

# Hit finding and pad response function for the LCTPC using resistive Micromegas

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On behalf of the LCTPC collaboration





# Outline

- **Intro: LCTPC Collaboration and MPGD**
- **Charge dispersion and Signal Pulse**
  - **Electronic response**
  - **Definition of amplitude and time ( $A_i, t_i$ ) for a pad**
  - **Conceptual Pad Response Function (PRF)**
- **Determination of PRF parameters (calibration)**
  - **Parameterization of the PRF**
- **Results**
  - **Field distortions**
  - **Transverse resolution**
- **Summary**

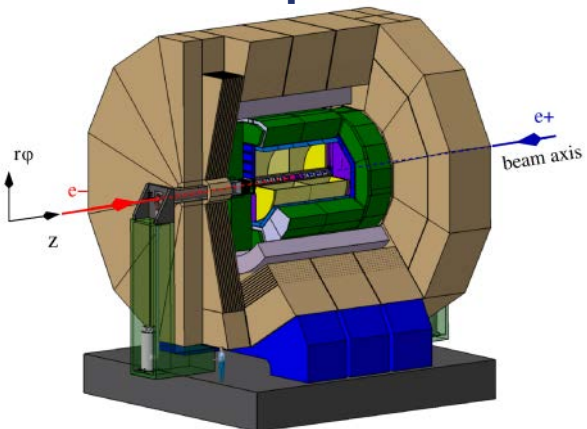


# Time Projection Chamber (TPC) for ILD

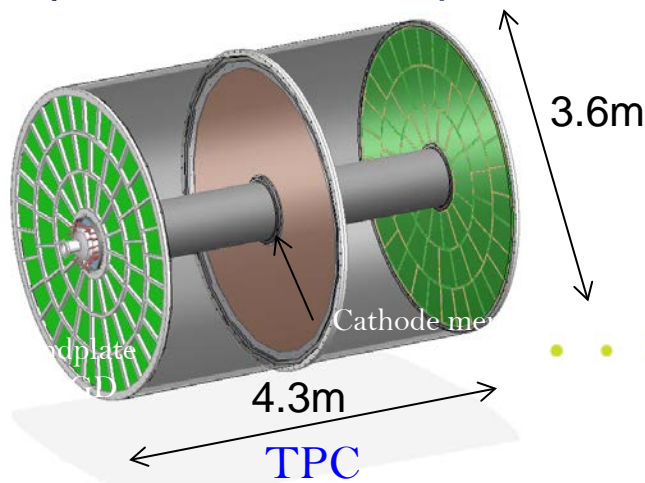
TPC is the central tracker for International Linear Detector

- Large number of 3D points → continuous tracking
- Good track separation and pattern recognition
- Low material budget inside the calorimeters (*c.f.* PFA)
  - Barrel:  $\sim 5\% X_0$
  - Endplates:  $\sim 25\% X_0$
- Two options for endplate readout:
  - **GEM**:  $1.2 \times 5.8 \text{ mm}^2$  pads
  - **Resistive Micromegas**:  $3 \times 7 \text{ mm}^2$  pads
- Alternative: **pixel** readout with pixel size  $\sim 55 \times 55 \mu\text{m}^2$

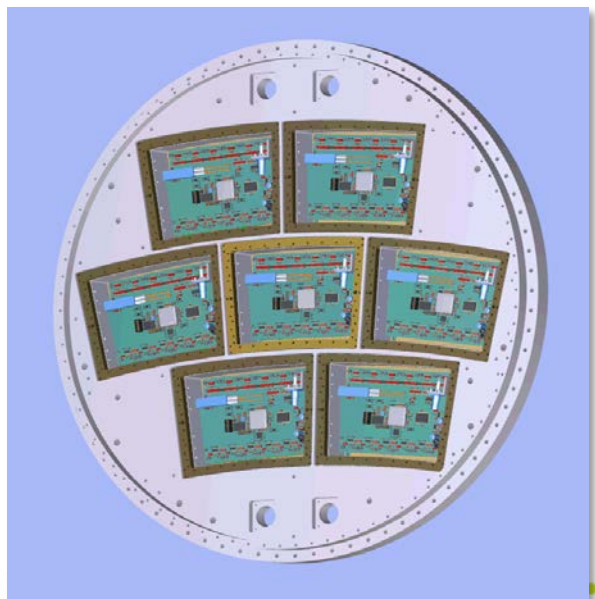
- TPC Requirements :**
- **Momentum resolution:**  
 $\delta(1/p_T) < 9 \times 10^{-5} \text{ GeV}^{-1}$
  - **Single hit resolution 3.5T:**  
 $\sigma(r\phi) < 100 \mu\text{m}$   
 $\sigma(z) < 500 \mu\text{m}$
  - **Tracking eff.** for  $p_T > 1 \text{ GeV}$ :  
97%
  - **dE/dx resolution**  $\sim 5\%$



ILD



TPC



Large Prototype



# Micro Pattern Gas Detector (MPGD)

## Technology choice for TPC readout: Micro Pattern Gas Detector

- more robust than wires
- fast signal & high gain
- better ageing properties
- no  $E \times B$  effect
- low ion backdrift
- easier to manufacture

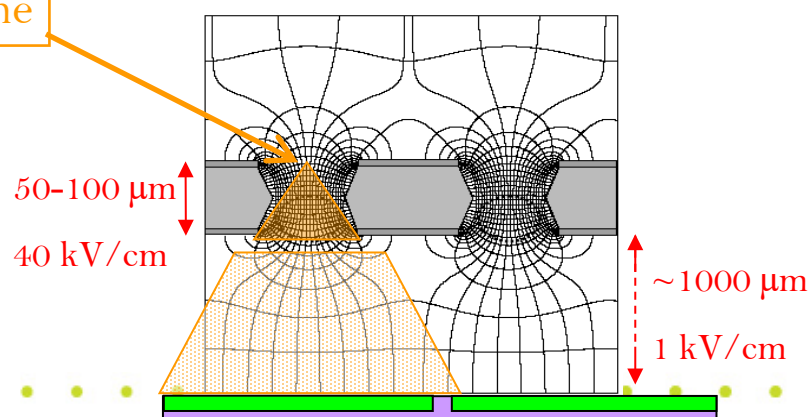
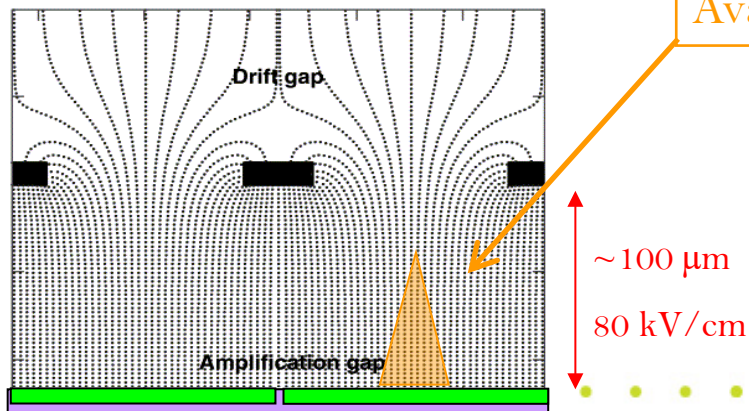
### Micromegas (MM)

- MICROMesh Gaseous Structure
- metallic micromesh (typical pitch  $50\mu\text{m}$ )
- supported by  $50\mu\text{m}$  pillars, multiplication between anode and mesh, high gain


### GEM

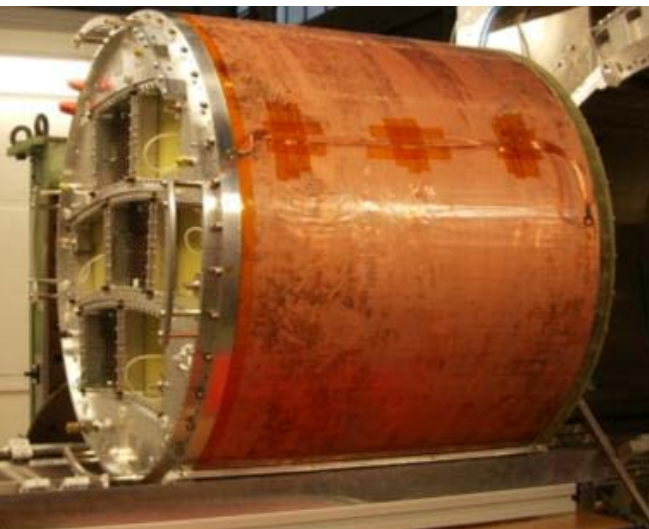
- Gas Electron Multiplier
- 2 copper foils separated by kapton
- multiplication takes place in holes, with 2-3 layers needed

### Avalanche

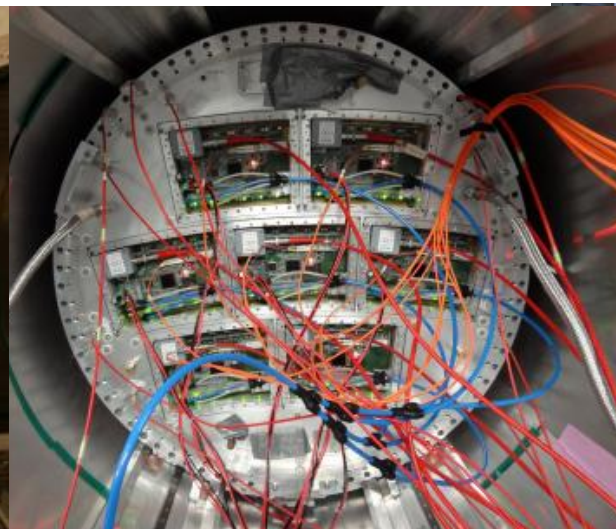


# MPGD readout modules under studied

Readout		Pad Size	Electronics	Groups
MPGDs	Double GEMs (Laser-etched)	(~ 1 × 6 mm <sup>2</sup> Pad)	ALTRO	Asia
	Triple GEMs (wet-etched)			DESY
	Micromegas (Resistive anode)	(~ 3 × 7 mm <sup>2</sup> Pad)	AFTER	Saclay- Carleton 



Large Prototype TPC



Endplate + 7 Micromegas modules

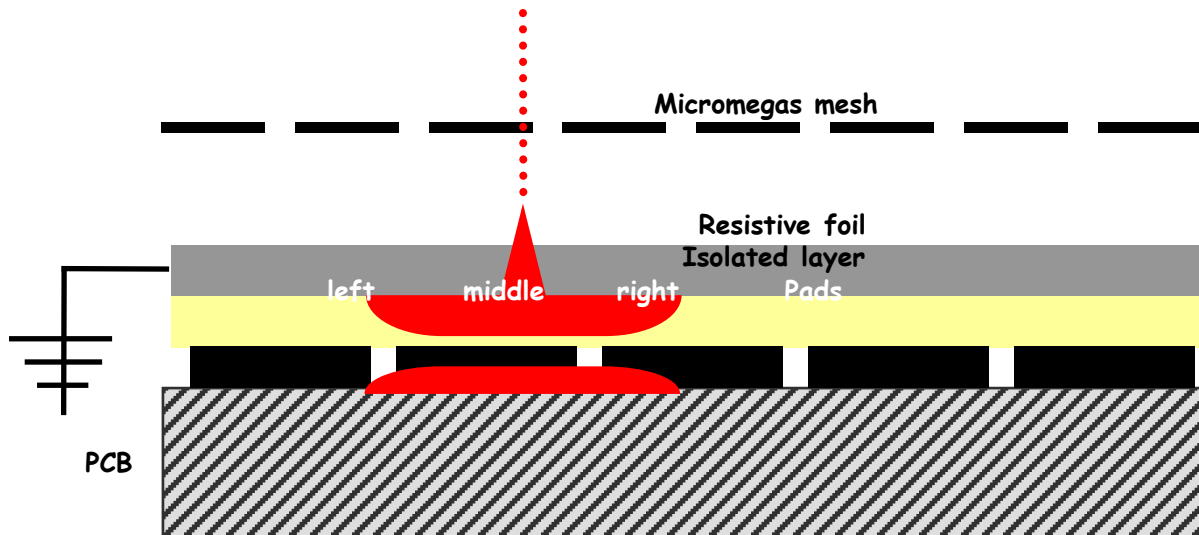


1T PC Magnet



# Charge Dispersion

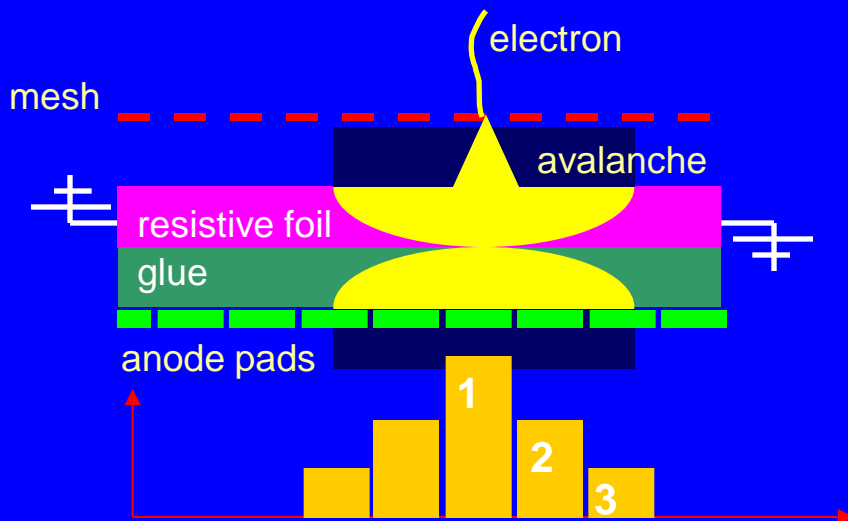
## Resistive Anode



# Charge dispersion

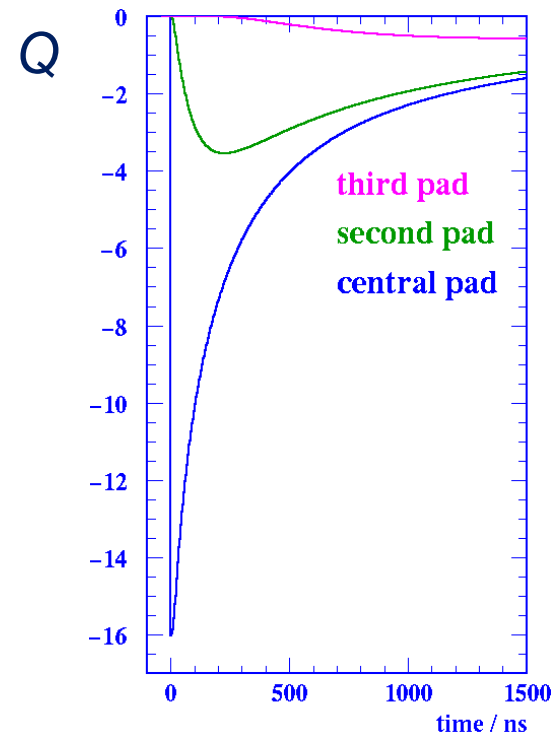
- A high resistivity film bonded to a readout plane with an insulating spacer
- 2D continuous RC network defined by material properties and geometry.
- point charge at  $r = 0$  &  $t = 0$  disperses with time.

## Micromegas + resistive anode



$$\frac{\partial \rho}{\partial t} = \frac{1}{RC} \left[ \frac{\partial^2 \rho}{\partial r^2} + \frac{1}{r} \frac{\partial \rho}{\partial r} \right]$$

$$\Rightarrow \rho(r, t) = \frac{RC}{2t} e^{-\frac{r^2 RC}{4t}}$$





Transverse diffusion

# Pulse shape origin

$$T(x) = \frac{1}{\sigma_x \sqrt{2\pi}} \exp\left(\frac{-x^2}{2\sigma_x^2}\right)$$

Longitudinal diffusion

$$L(t) = \frac{1}{\sigma_t \sqrt{2\pi}} \exp\left(\frac{-t^2}{2\sigma_t^2}\right)$$

Induction gap

$$R(t) = \begin{cases} \frac{t}{T_{rise}} & 0 < t < T_{rise} \\ = 1 & t > T_{rise} \\ = 0 & t < 0 \end{cases}$$

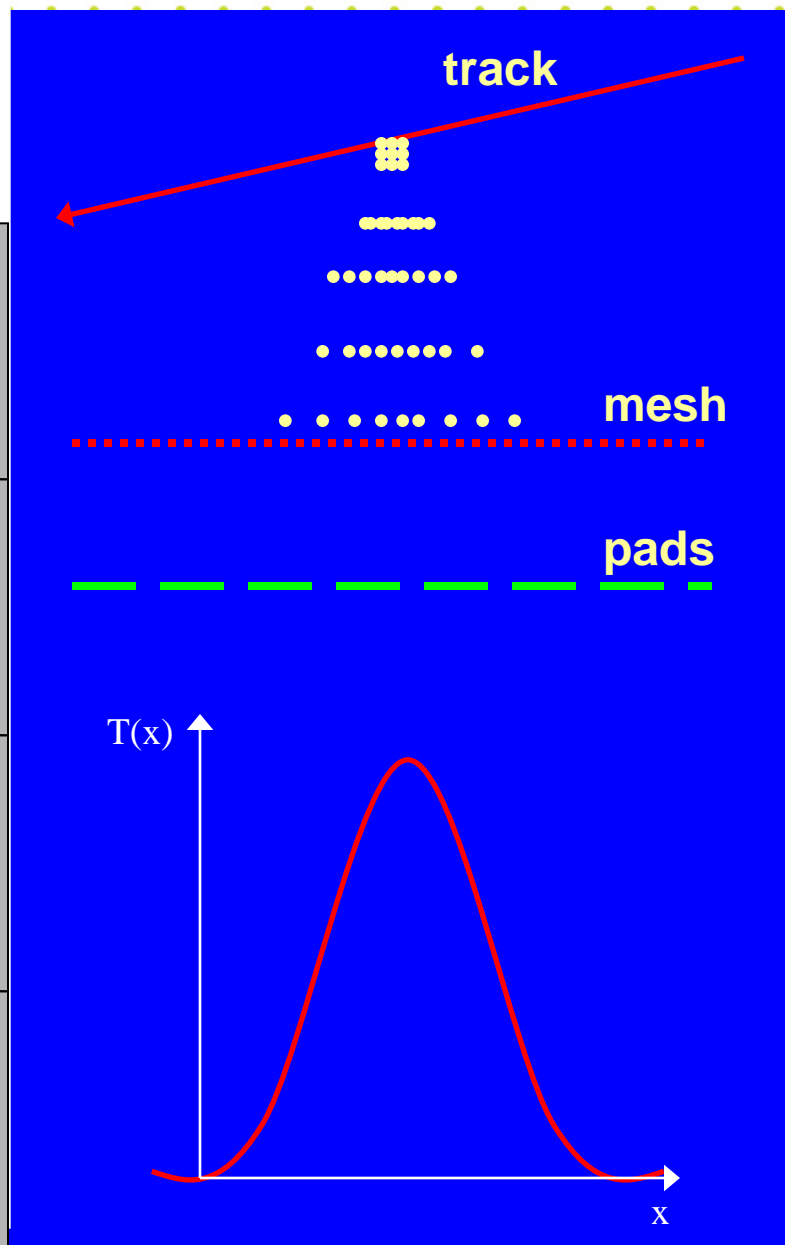
Preamplifier Response

$$H(t) = \begin{cases} \exp\left(-\frac{t}{t_f}\right) \left(1 - \exp\left(\frac{t}{t_r}\right)\right) & t > 0 \\ = 0 & t < 0 \end{cases}$$

Resistive foil + glue

$$\rho(x, y, t) = \left(\frac{1}{\sigma_t \sqrt{\pi t h}}\right)^2 \exp\left(\frac{-(x^2 + y^2)}{4th}\right)$$

$$h = 1/RC$$







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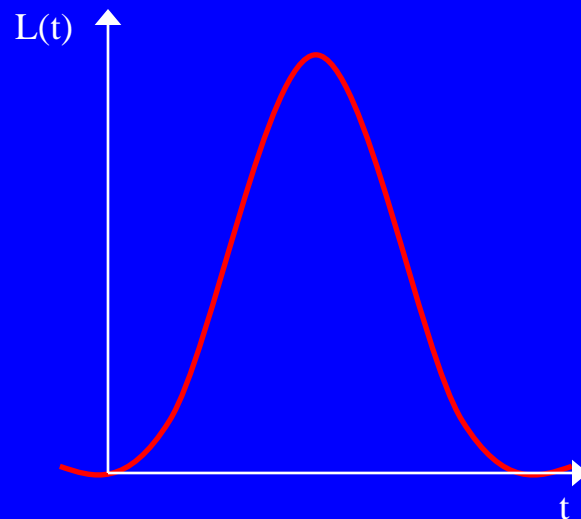
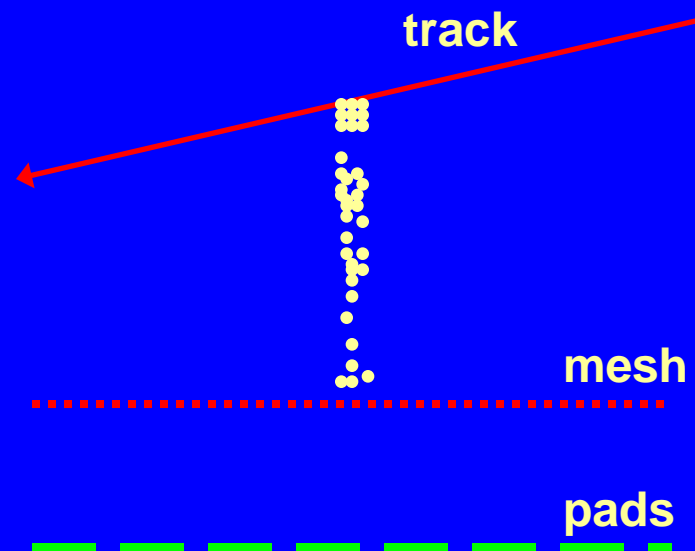
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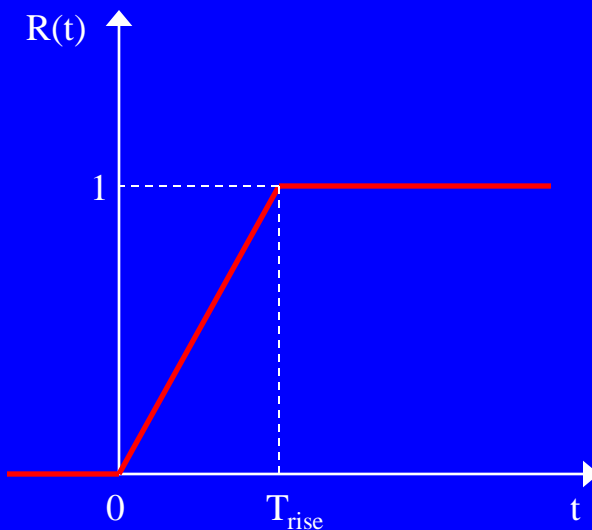
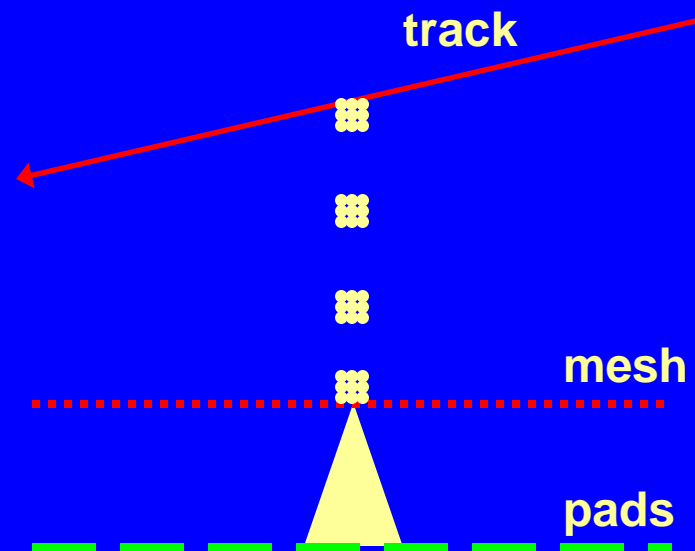
Preamplifier Response

$$A(t) = \begin{cases} \exp\left(-\frac{t}{t_f}\right) \left(1 - \exp\left(\frac{t}{t_r}\right)\right) & t > 0 \\ 0 & t < 0 \end{cases}$$

Resistive foil + glue

$$\rho(x, y, t) = \left(\frac{1}{\sigma_t \sqrt{\pi t h}}\right)^2 \exp\left(\frac{-(x^2 + y^2)}{4th}\right)$$

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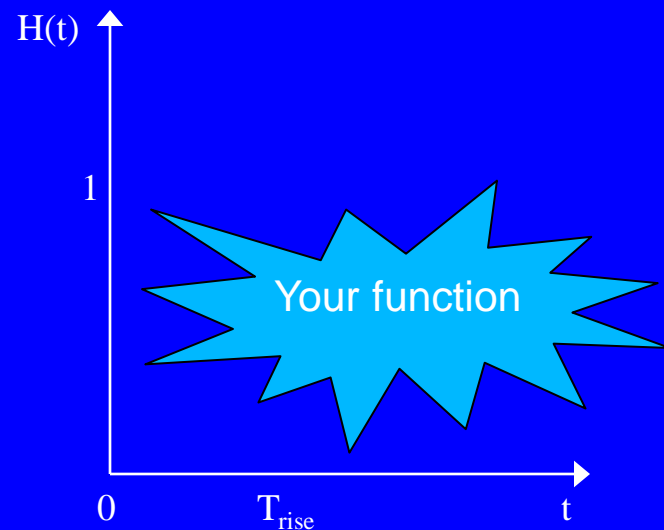
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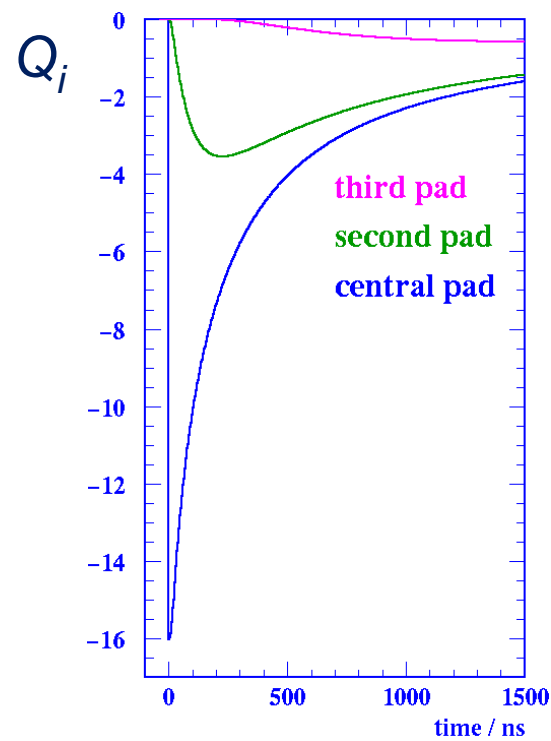
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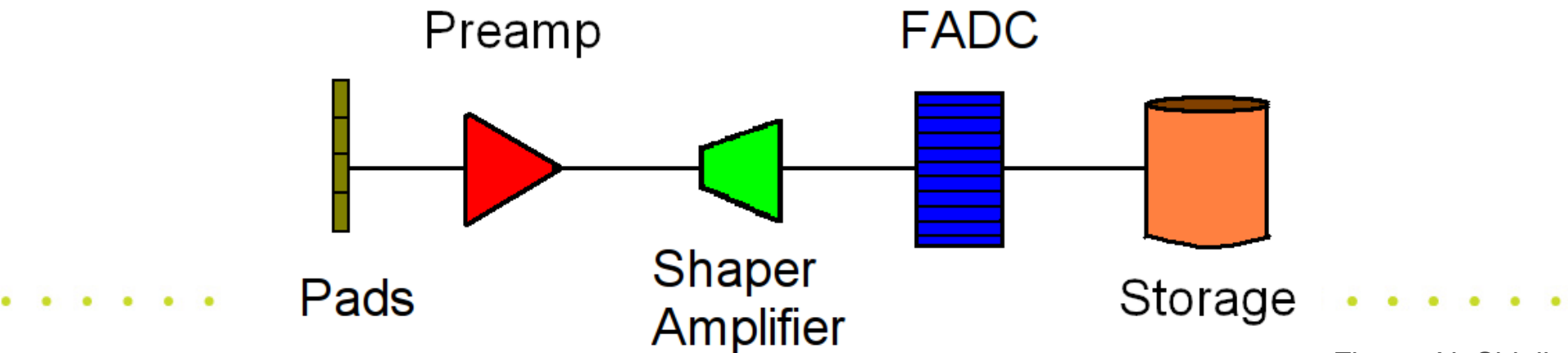
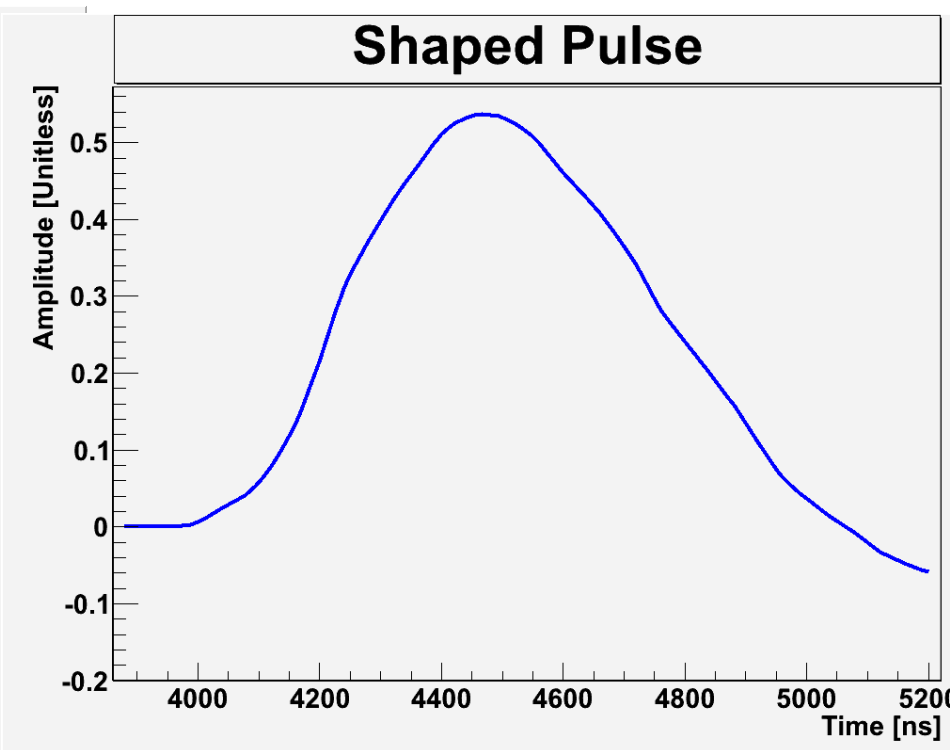
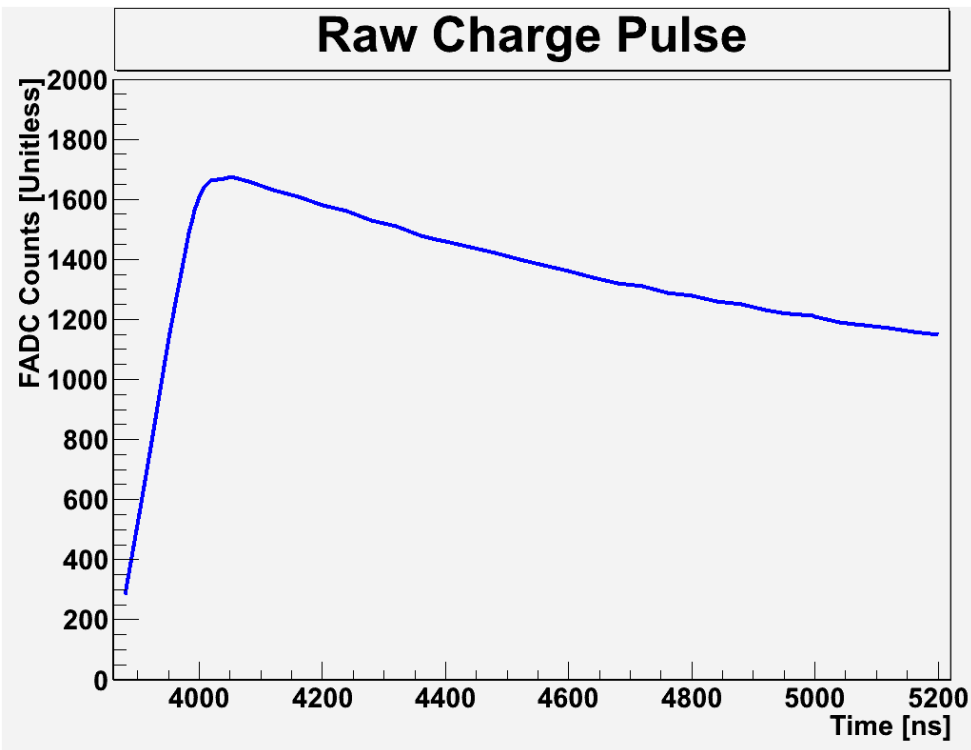
$$h = 1/RC$$

$$Q_i = \int \rho_i(r) dr$$

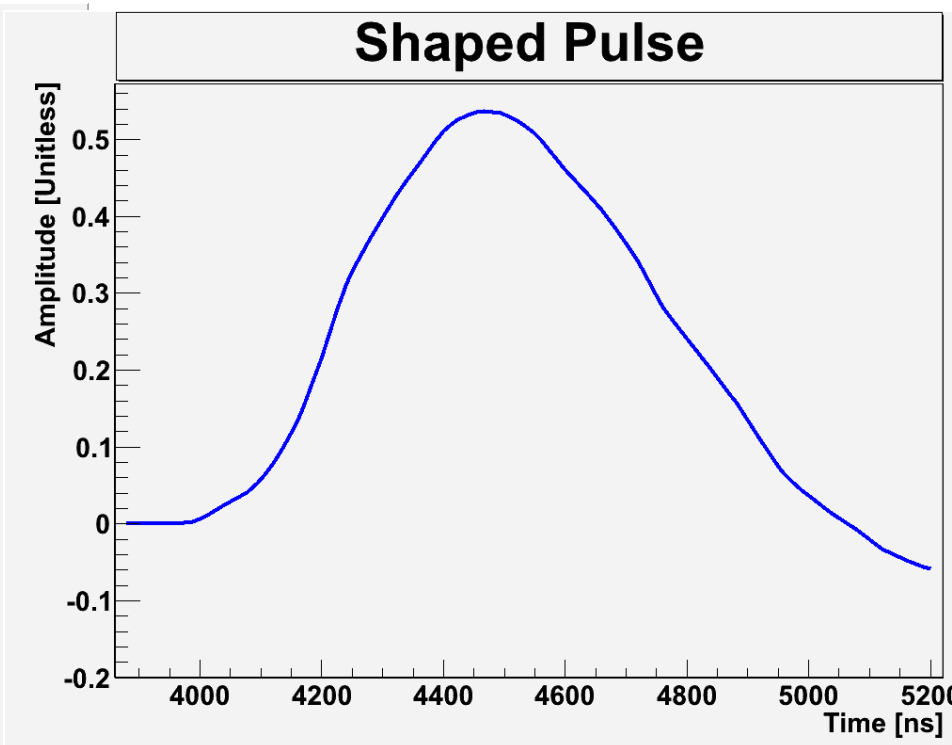
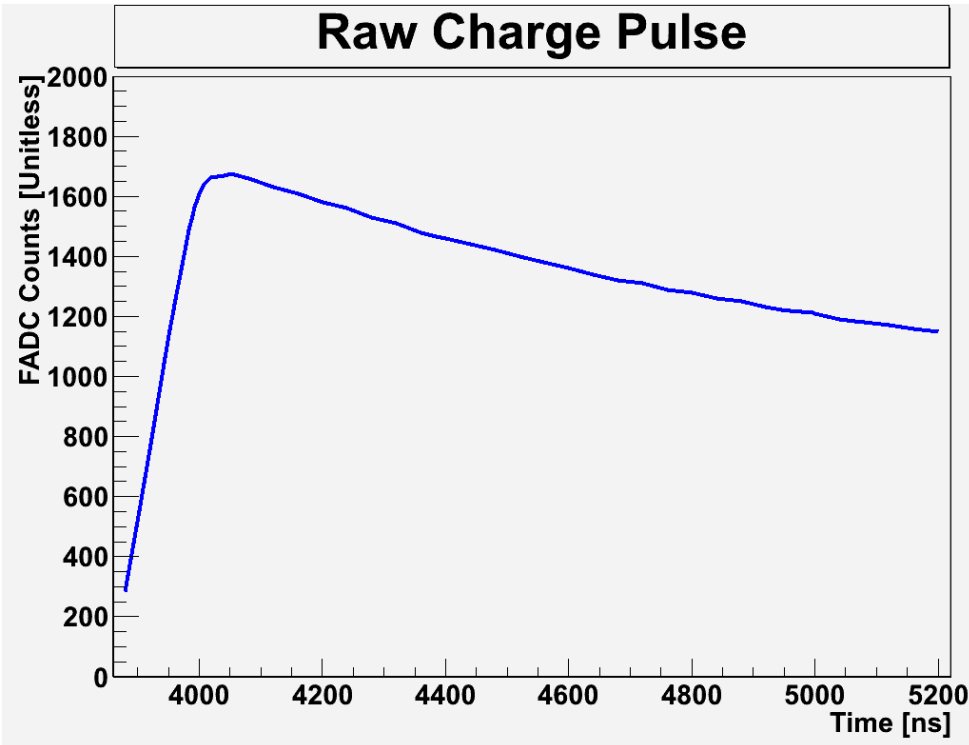
Stand alone simulation



# Raw Charge Shape versus Shaped Pulse



# Raw Charge Shape versus Shaped Pulse

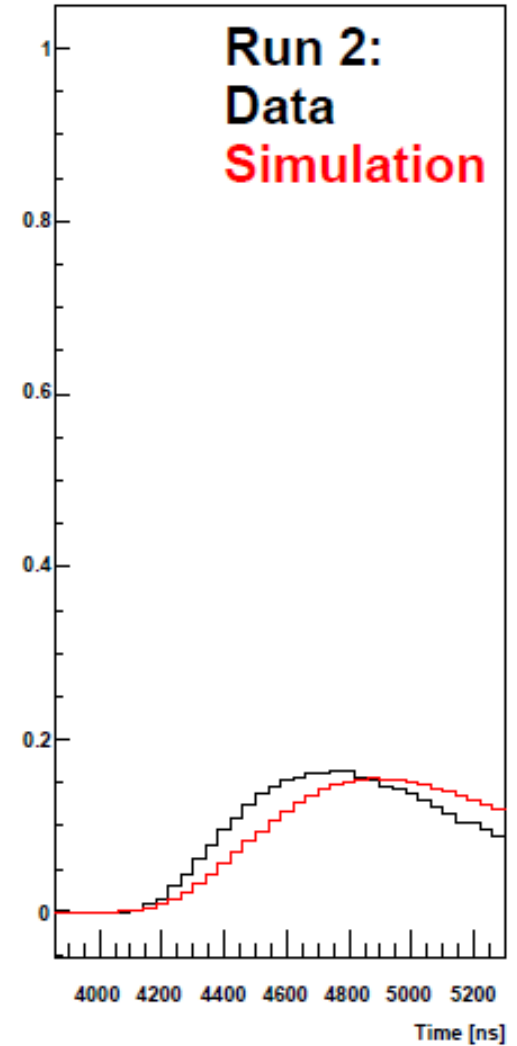
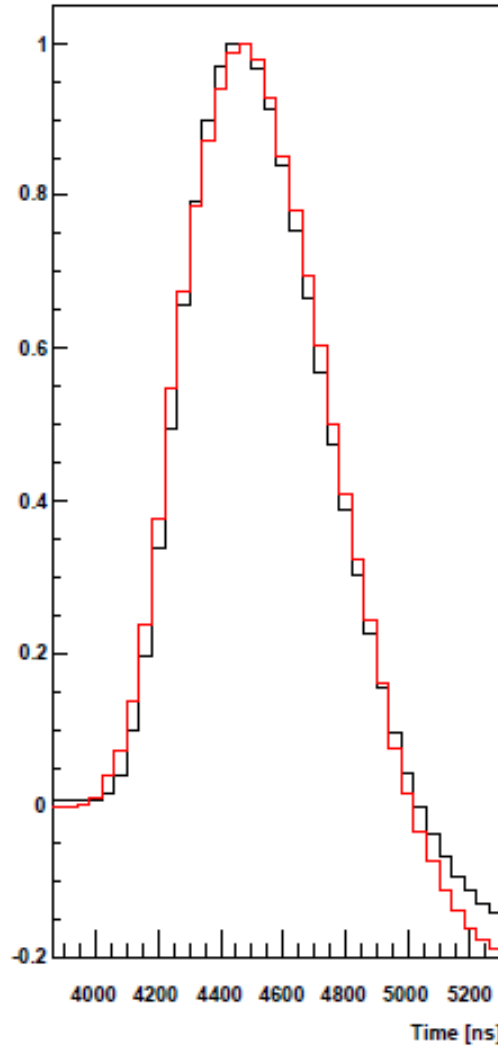
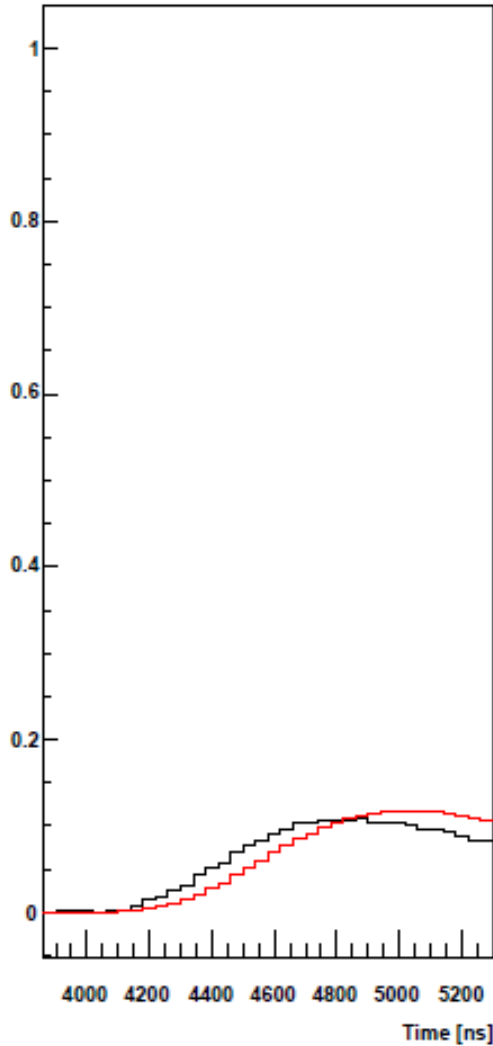


$$H(t) = A_0 \left( \frac{t}{\tau} \right)^3 \sin\left(\frac{t}{b\tau}\right) \exp\left(-\frac{t}{\tau}\right)$$

from Eric Delagnes et al at Saclay



# Stand-Alone Calculation



CRUCIAL TO CHARACTERIZE DETECTOR PARAMETERS



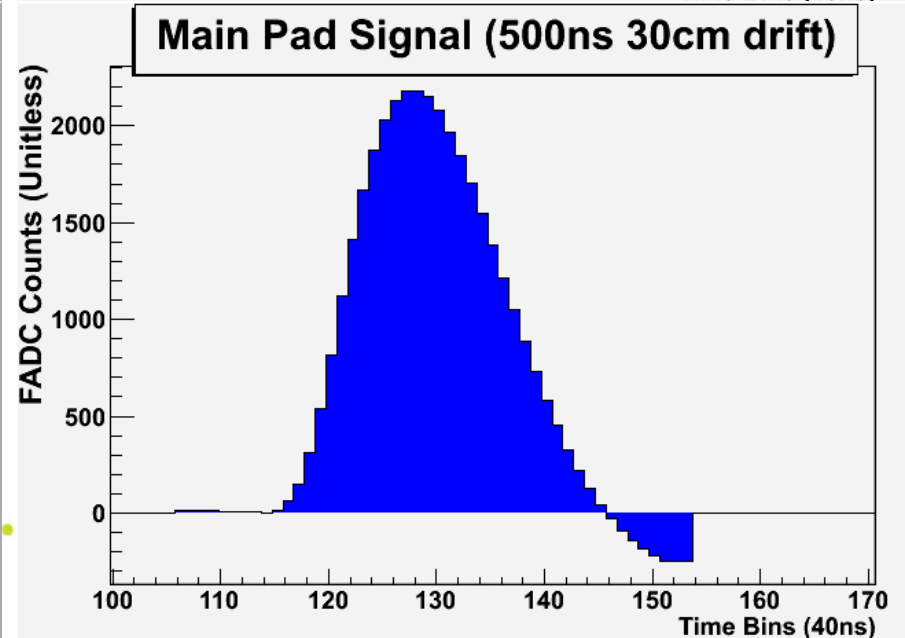
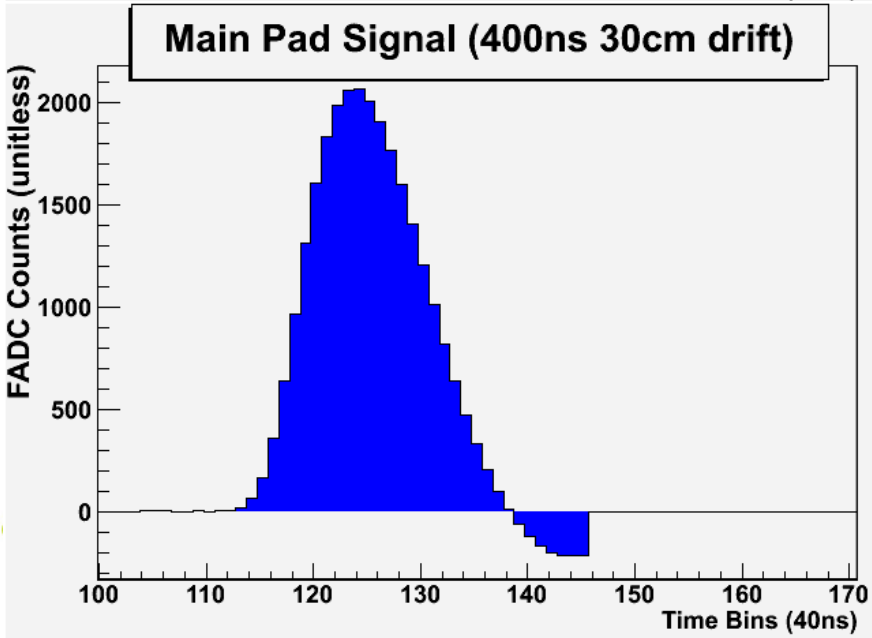
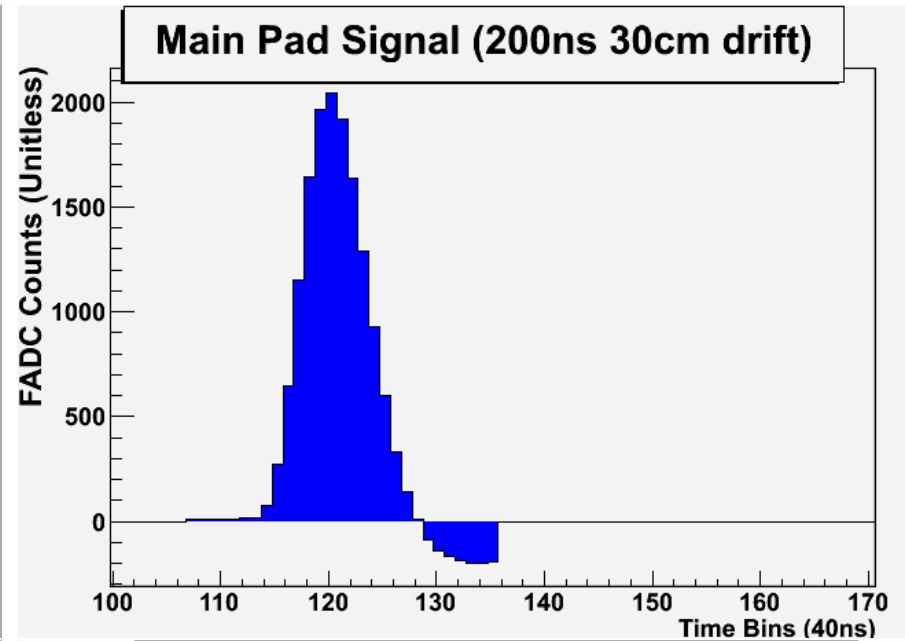
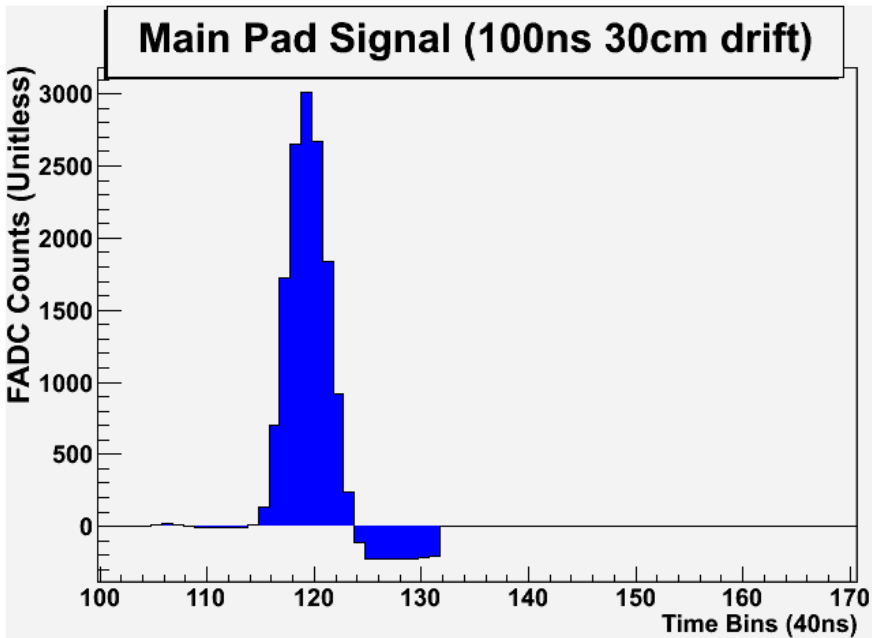
# Stand-Alone Calculation

Parameter	Initial value	Final value
Drift speed	76.98 um/ns	fixed
Transverse diffusion	95.4 um/root(cm)	fixed
Longitudinal diffusion	231.289 um/root(cm)	fixed
Resistivity	2.9 MOhm/sq	fixed
Glue thickness	75 um	fixed
Dielectric constant	4.5	2.66
Induction time	120 ns	166 ns
b (shaper)	3.7	3.42
$\tau$ (shaper)	151 ns	151 ns
Pad angular width	0.001984 rad	fixed
Pad height	6.84 cm	fixed
Lower radius of bottom row	1.522457785 m	fixed
$X_0$ track	event dependent	
$\phi$ track	event dependent	
Drift distance	30 cm	30 cm

NEED INPUT OF DESIGN ENGINEER AND ELECTRONIC EXPERT

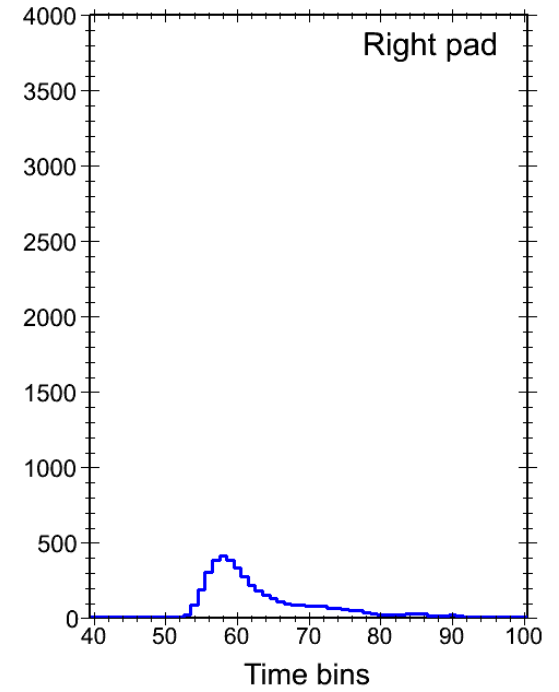
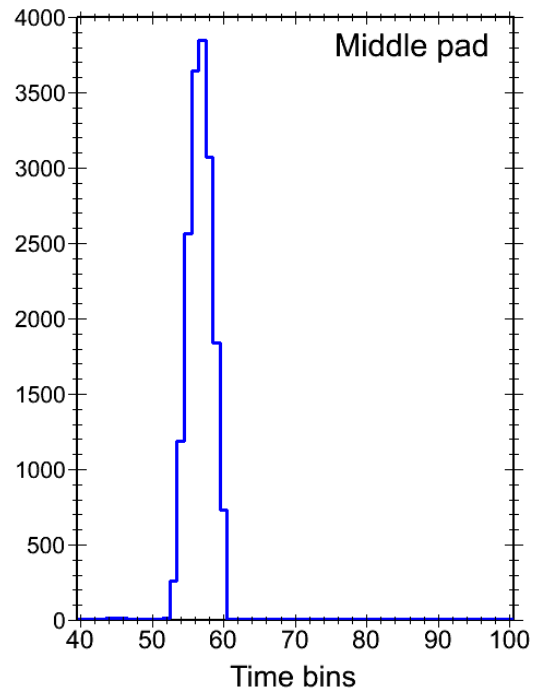
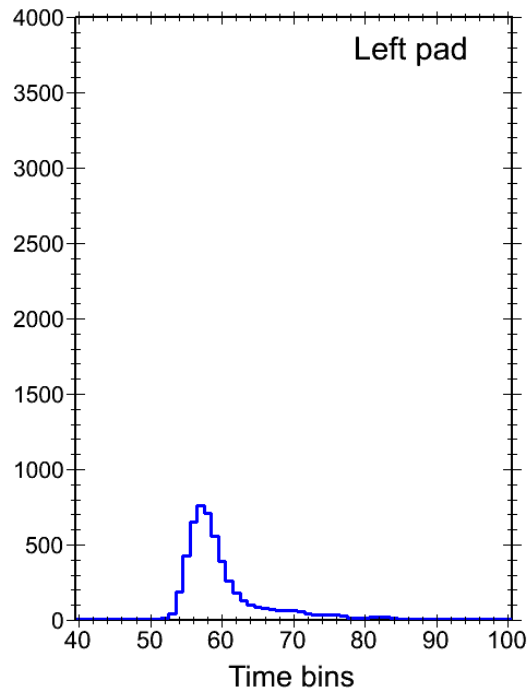


# Shaped Pulse (for different shaping time)





# Pad Amplitude

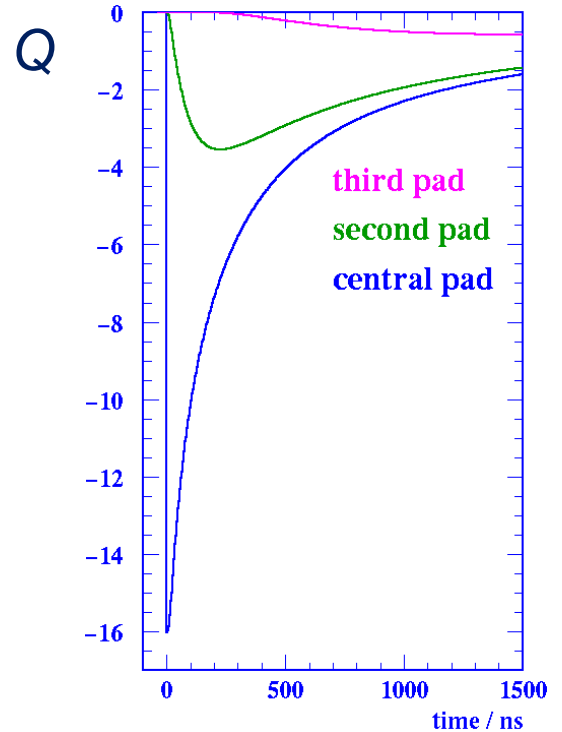
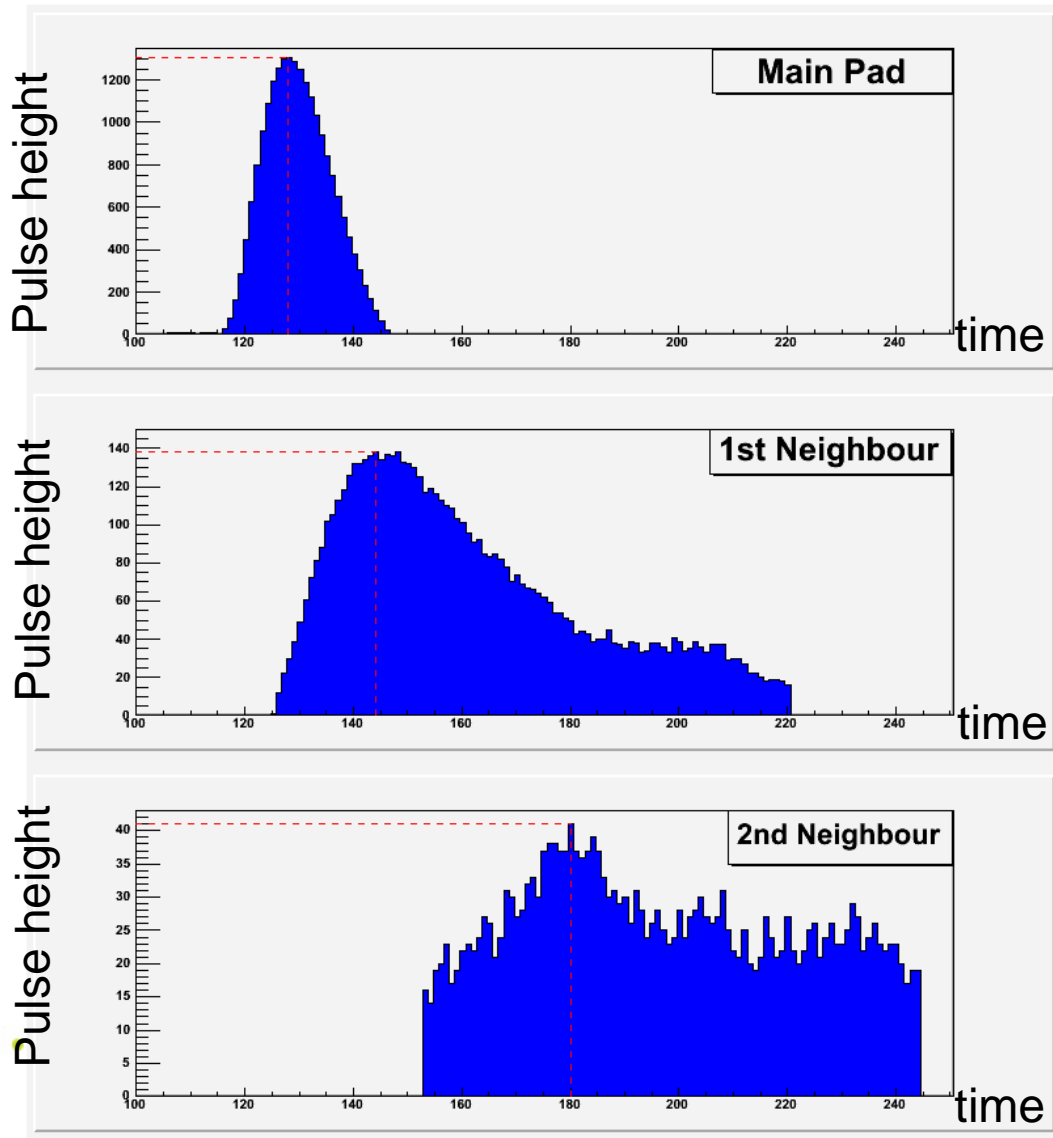


1) Use the maximum as the amplitude  
Single Point Maximum(SPM)

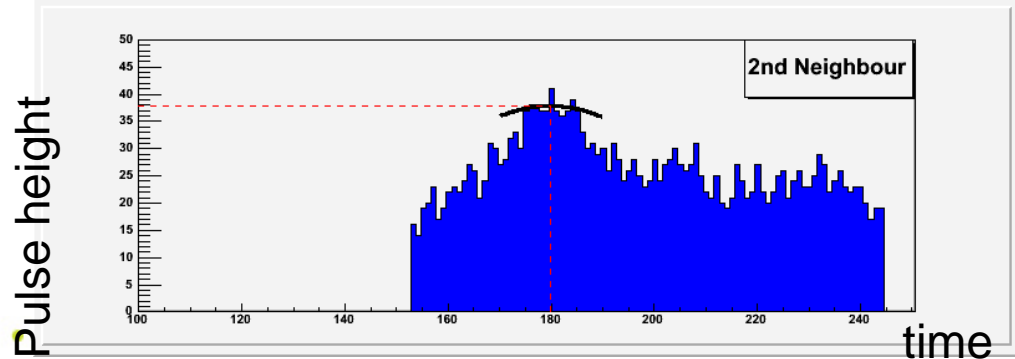
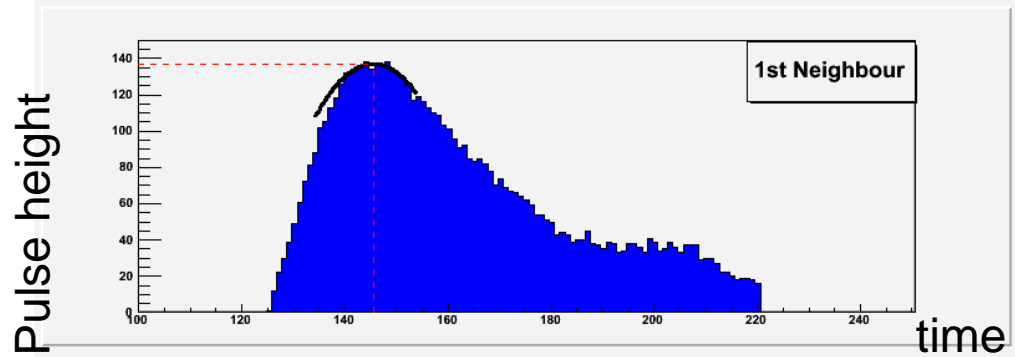
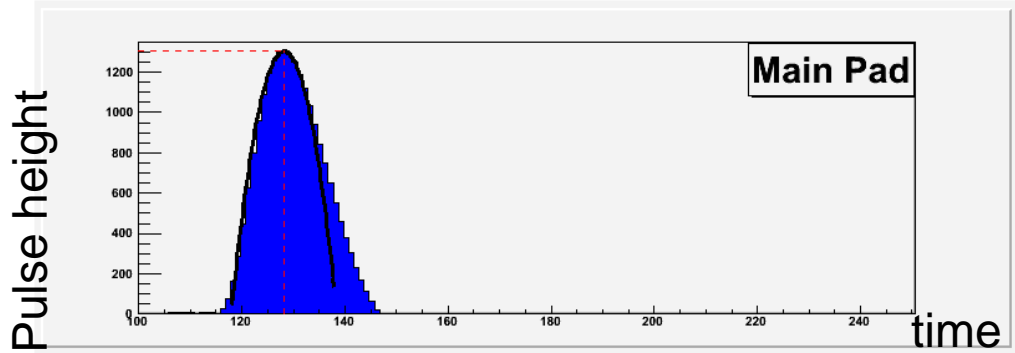
$$A_i = \max \text{ pulse height } P(i)$$

# Pad Amplitude

method used here

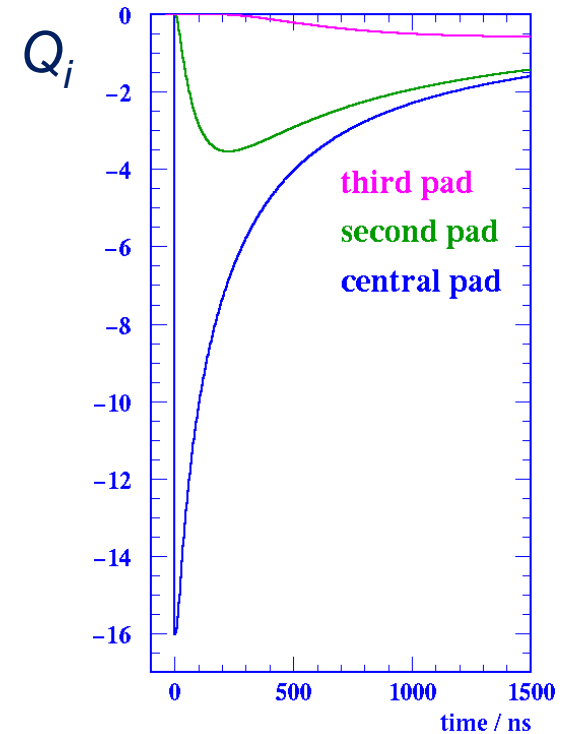


## 2) Maximum of Parabola Quadratic Fit Method (QFM) $A_i = \max$ of parabola $P(i)$



# Pad Amplitude

Method use pre-2011

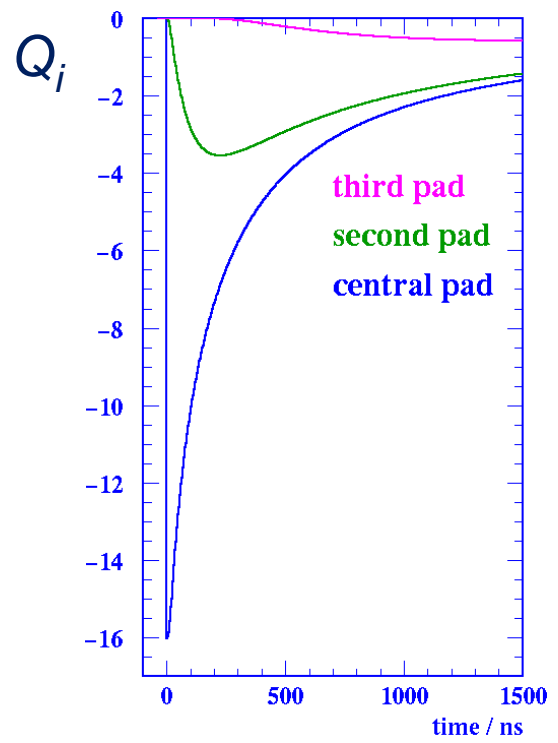
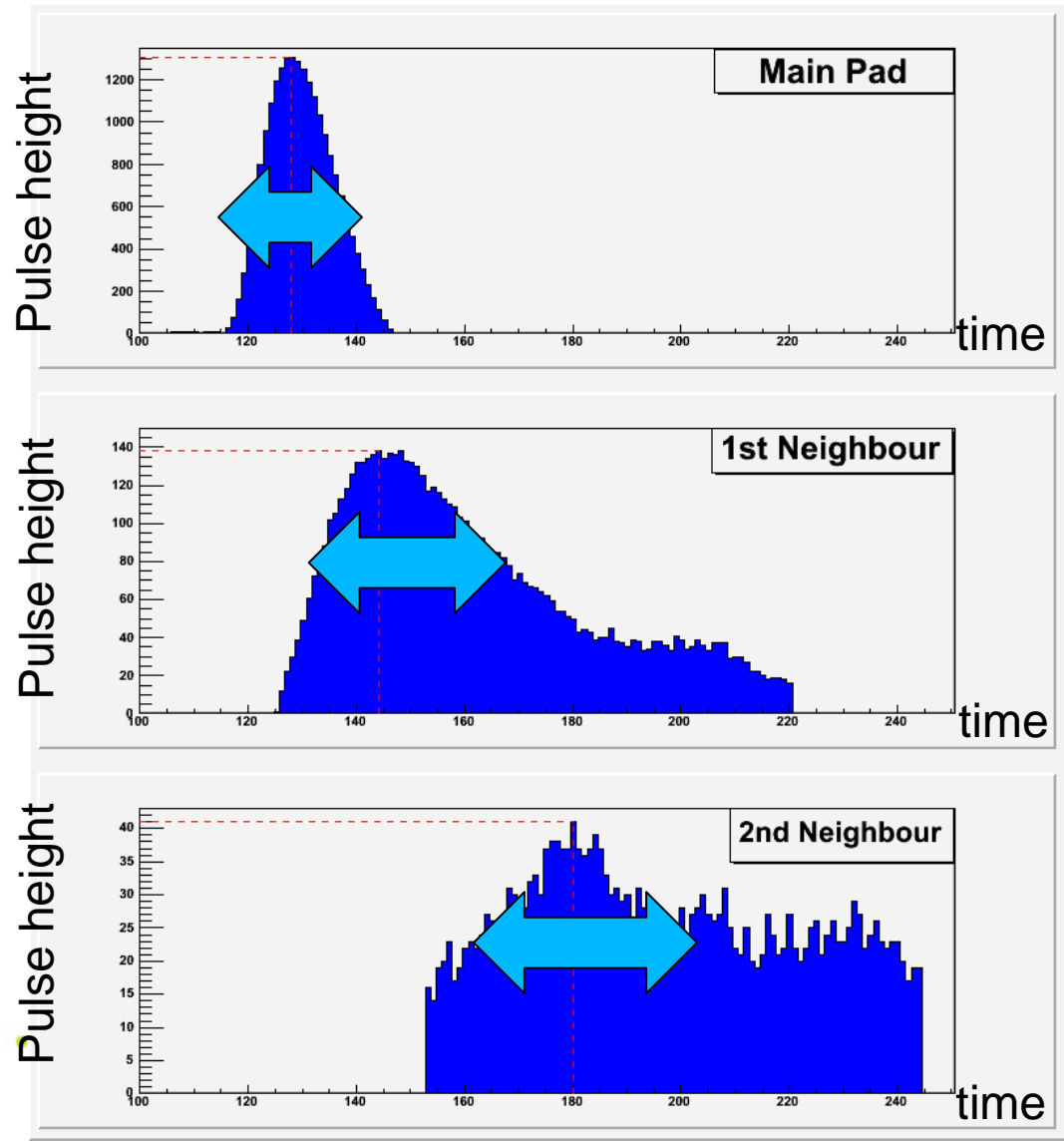


3) Integrate above threshold  
Re-integration method (RM)

$$A_i = \text{Sum } P(i)$$

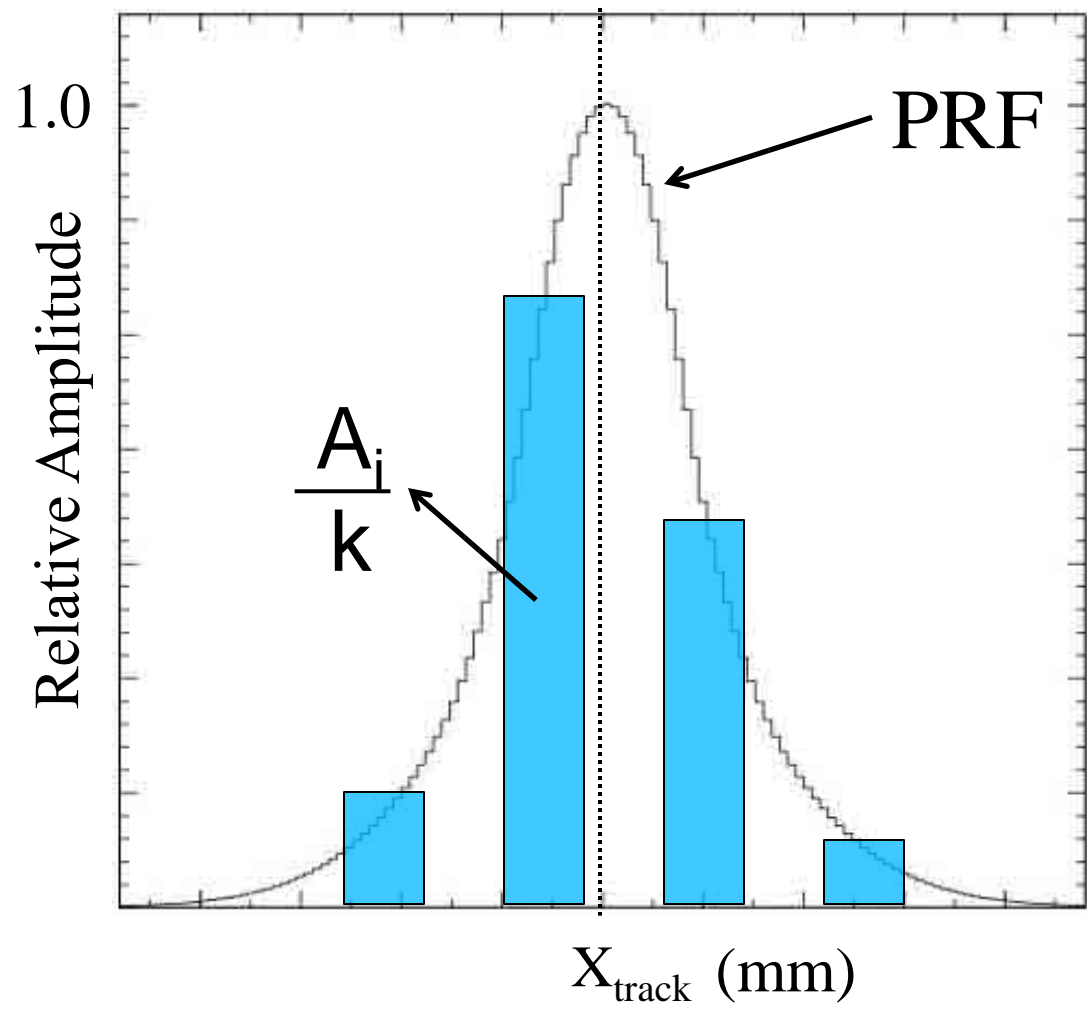
# Pad Amplitude

Method use in 2011



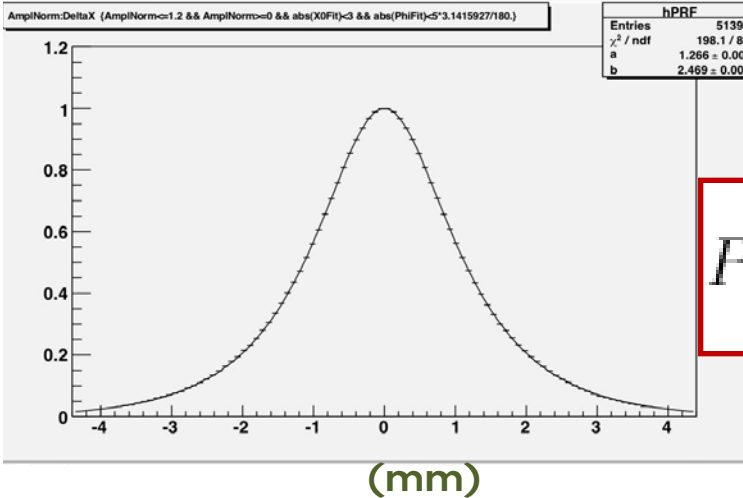
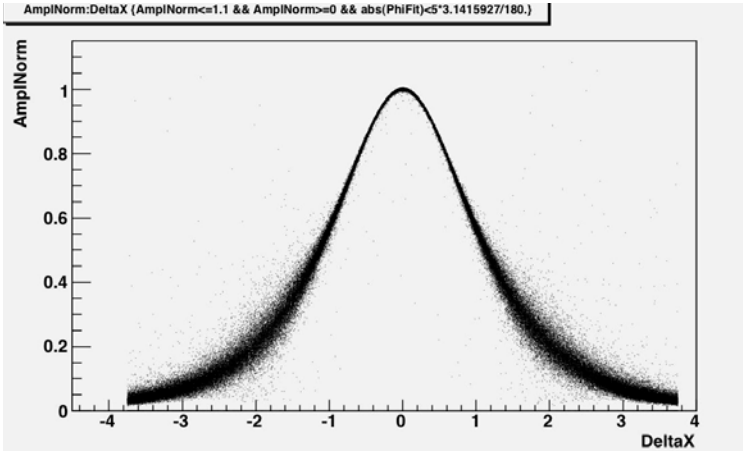


# Pad Response Function (PRF)

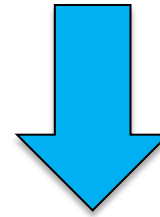


For a given  $X_{\text{track}}$  (known position) the PRF is defined to be unity

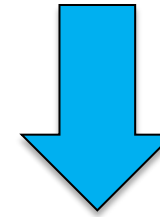
# Pad Response Function (model)



$$PRF(x, \Gamma, \Delta, a, b) = \frac{1 + a_2x^2 + a_4x^4}{1 + b_2x^2 + b_4x^4}$$



$$PRF(x, a, b) = b^2 \frac{e^{-\frac{x^2}{2a^2}}}{x^2 + b^2}$$



new (used here)

$$PRF(x; r, w) = \frac{\exp(-4\ln(2)(1-r)x^2/w^2)}{1 + 4rx^2/w}$$

- Only two parameters (simpler model)
- Easier to work with
- Better fits to data



# PRF versus Z

Micromegas

electron

mesh

anode

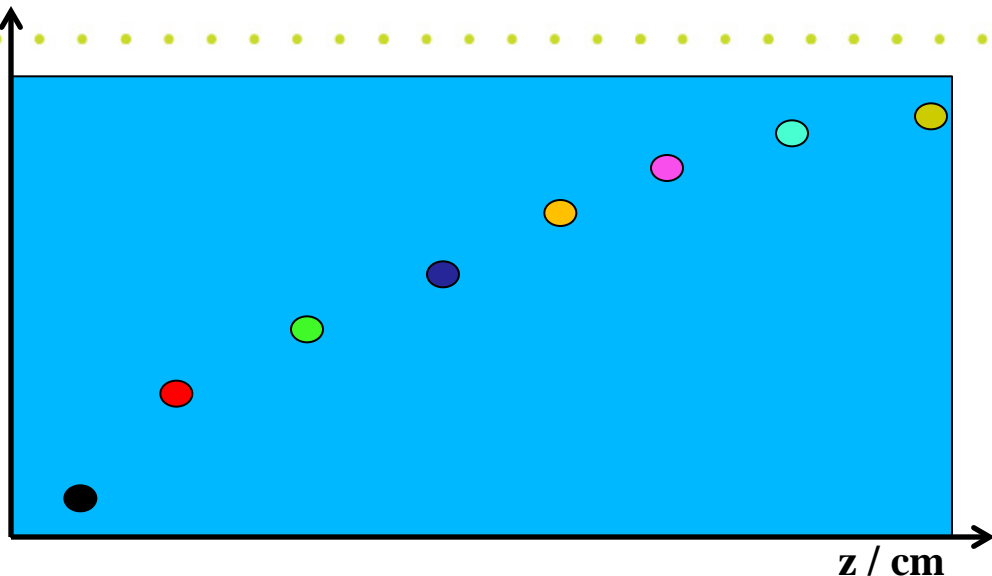
pads

avalanche

Direct signal

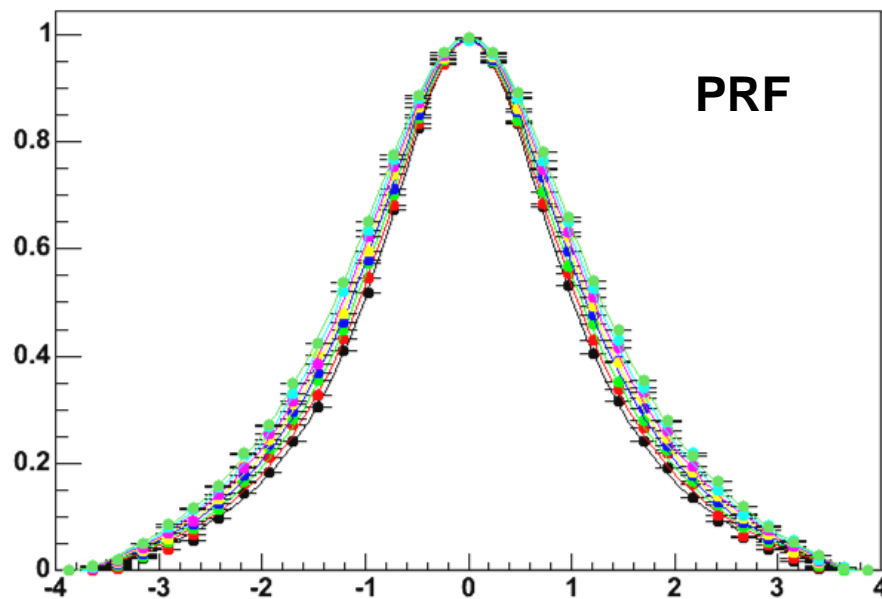
x

Width  
PRF



z / cm

relative amplitude



PRF

$x_{\text{pad}} - x_{\text{track}} / \text{mm}$

14 < z < 15cm

12 < z < 13cm

10 < z < 11cm

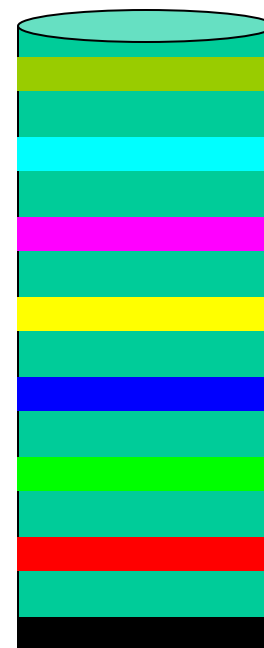
8 < z < 9cm

6 < z < 7cm

4 < z < 5cm

2 < z < 3cm

0 < z < 1cm



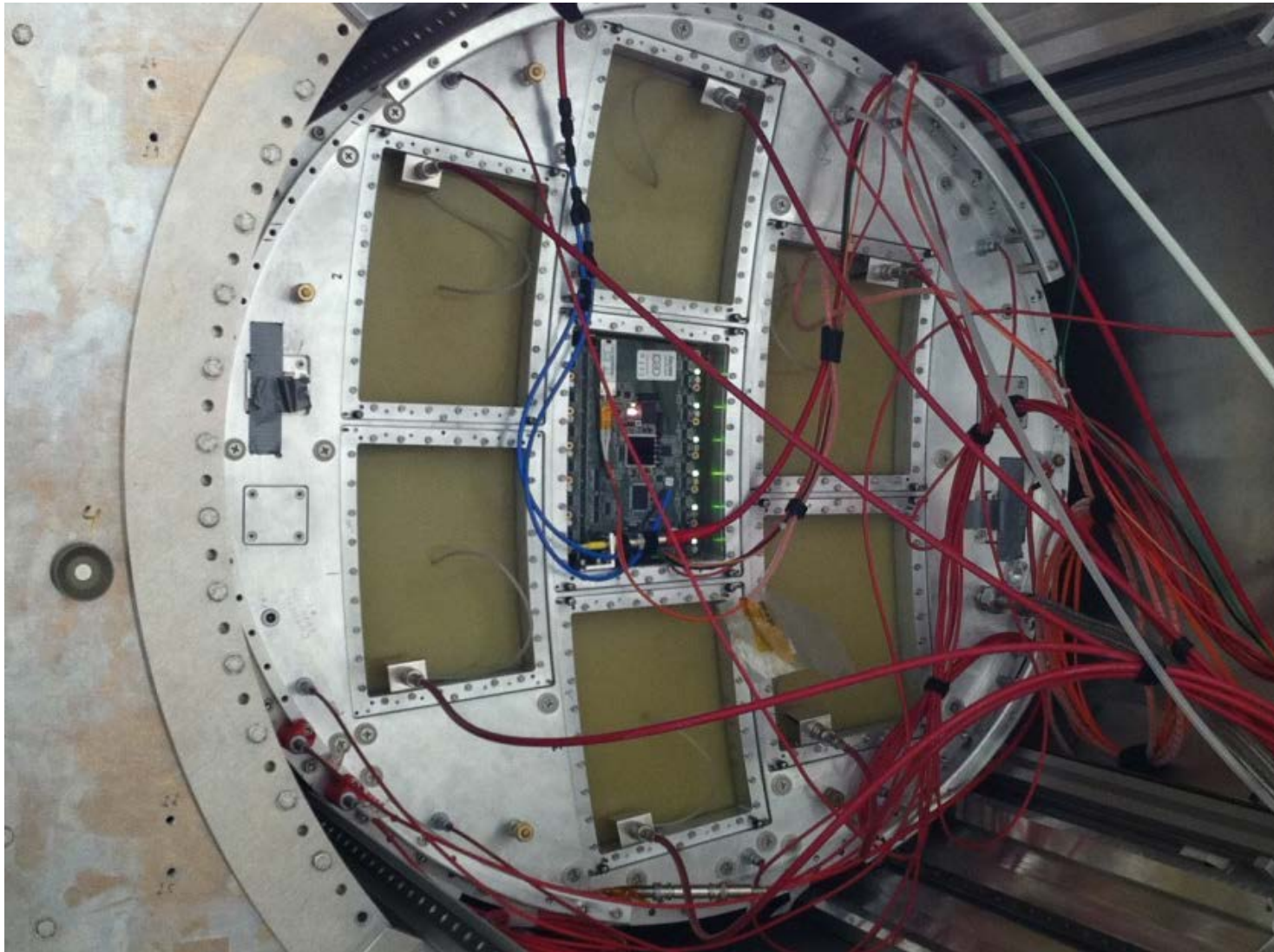
TPC



# Single Module LCTPC (MM)

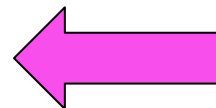
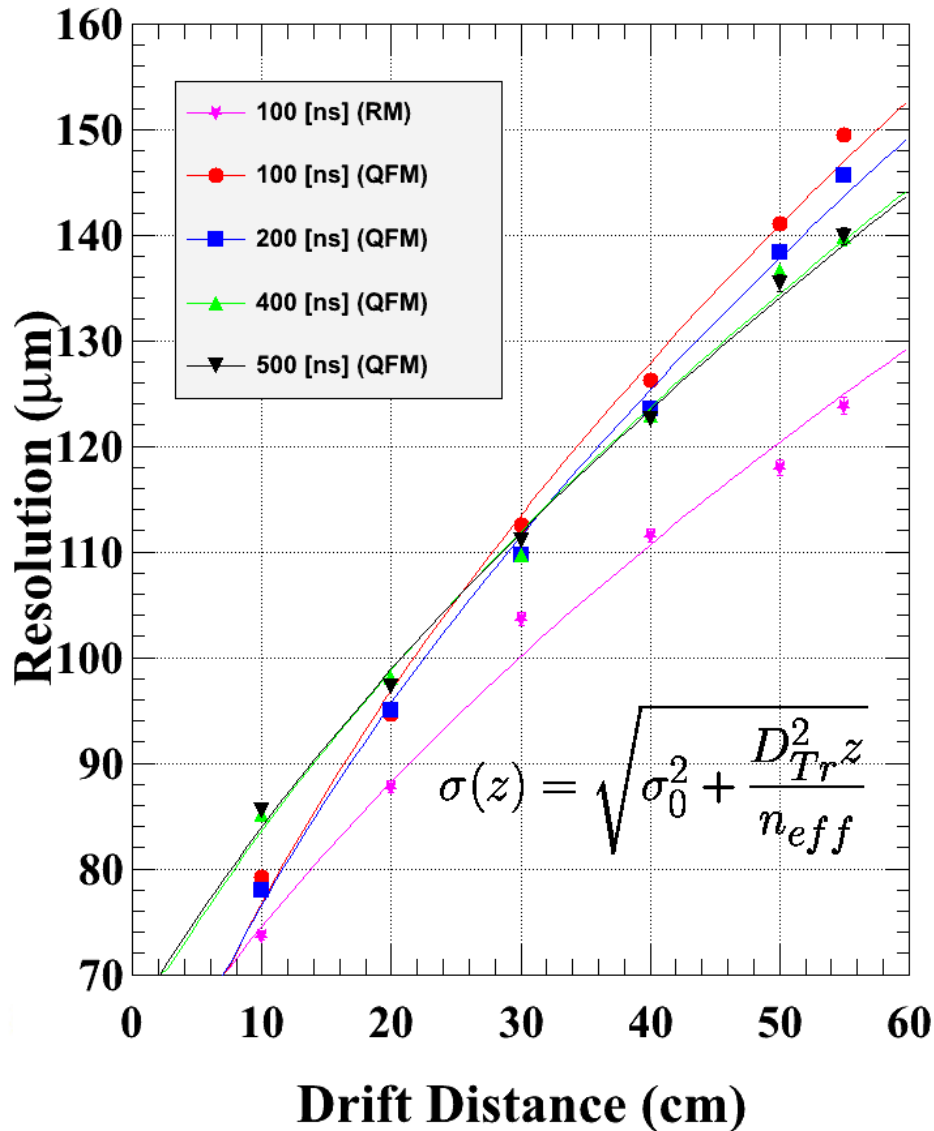
Period:  
2008-2011

2011 data  
Single module



# Transverse Resolution MM

Resolution v. Drift Distance (All Scans)



2011 data  
Single module

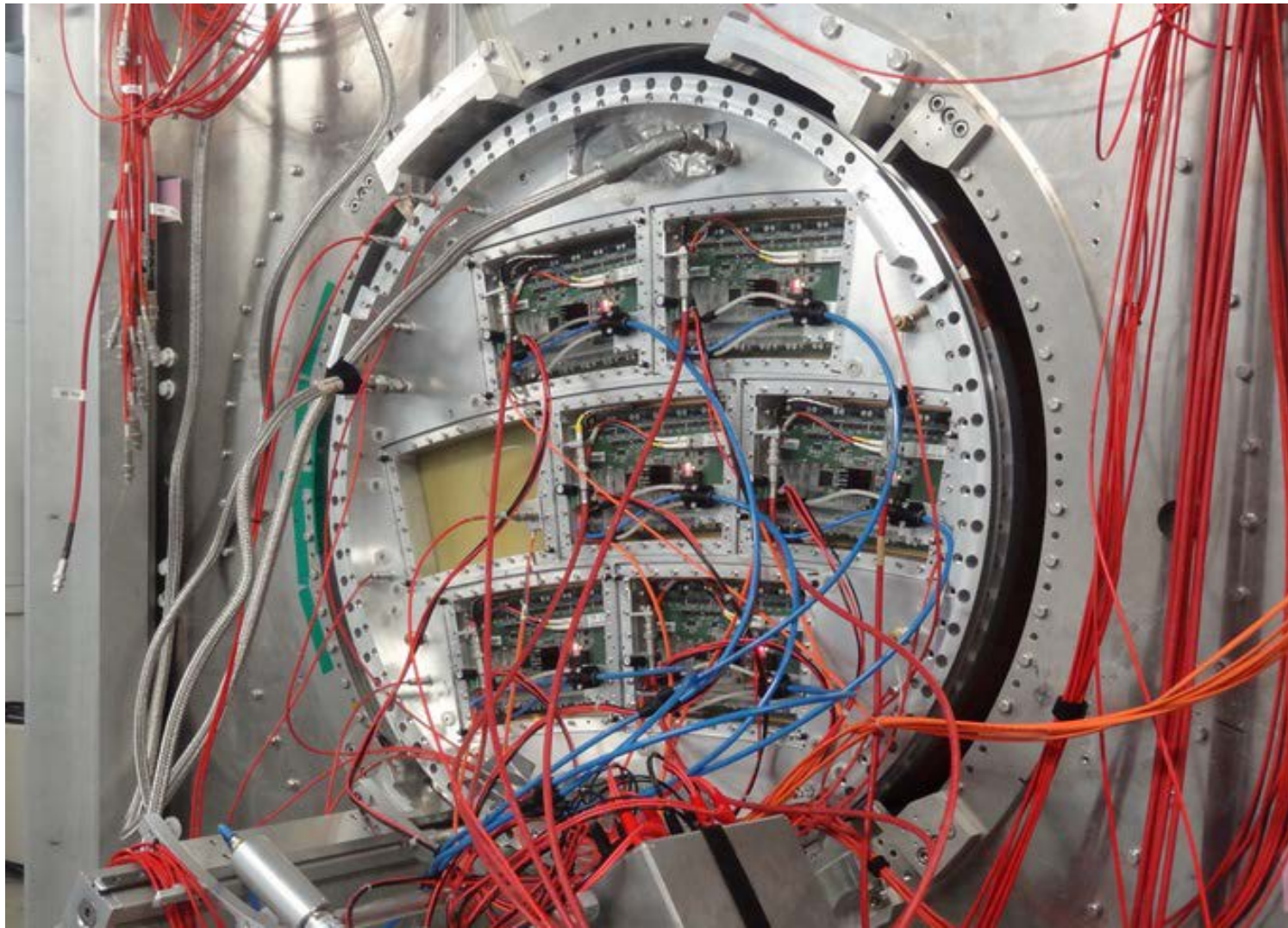
Source:  
Nicholi Shiell  
M.Sc. Thesis  
Carleton University



# 7-module LCTPC (MM)

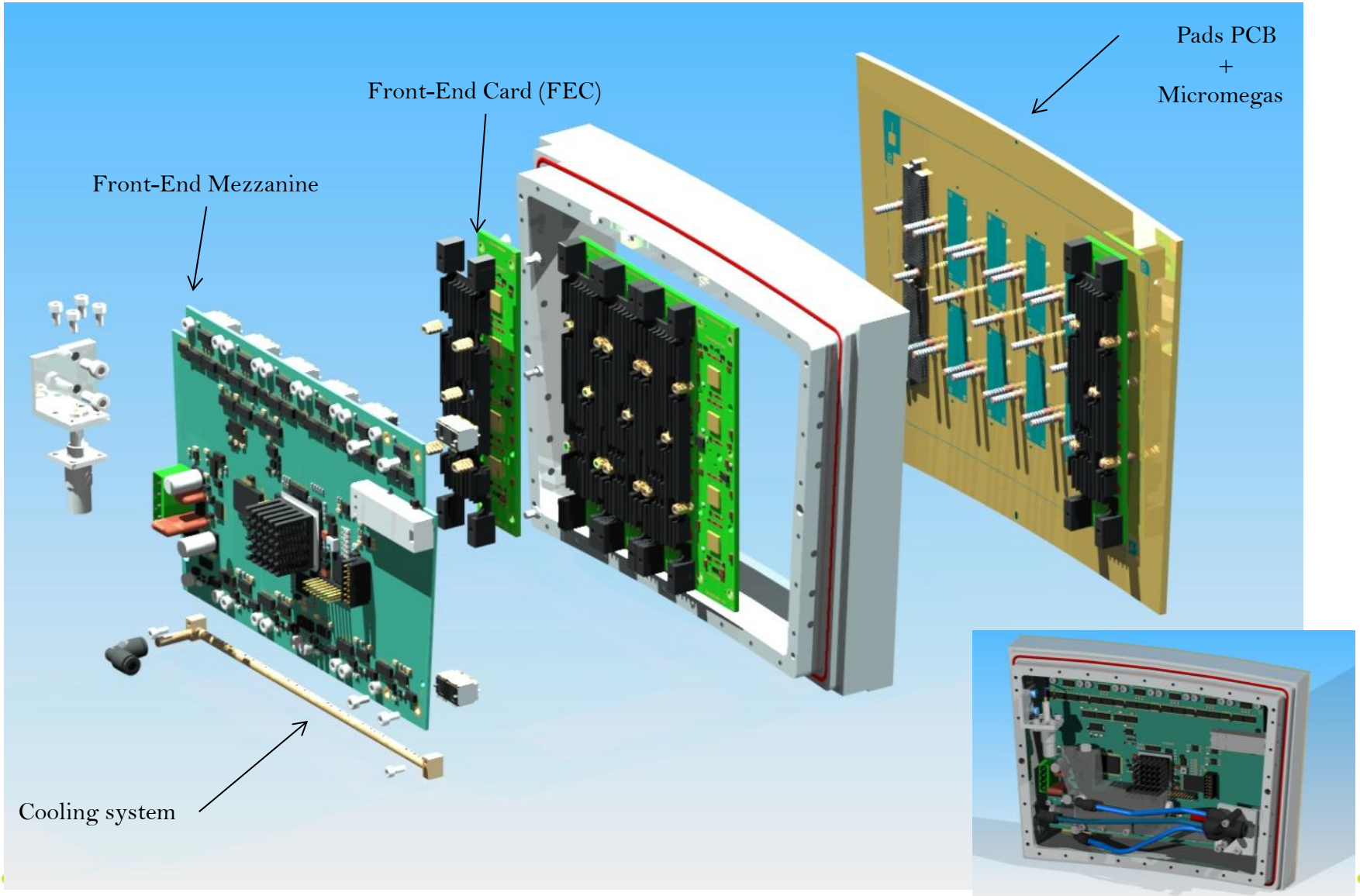
Period  
2012-2013

2013 data  
7-module

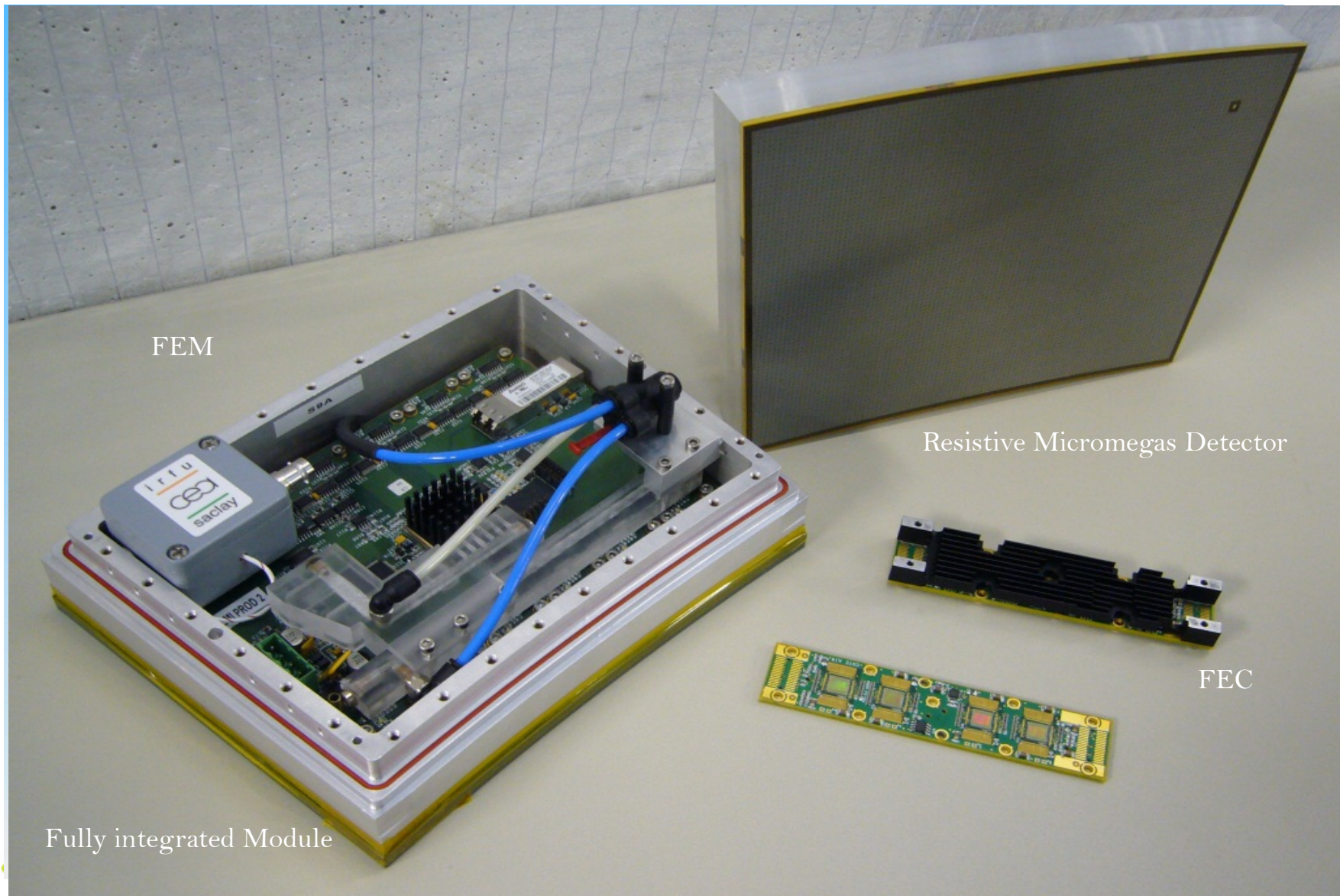




# Resistive MM: Module Design



# Resistive MM: Module Design



FEM

Resistive Micromegas Detector

FEC

Fully integrated Module



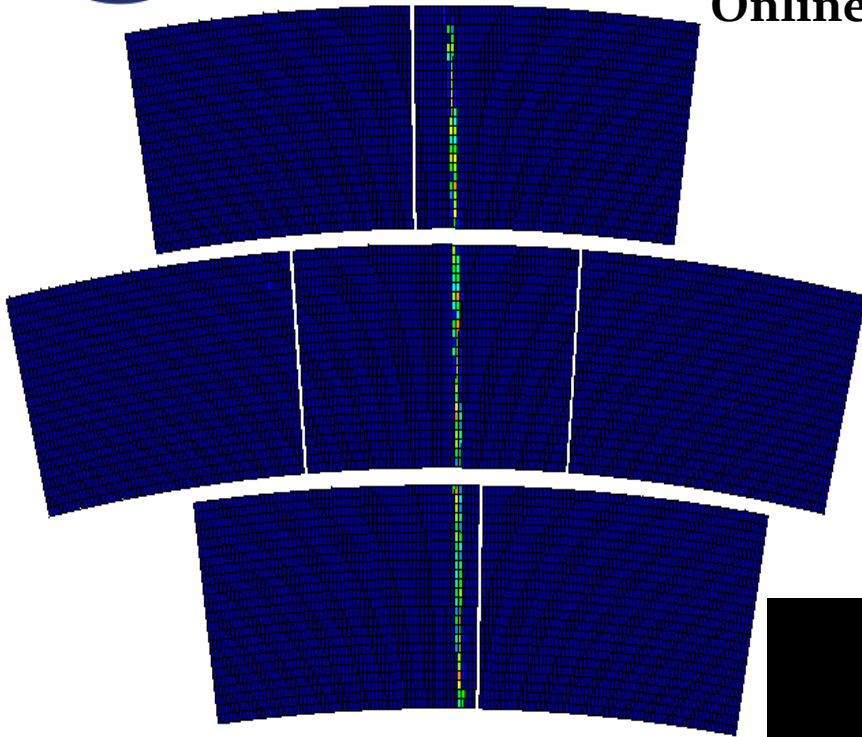
# Analysis Framework: MarlinTPC

- MarlinTPC (LCIO) is the global effort to develop a single analysis code package for all the different prototype TPCs being developed.
- It is far from complete, but it has a solid foundation
- Furthermore, not sustainable to rely on stand alone code with hardcoded geometry, stand alone track-fit algorithm, calibration constants, etc...
- MarlinTPC processors: calibration for PRF determination, bias corrections and resolution determination (transverse and longitudinal)



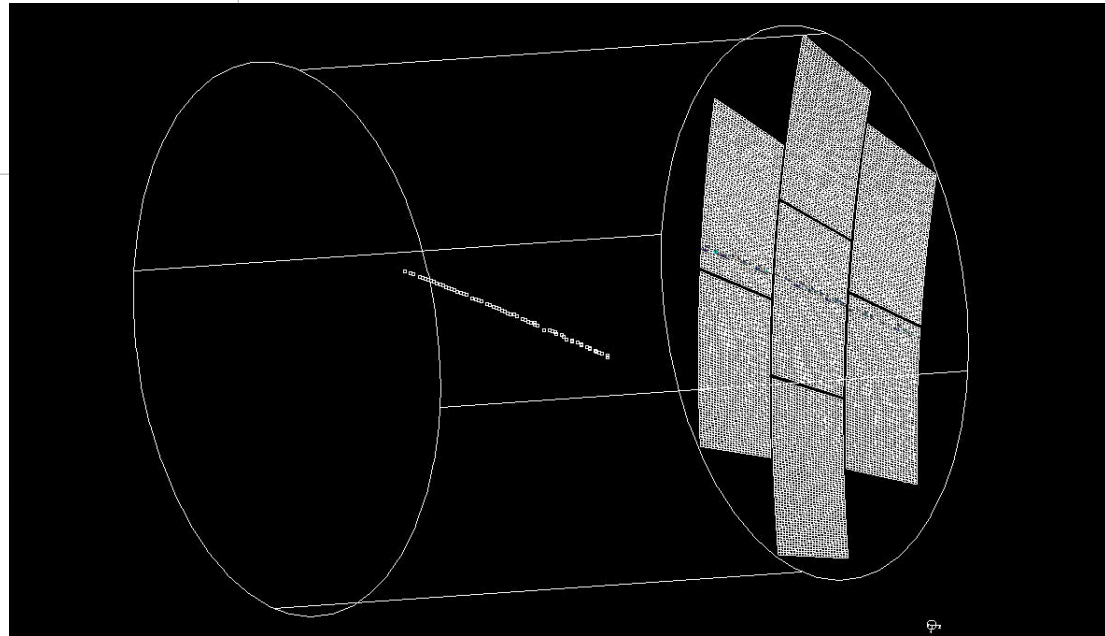
# Event Display: MarlinTPC

Online monitor



2D or 3D display  
software available

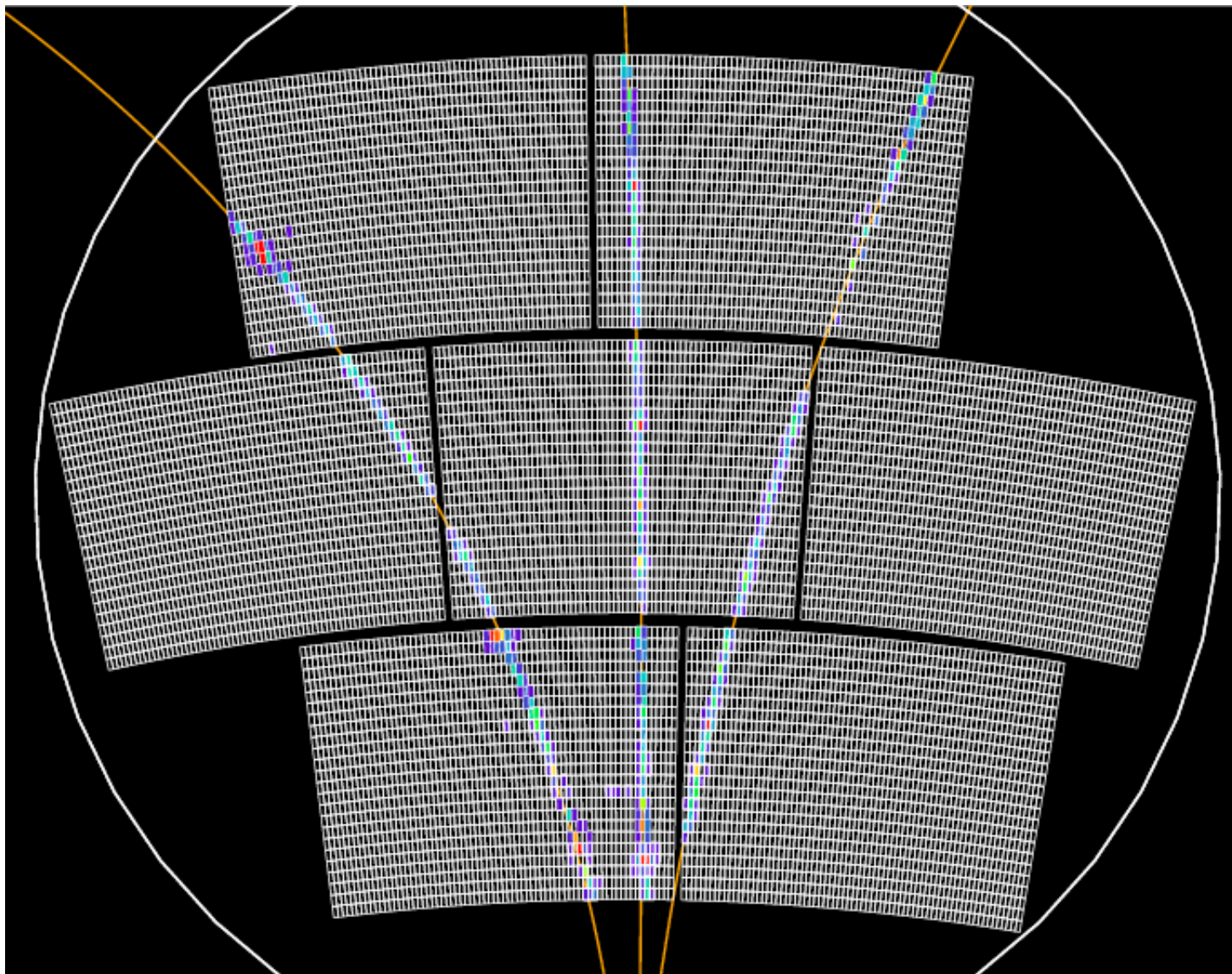
Offline monitor





# Multi-track Pattern Recognition

Kalman Filter within MarlinTPC – LCIO geometry



Acknowledgment:

Bo Li

Keisuke Fujii

Martin Killenberg



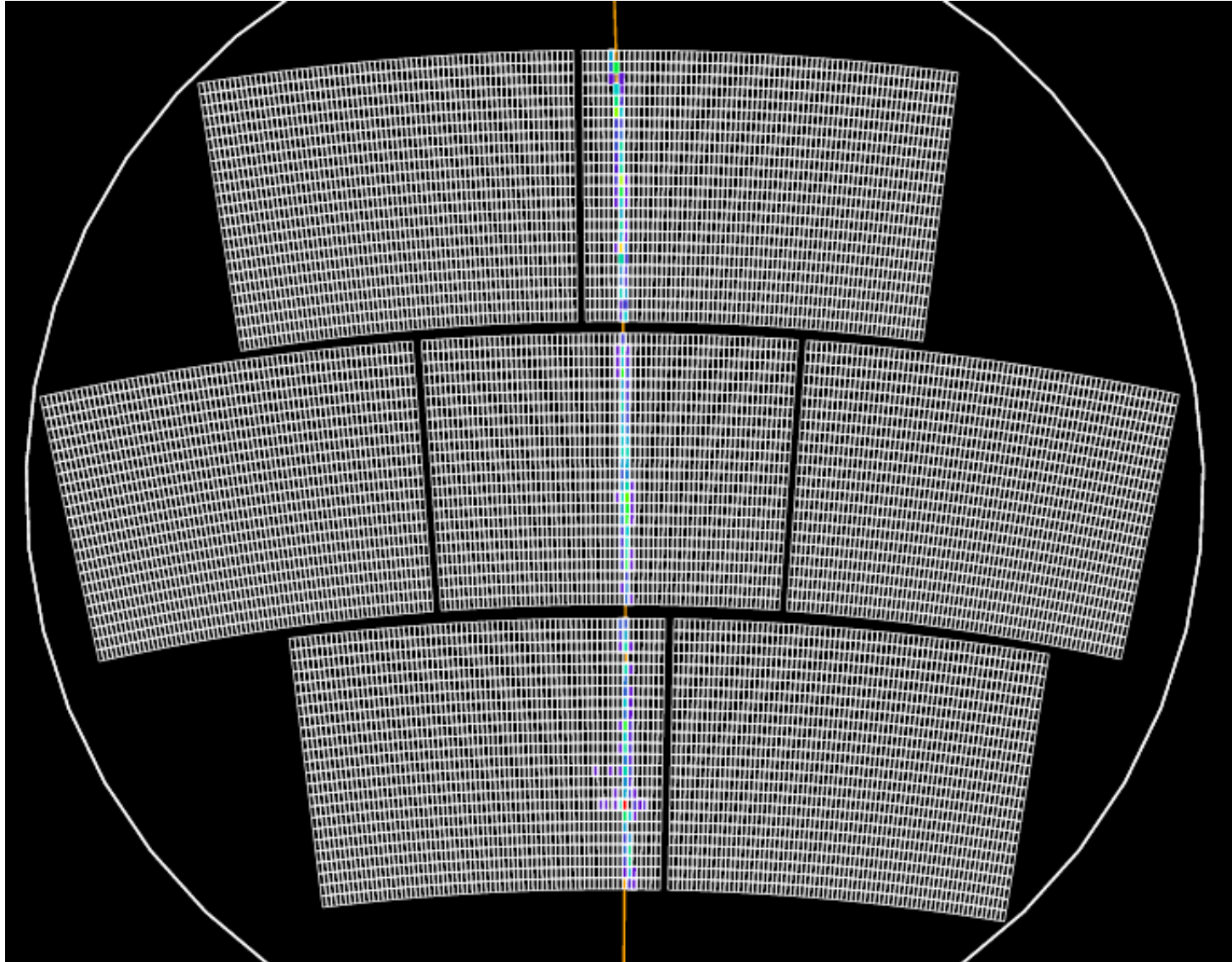
Carleton  
UNIVERSITY



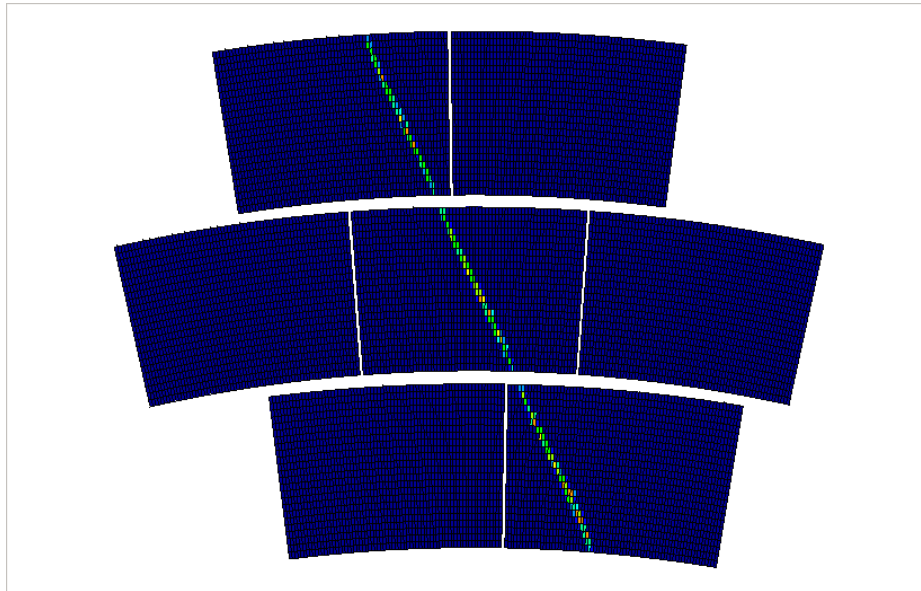


# Single-track events for calibration

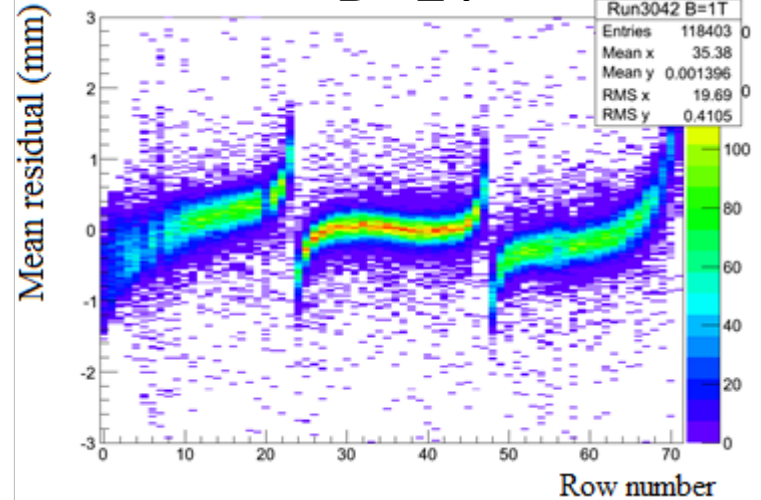
PRF calculation – bias – resolution study



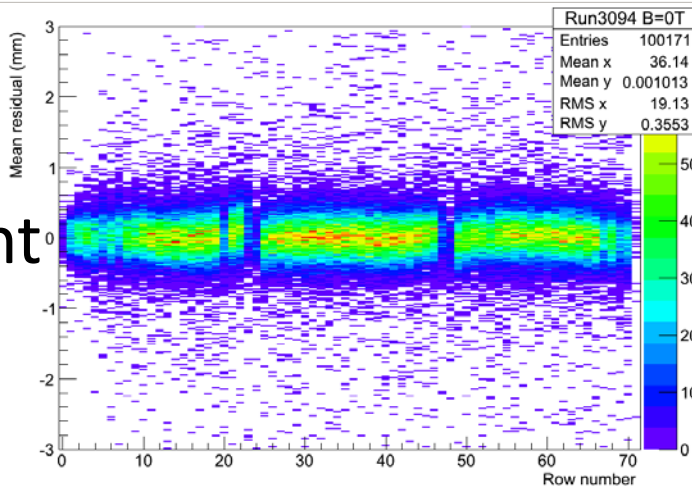
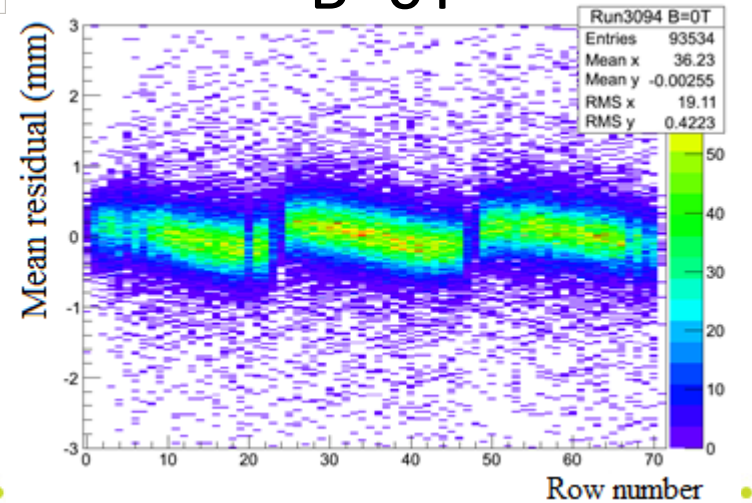
# Field Distortions (E x B effect)



B=1T

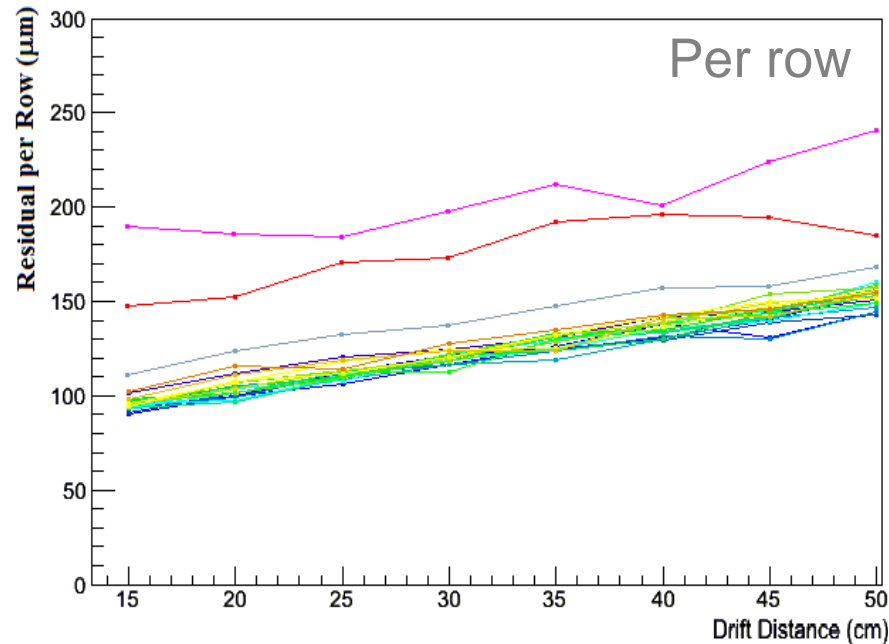


B=0T



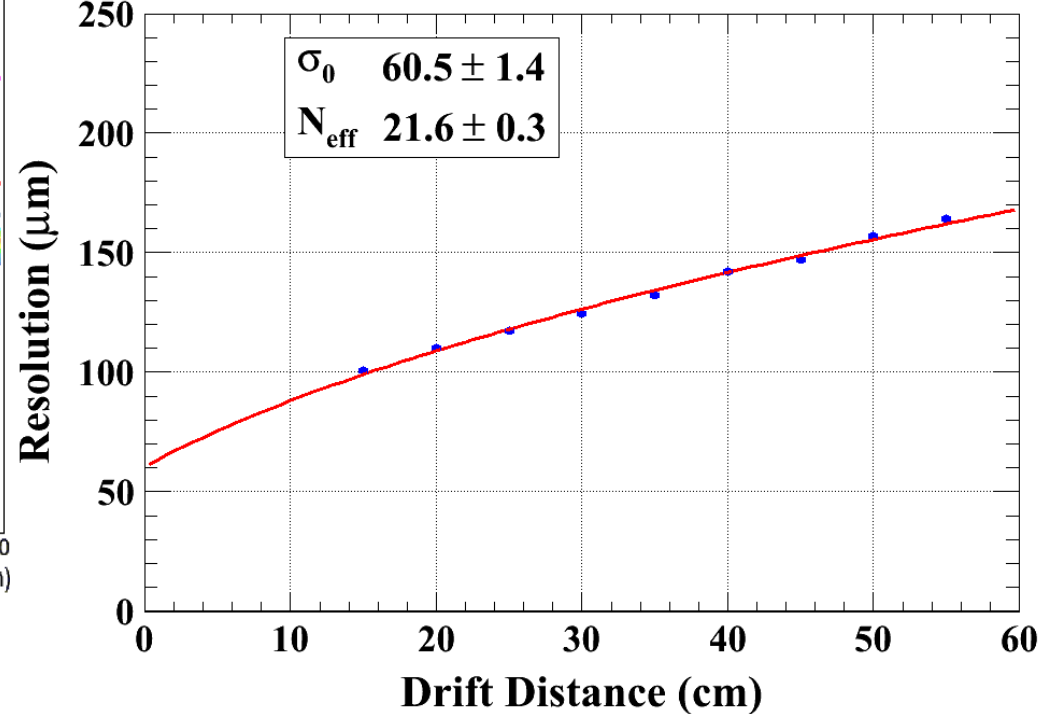
After alignment

2013 data  
7 module



$$\sigma = \sqrt{\sigma_0^2 + \frac{C_d^2 \cdot z}{N_{eff}}}$$

B=1 T  $C_d = 94.2 \mu\text{m}/\sqrt{\text{cm}}$  (Magboltz)

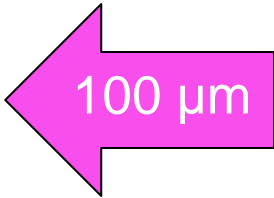
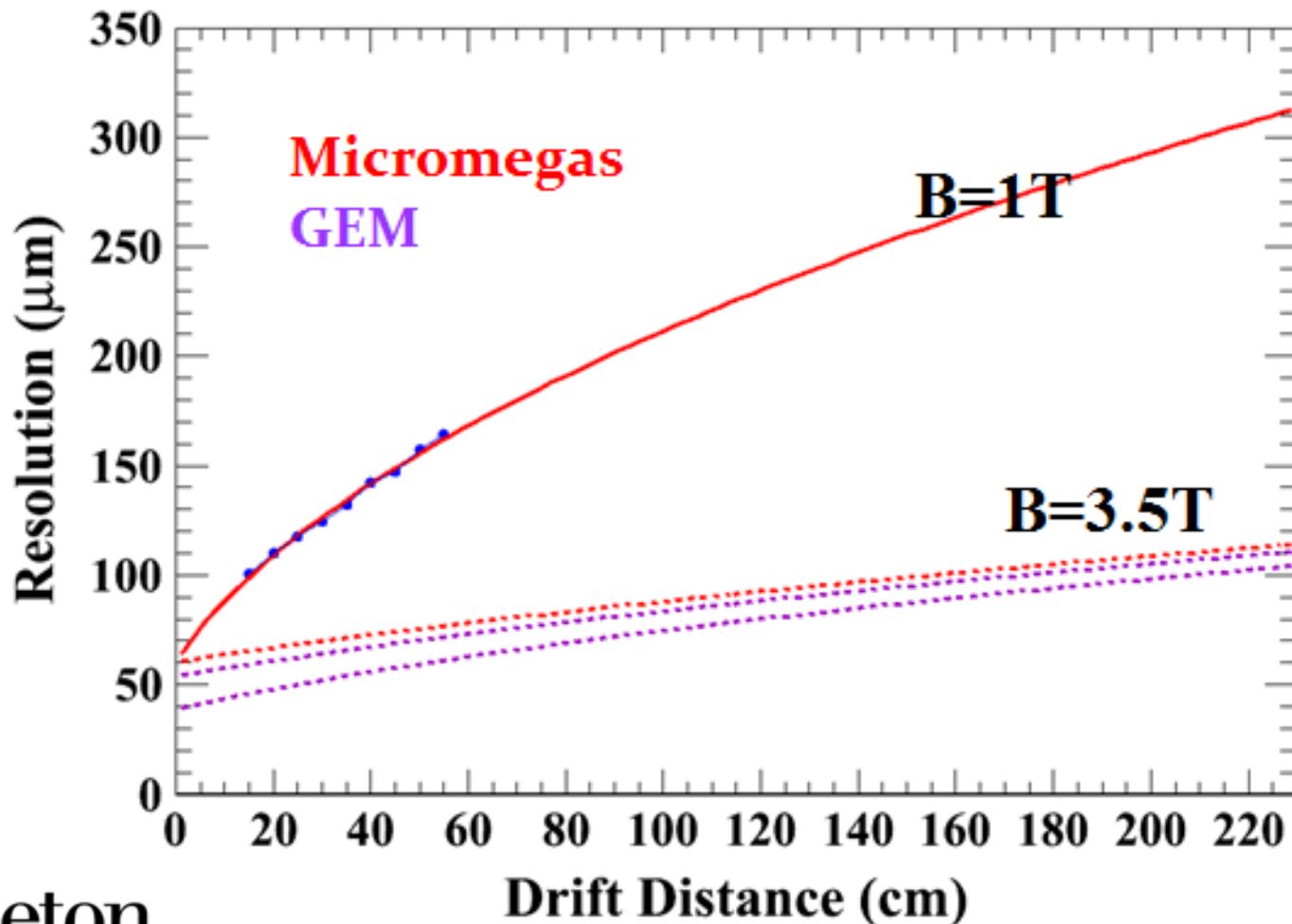


$\sigma_0$  : the resolution at Z=0  
 $N_{eff}$  : the effective number of electrons

# Transverse Resolution

Micromegas (MM) versus GEM

**Extrapolate to B=3.5T**



- A lot of experience has been gained in building and operating Micromegas TPC panels.
- The characteristics of the Micromegas modules, such as the uniformity, spatial resolution, stability have been studied in detail.
- **7 modules** have been successfully tested with full integration of the electronics at the same time. The modules have been manufactured and characterized in a quasi-industrial process.
- Thanks to the **resistive technology**, the measured resolution is about **60 microns** at zero drift distance with **3 mm** wide pads. This meets ILC requirements of 100  $\mu\text{m}$  single hit resolution in  $r\phi$  (over 2 m drift).