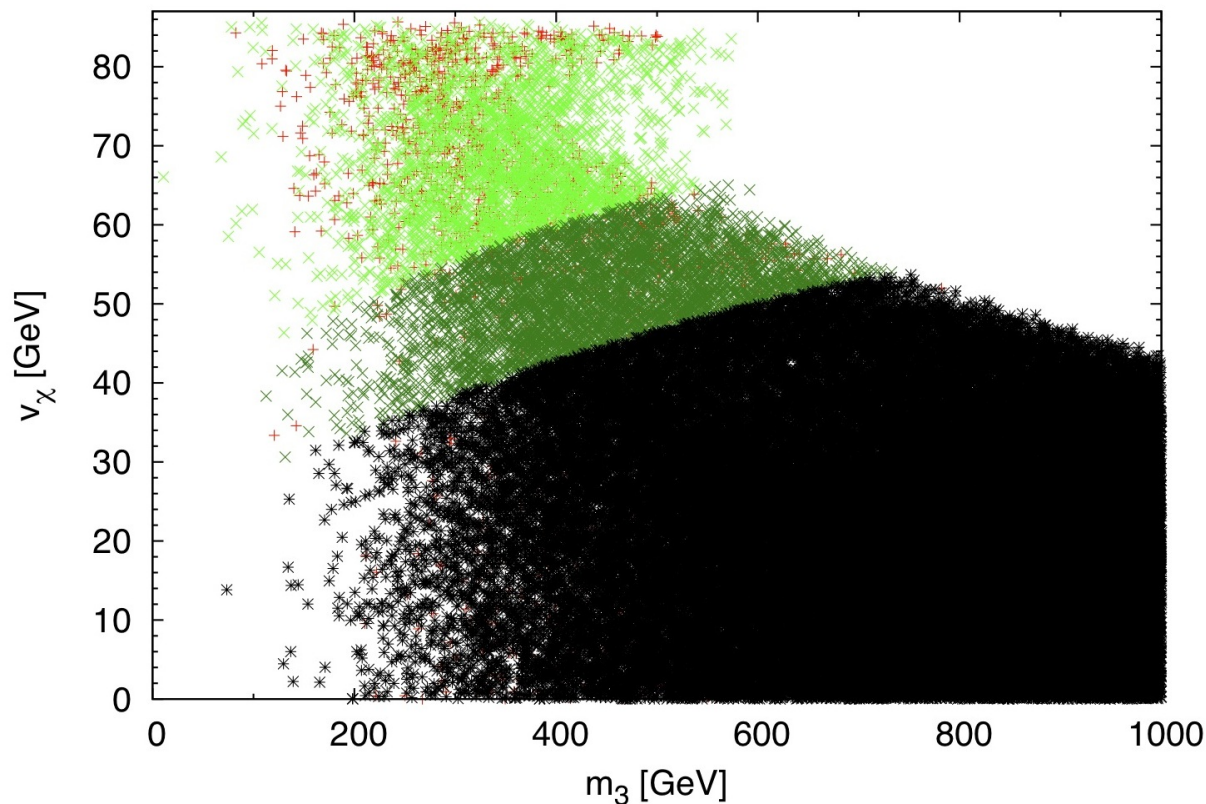
Hartling, Kumar & HEL, 1410.5538

Constraint from $b \rightarrow s\gamma$ in original Georgi-Machacek model:

Apply to original Georgi-Machacek model: $s_H^2 < 0.56$

Can constrain because high s_H at high m_3 is theoretically inaccessible.

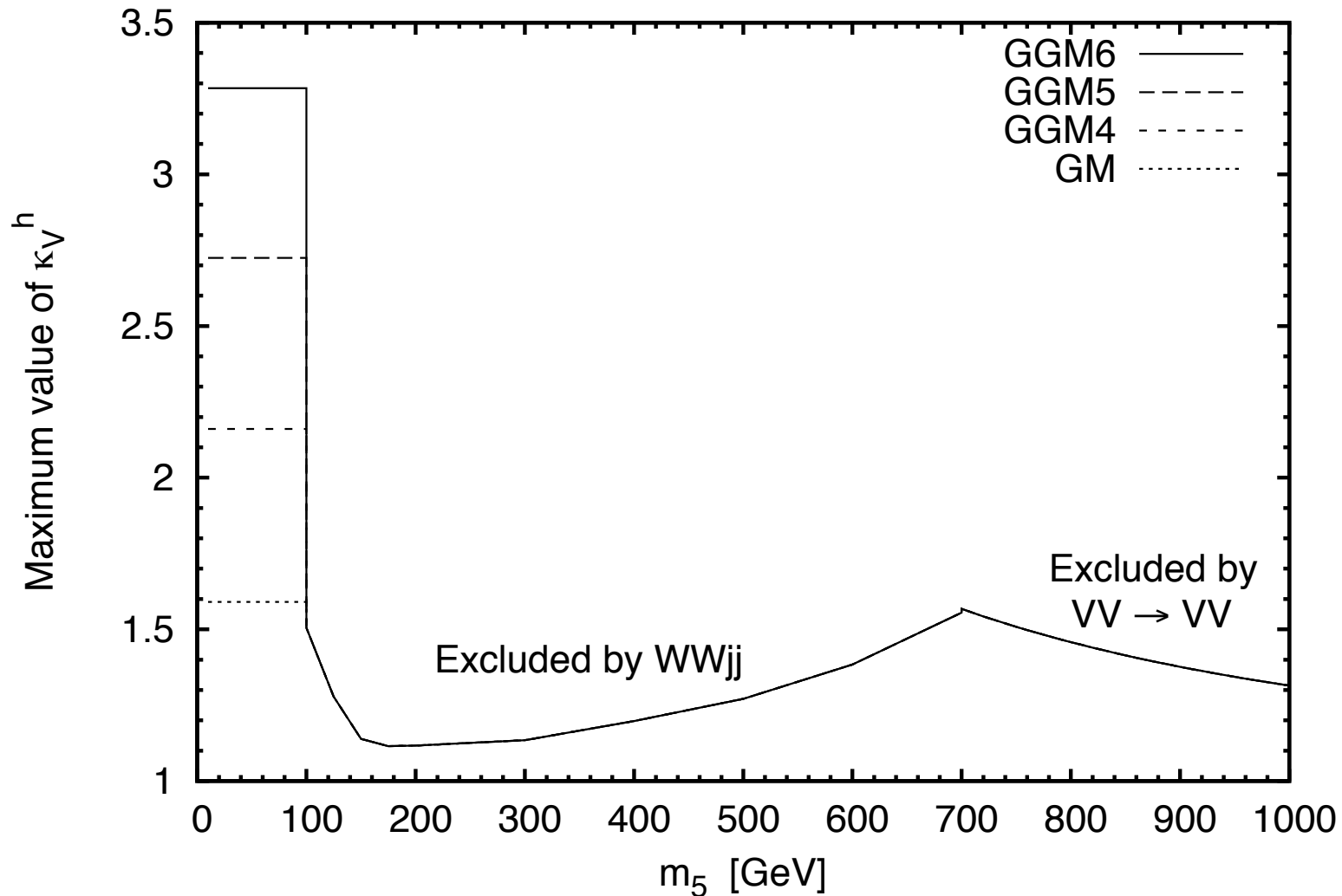
\Rightarrow at least 44% of $M_{W,Z}^2$ is due to doublet vev (Model-dependent bound)



Hartling, Kumar & HEL, 1410.5538 (Light green points excluded by $b \rightarrow s\gamma$)

Heather Logan (Carleton U.) Higgs physics beyond the Standard Model APS April 2016

All the $SU(2)_L \times SU(2)_R$ models are the same when expressed in terms of g_5 : use sum rule, $(\kappa_V^h)^2 \leq 1 + 5g_5^2/6$



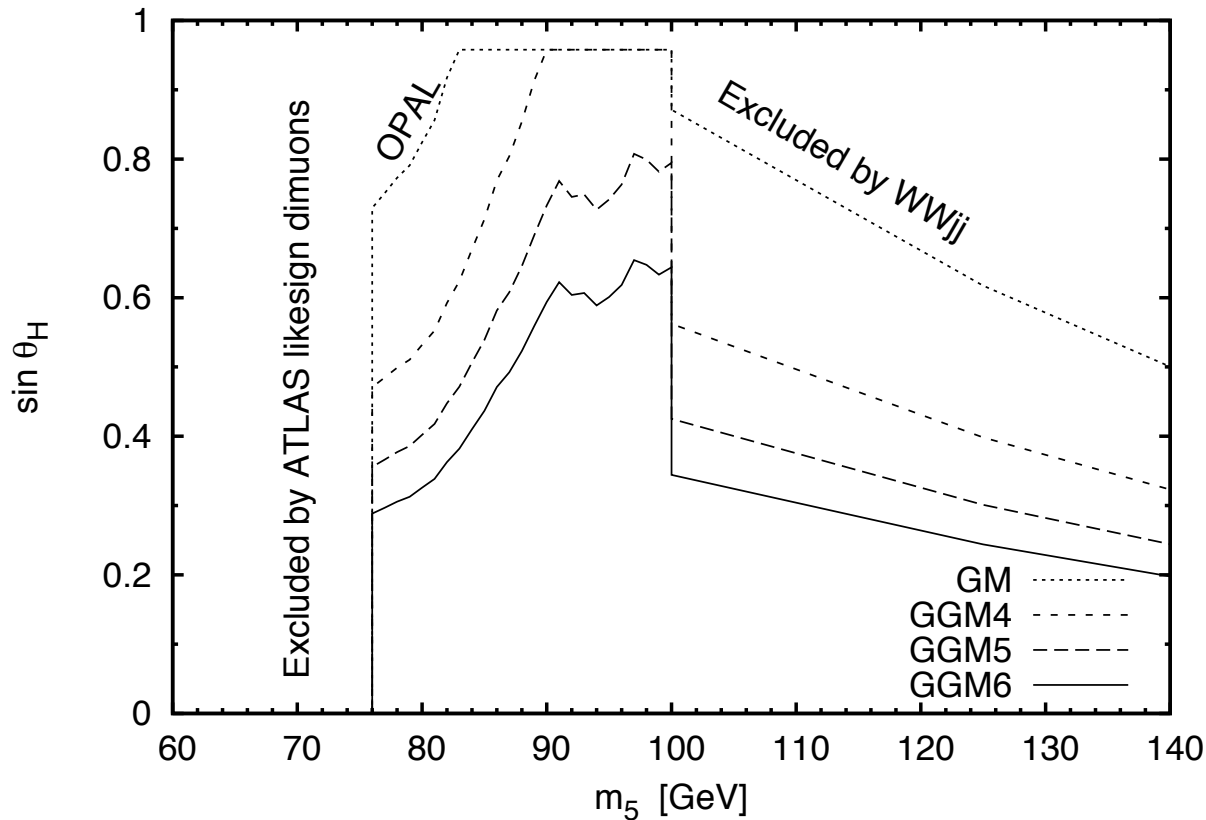
$\Rightarrow \kappa_V^h \lesssim 1.57$ for $m_5 > 100$ GeV

HEL & Rentala, 1502.01275

What about lower H_5 masses?

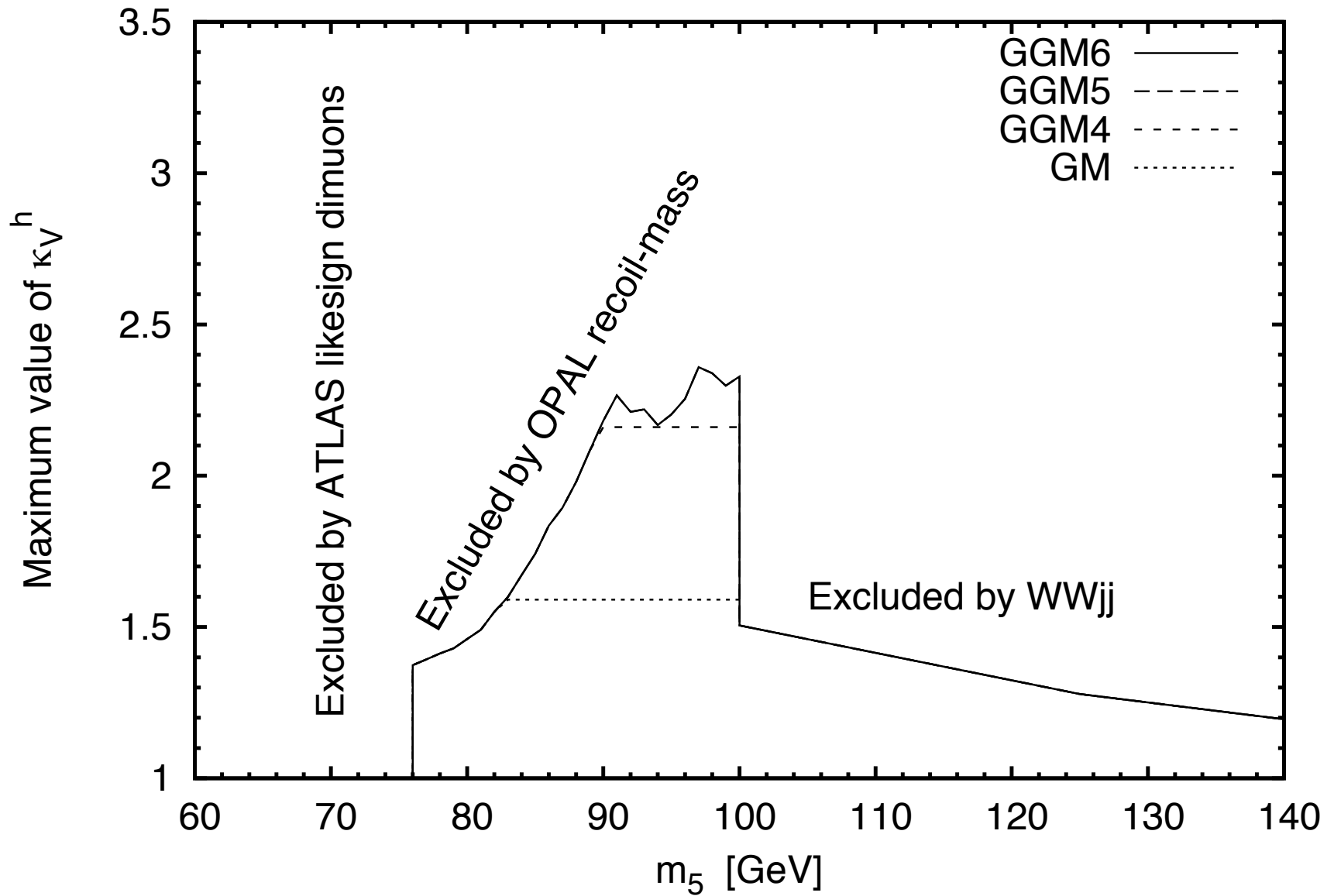
Decay-mode-independent OPAL search for $Z + S^0$ production:
 constrain $H_5^0 ZZ$ coupling $\propto g_5$

OPAL, hep-ex/0206022



HEL & Rentala, 1502.01275; used HiggsBounds 4.2.0 for OPAL exclusion contour

Takes advantage of mass degeneracy H_5^0 and H_5^{++}



$\Rightarrow \kappa_V^h \lesssim 2.36$ for all m_5 !

HEL & Rentala, 1502.01275

compare $\kappa_V^h \lesssim 3.3$ in unconstrained GGM6

~~ Heavy BSM Higgs Rules of Thumb ~~

- #1. Heavy Higgs couplings to WW/ZZ generically fall like $1/M_H$ except sometimes there are tighter indirect constraints
except in 2HDM they fall like $1/M_H^2$ (reason: no cubic terms in V)
SM+triplets model $H_5^{0,\pm,\pm\pm}$ couplings to VV fall like $1/M$
- #2. Heavy Higgs couplings to fermions need not be suppressed in Type-II 2HDM can even be enhanced $\sim \tan\beta$ (down-type & leptons) except in SM+singlet where fermion couplings are tied to VV couplings except in SM+triplets where fermion coups due to doublet mixing $\sim v/M$
- #3. Heavy Higgs states become more degenerate at high mass generic for the members of an $SU(2)$ multiplet: $\Delta m \sim \lambda v^2/M$

Spectrum separates into light SM-like Higgs doublet and heavy complete $SU(2)_L$ multiplet(s). Keys are (1) degree of mixing and/or vev carried by heavy multiplet; (2) heavy multiplet coupling to fermions (doublets only).